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## In this issue

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Foster-Seeley Discriminator
Coaxial Transmission Lines
Push-Pull Amplifier Design

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FEBRUARY 1958 Vol 35 new series No 2

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Established 1923
Published on the fifth of each month
ANNUALSUBSCRIPTION
(including Annual Index to Abstracts and References)
Home and Overseas f2 9s od Canada and U.S.A. $\$ 7.50$
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at New York, N.Y.

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## Automatic Testing

IN our complex civilization, the repair and maintenance of our complicated devices is a serious problem. In electrical and electronic apparatus, particularly, it is the diagnosis of the cause of the trouble which occupies so much time and effort.

In some cases, it is possible to apply automatic testing methods which not only indicate a fault at once but give a fairly precise indication of its nature and place. Such methods have been used for the automatic inspection of radio equipment as it comes off the production line. They are now being applied by the British Post Office for the testing of telephone circuits in automatic telephone networks.

In London, there are 2 million automatic telephones and 35 million calls a week and it is plain that routine testing and fault-finding is quite a problem.
One difficulty encountered is that a call between two exchanges may use any one of a large number of combinations of sections of line and pieces of exchange equipment. Thus, when a fault is reported, it is impracticable to repeat the particular combination of lines and exchange equipment with which the fault was observed. A piece of test equipment has recently been introduced which makes calls from the faulty number to special numbers at 100 or more exchanges. If these are received, the call is automatically answered and a $1,000-\mathrm{c} / \mathrm{s}$ tone returned to the calling number.

Another device assists engineers who are installing new telephones at subscribers' premises. When the instrument is ready for use, the engineer dials a special number which connects the subscriber's line to test equipment at the exchange. A complete series of tests is accomplished in about 15 seconds and, if any test fails, the engineer is informed verbally by means of a magnetic recording on a drum at the exchange. Transistors are used in the amplifiers associated with the recording, since the required circuitry is compact and a ready source of supply voltage is available in the form of the exchange battery.

A third equipment tests the insulation resistance of telephone lines at the rate of about 600 lines per hour. (Several tests are carried out on each line.) It thus becomes practicable to test lines sufficiently often to observe the gradual deterioration of a line and repair it before it develops a definite fault.
These are automatic methods which perhaps as yet can hardly be called automation. Their purpose is to speed up testing and to relieve engineers of much routine work. The time has not yet come when a piece of electronic apparatus will announce through its loudspeaker 'Please replace $\mathrm{R}_{39}$ '. That is now possible, but it may never come, for we suspect that the automatic testing equipment would be so complex that it would have a higher probability of faults than the equipment it was designed to test!
In test apparatus, as in everything else, it is necessary to exercise a fine discrimination and to guard against the tendency to over-elaboration.

# Total Differential Feedback 

A DEVICE FOR SQUARING THE EFFECTIVE POSSIBLE FEEDBACK IN A FEEDBACK AMPLIFIER

By J. C. H. Davis*

In feedback amplifiers, such as those used as line amplifiers in frequency division multi-channel systems, which may, for example, have a bandwidth of six octaves and require more than 25 dB of feedback in order to suppress intermodulation products, there is a definite maximum amount of feedback which can be applied for given valve characteristics ${ }^{1}$. This limit is set primarily by the slopes and interelectrode capacitances of the valves used, which determine the maximum possible interstage impedances. Particularly in multistage amplifiers the limit may appear as loop instability

Fig. 1. Two methods of applying total differential feedback

resulting in oscillations far outside the transmission band.
The principle of total differential feedback may overcome this limitation. The term is used to describe circuits in which the difference between the input signal to one amplifying path and the total signal fed back by its associated loop is applied to the input of another amplifying path, as shown in Fig. 1. The two output signals are combined in such a way that the transmission gain of the complete amplifier is substantially that of either path with the other path dead, while the gain stability, harmonic margiris and signal-to-noise ratios produced other than at the grid of the first stage are improved ${ }^{2}$. If each amplifying path has $A \mathrm{~dB}$ of feedback applied to it, the effective feedback on the complete amplifier is practically that expected from a single path with $2 A \mathrm{~dB}$ of feedback applied. This is achieved without the additional stability penalty resulting from this amount of feedback in a single loop and also has the advantage that, if one path goes dead, the other path maintains the transmission with $A \mathrm{~dB}$ of feedback.

## The Theory of Single-Stage Amplifying Paths

Fig. 2 shows the simplified circuit diagram of a singlestage feedback amplifier; $i_{x}$ represents a current source of distortion products in the valve of slope $g_{1}$.
The total current in $Z_{2}$

$$
I=i_{1}+i_{x}=\left(e_{i n} / Z_{1}\right)\left[1-1 /\left(1+g_{1} Z_{1}\right)\right]+i_{x} /\left(1+g_{1} Z_{1}\right)
$$

This may also be written

$$
\begin{equation*}
I=\left(e_{i n} / Z_{1}\right)\left[g_{1} Z_{1} /\left(1+g_{1} Z_{1}\right)\right]+i_{x} /\left(1+g_{1} Z_{1}\right) \tag{1}
\end{equation*}
$$

This shows the normal stabilization of gain and reduction of noise due to the feedback $g_{1} Z_{1}$.
The voltage between grid and cathode

$$
\begin{align*}
& =e_{i n}-e_{1} \\
& =e_{i n}-I Z_{1} \\
& =e_{i n} /\left(1+g_{1} Z_{1}\right)-i_{x} Z_{1} /\left(1+g_{1} Z_{1}\right) \tag{2}
\end{align*}
$$

using Equ. (1).
Let this voltage difference be applied to an amplifying path whose effective slope is $I / Z_{1}$ and the resulting output current be added to $I$.
The combined output current $=e_{i n} / Z_{1}$ exactly.
This depends on the effective slope of the second amplifying path being exactly $1 / Z_{1}$. In practice, a sufficiently close approximation can be achieved.
Figs. 3(a) and 3(b) show two methods of connecting che second path, corresponding to Figs. 1 (a) and 1 (b).

[^2]In Fig. 3(a) a three-winding output transformer is required where the ratio of the turns on windings $A$ and B will normally be 1: l. Similarly, the transformer at the input in Fig: 3(b) will normally have a turns ratio $1: 1$. When this is so, $Z_{1}=Z_{3}$. The turns ratio of windings A and C in Fig. 3(a) are shown as $1: 1$ for convenience in analysis.

The current in $Z_{2}$ due to $i_{2}$; i.e., $k i_{2}$ in Fig. 3 (a) and $i_{2}$ in Fig. 3 (b)

$$
\begin{align*}
& =\frac{k\left(e_{i n}-e_{1}\right)}{Z_{3}} \cdot \frac{g_{2} Z_{3}}{1+g_{2} Z_{3}} \\
& =\frac{k}{Z_{3}} \cdot \frac{e_{i n}-i_{x} Z_{1}}{1+g_{1} Z_{1}} \cdot \frac{g_{2} Z_{3}}{1+g_{2} Z_{3}} \tag{3}
\end{align*}
$$

using Equ. (2). Here $g_{2}$ is the slope of the second valve and $k$ the turns ratio of the transformer as shown. The addition of equations (1) and (3) gives the total output current.

$$
\begin{align*}
& =\frac{e_{i n}}{Z_{1}} \frac{g_{1} Z_{1}\left(1+g_{2} Z_{3}\right)+k g_{2} Z_{1}}{\left(1+g_{1} Z_{1}\right)\left(1+g_{2} Z_{3}\right)}+\frac{i_{x}}{1+g_{1} Z_{1}} \\
& \quad\left(1-\frac{k Z_{1}}{Z_{3}} \frac{g_{2} Z_{3}}{1+g_{2} Z_{3}}\right) \\
& =\frac{e_{\text {in }}}{Z_{1}}\left[1-\frac{1}{\left(1+g_{1} Z_{1}\right)\left(1+g_{2} Z_{3}\right)}\right] \\
& \quad \quad+\frac{i_{x}}{\left(1+g_{1} Z_{1}\right)\left(1+g_{2} Z_{3}\right)} \text { when } \frac{k Z_{1}}{Z_{3}}=1 \tag{4}
\end{align*}
$$

Comparison of Equs. (1) and (4) shows that both the gain stabilization and the harmonic suppression have been increased by a factor ( $1+g_{2} Z_{3}$ ). This has been done without, in simple theory, affecting the feedback loop of the first path.

If $g_{1}$ or $g_{2}$ is zero ; i.e., if either path fails, the output current

$$
=\frac{e_{i n}}{Z_{1}}\left(1-\frac{1}{1+g Z}\right)+\frac{i_{x}}{1+g Z}
$$

The extra feedback is removed but the amplifier continues to operate with substantially the same gain as before.


While noise in the first path is suppressed, noise in the second path is added. However, the voltage fed to the second path $=e_{i n}-e_{1}=e_{i n} / g_{1} Z_{1}$ approx., so that this path works at a much lower level than the first and produces correspondingly negligible noise and harmonics.
The amount of effective feedback added from the second path depends on how closely $1-\left(k Z_{1} / Z_{3}\right)$ $g_{2} Z_{3} /\left(1+g_{2} Z_{3}\right)$ approximates to zero. If $k Z_{1} \mid Z_{3}=1$ and the second path has 20 dB of feedback, $g_{2} Z_{3}=10$ and $1-\left(k Z_{1} / Z_{3}\right) g_{2} Z_{3} /\left(1+g_{2} Z_{3}\right)=1 / 11$. If the feedback is very large, the amount of effective feedback which can be added to the first path depends on the accuracy of $k Z_{1} / Z_{3}$. For the limit of added feedback to be $20 \mathrm{~dB}, k Z_{1} / Z_{3}=10 / 11$; i.e., $k Z_{1} / Z_{3}=1 \pm 9 \%$. As this assumes a large amount of feedback in the second path, the accuracy will have to be greater than this when the feedback in the second path approaches 20 dB , but it can be seen that the required accuracy is not very high ; e.g., if the feedback in the second path is 20 dB and $k Z_{1} / Z_{3}=1 \pm 4 \%$ the effective feedback added to the first path is 17 dB .

In principle, it should be possible to add a third path to increase the apparent feedback on the second path and thus on the first. This could be extended indefinitely, but the limit of usefulness is set by the accuracy of the expression $k Z_{1} / Z_{3}=1$ which controls the maximum amount of feedback which can be added to the first path from all subsequent paths.

It is of interest to see what the effect of a catastrophic

Fig. 3. Two single-stage negative-feedback amplifiers connected as in Fig. 1 to take advantage of total differential feedback



Fig. 4. A circuit using a two-stage amplifier in one path and a three-stage amplifier in the other to minimize difficulties in building wideband transformers
failure of one path would be in a 1500 -mile route where the C.C.I.T.T. requirements are hardest to meet. The total feedback on a repeater is unlikely to be much more than 40 dB . Therefore, on failure of one path, the repeater would lose a maximum of 20 dB of effective feedback. There would be a small gain change, some of which might be absorbed by the regulation system, but the main effect would be on noise and harmonics, which would increase by 20 dB . This is an increase of 10 times in voltage and 100 times in power. The fault is, therefore, equivalent to the addition of 10 or 100 amplifiers to the system if the harmonics or noise add as voltages or power respectively. In a system planned to contain over 250 amplifiers in each direction of transmission, as in a $4-\mathrm{Mc} / \mathrm{s}$ system, or 500 in each direction, as in a $12-\mathrm{Mc} / \mathrm{s}$ system, the system should remain within the specification even in a fault condition.

## Multi-Stage Paths and Other Configurations

The same principles apply to multi-stage as to single paths, but the anode load on the first stage of the first path, $Z_{1}$ in Fig. 4, must be decoupled to the cathode so that the local feedback does not affect the signal fed to the second path. This is not necessary in the second path unless a third is added.

Circuits based on Fig. 1 (a) have the disadvantage of requiring a transformer, $\mathrm{T}_{2}$, which has three windings, one of which is isolated from earth. The design of the output transformer of a wideband line amplifier is already a very difficult problem when it has two windings which both have one side earthed. When an extra winding is added and this is isolated from earth the difficulties become forbidding. The configuration in Fig. 1 (b) overcomes this difficulty but $\mathrm{T}_{3}$ now presents an impedance to the input which may have a serious effect on the transmission unless the input impedance is kept low, reducing the maximúm possible transmission gain. Fig. 4 shows one way of minimizing these difficulties. The fact that the two paths have different numbers of stages and thus, almost certainly, different loop characteristics is immaterial. Only the gains and phases of the transmissions through the two paths affect the characteristics of the complete amplifier.

Fig. 5 shows how the second path through $\mathrm{V}_{3}$ can be
used to compensate for the distortion in only part of the first path, namely $\mathrm{V}_{2}$. Here $g_{1}, Z_{1}, Z_{2}$, perform the same function as $Z_{1}$ in Fig. 3 (a) in providing a difference between the signal at the grid of $\mathrm{V}_{2}$ and the feedback voltage which is applied to $\mathrm{V}_{3}$. The condition for cancellation is

$$
g_{1} Z_{1} Z_{2} / Z_{3}=1
$$

There seems no reason to doubt that transistors could replace valves in any of the circuits mentioned, though an amplifier using them was not built.

## A Practical Amplifier

The amplifier shown in Fig. 6, using two stages in each of the transmission paths, was built to test the theory without the detailed loop design required for three-stages. This made it necessary to use a threewinding output transformer, but the bandwidth aimed at in this test was not comparable with that often used on coaxial cable systems and no trouble was taken to produce the best design.

It can be shown that, in simple theory, the condition of the loop of one amplifying path should not affect the stability margin of the loop of the other amplifying path. This was supported by practical evidence. When the feedback ratio in the loop of each amplifying path was measured, it was found that there was no change when the other path was made inactive.

The transmission gain of the complete amplifier was between 19 dB and 20 dB from $15 \mathrm{kc} / \mathrm{s}$ to $150 \mathrm{kc} / \mathrm{s}$ as shown in Fig. 7. With one path dead the gain dropped by 2 dB . This was a consequence of the effective feedback of the complete amplifier dropping from 20 dB to 10 dB . With larger amounts of feedback this would become less marked. The irregularities below $15 \mathrm{kc} / \mathrm{s}$ and above $150 \mathrm{kc} / \mathrm{s}$ were due to imperfections of the transformer $\mathrm{T}_{1}$ which should be an ideal transformer having no phase shift in the transmission band and with 0 dB voltage gain. These irregularities could be reduced considerably by careful design and some compensation could also be applied.

The second and third harmonic margins for the complete amplifier and for each transmission path alone are shown in Table 1. The fundamental output level was kept within 0.5 dB of that at $60 \mathrm{kc} / \mathrm{s}$ for second

Fig. 5. A circuit showing how $V_{3}$ and $Z_{3}$ can be connected to compensate for distortion in $V_{2}$ only



Fig. 6. A practical amplifier using total differential feedback
and third harmonic readings so that the apparent improvements in margins between one path dead and the complete amplifier were approximately 16 dB and 18 dB . This was greater than expected from the incréased feedback alone as the added path contributed 2 dB to the transmission gain without adding appreciably to harmonics. This was equivalent to an additional improvement of 4 dB and 6 dB in the second and third harmonic margins.

It was the input impedance which provided the most serious objection to the use of an unterminated transformer as $\mathrm{T}_{1}$. The experimental amplifier was fed from a terminated 75 -ohm source which swamped the variations in impedance but wasted possible transmission gain. When the first transmission path was dead, the input impedance, with the 75 -ohm termination removed, was that of the transformer whereas, when the first path was active, the feedback increased the impedance greatly. Circuits based on Fig. 1 (a) avoid this, but when two stages are used the second path is potentially a multivibrator.

## Conclusions

The device works substantially as simple theory predicts, but the circuit used must be chosen so that the input and output impedances do not interfere with preceding or succeeding circuits. If a circuit based on that in Fig. 1 (a) is used, an output transformer must normally be used which is difficult to make in wideband applications. A circuit based on Fig. 1 (b) demands either a low impedance source or the toleration of a variation of gain with frequency of an irregular shape
when one of the amplifying paths fails. There may be a limited number of circuits such as in Fig. 4 where the penalties are small.

With the above disadvantages the device has the following advantages.
(1) Even when an amplifier has been designed with the maximum feedback consistent with stability, the apparent feedback ratio may be squared without

TABLE 1
Harmonic Margins Produced by the Amplifier in Fig. 6

| Fundamental Frequency (kc/s) | $\begin{aligned} & \text { Transmission } \\ & \text { Path } \end{aligned}$ | Second Harmonic |  | Third Harmonic |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Fundamental Output Level ( dBm ) | Harmonic Margin (dB) | Fundamental Output Level ( dBm ) | Harmonic Margin (dB) |
| 60 | Complete Amp. First path Second path | -1 -1 -1 | $\begin{aligned} & 57 \frac{1}{2} \\ & 41 \frac{1}{2} \\ & 41 \frac{1}{2} \end{aligned}$ | $\begin{aligned} & +5 \\ & +5 \\ & +5 \end{aligned}$ | $\begin{aligned} & 69 \\ & 50 \frac{1}{2} \\ & 50 \frac{1}{2} \end{aligned}$ |
| 120 | Complete Amp. First path Second path | -1 -1 -1 | $\begin{aligned} & 59 \\ & 42 \frac{1}{2} \\ & 42 \frac{1}{2} \end{aligned}$ | +5 +5 +5 | $\begin{aligned} & 69 \frac{1}{2} \\ & 52 \frac{1}{2} \\ & 52 \frac{1}{2} \end{aligned}$ |
| 240 | Complete Amp. First path Second path | $\begin{aligned} & -1 \frac{1}{2} \\ & -1 \frac{1}{2} \\ & -1 \frac{1}{2} \end{aligned}$ | $\begin{aligned} & 57 \frac{1}{2} \\ & 43 \\ & 43 \end{aligned}$ | $\begin{aligned} & +4 \frac{1}{2} \\ & +4 \frac{1}{2} \\ & +4 \frac{1}{2} \end{aligned}$ | $\begin{aligned} & 61 \frac{1}{2} \\ & 55 \frac{1}{2} \\ & 55 \end{aligned}$ |
| 480 | Complete Amp. <br> First path Second path | $\begin{aligned} & -1 \\ & -1 \\ & -1 \end{aligned}$ | $\begin{aligned} & 38 \\ & 40 \\ & 34 \frac{1}{2} \end{aligned}$ |  |  |



Fig. 7. Transmission gain of the amplifier in Fig. 6; $\qquad$ plete amplifer as in Fig. 6; o 0-0-0 as in Fig. 6, but with first amplifying path inactive; $\mathbf{x}-\mathbf{x}-\mathbf{x}-\mathbf{x}$ as in Fig. 6, but with second amplifying path inactive
affecting the stability substantially. This feedback has the normal beneficial effects on gain stability, harmonics and noise produced in the amplifier.
(2) If one part of the complete amplifier is faulty the other part continues working with a slightly changed gain and reduced harmonic margin.

## Acknowledgements

The author wishes to thank British Telecommunications Research Limited, for permission to publish this article and Mr. H. O. Friedheim for his advice and help.

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# Foster-Seeley Discriminator 

By C. G. Mayo, M.A., B.Sc., M.I.E.E.,* and J. W. Head, M.A.*

SUMMARy. The Foster-Seeley discriminator is essentially a parallel-tuned circuit and an impedance inverter by means of which the frequency variation is converted into amplitude variation in a linear manner. A series-tuned circuit could also in theory achieve this conversion, but impossibly-high values of inductance would be required.

The analysis has been carried out by means of elementary matrices (having not more than four rows and columns) and straightforward if somewhat tedious mathematics, the detail of which is relegated to the Appendices. This procedure enables us to understand the essential behaviour of the discriminator rather than merely to obtain numerical results, and has enabled the authors to devise an improved version of the discriminator which will be described in due course. Normalized units have been used to simplify the general discussion, but the derivation of the relevant parameters for a particular assembly is briefly discussed.

With the circuit arrangements here discussed, sensitivity of about 1.4 audio signal volts per i.f. milliampere can be obtained, with less than $0.1 \%$ second-harmonic distortion at $100 \%$ modulation, and n th-harmonic distortion less than $\left(0 \cdot 1 / 2^{\mathrm{n}-1}\right)$ per cent, with current British f.m. practice. Errors of the same order can be caused by mistuning by, say, $50 \mathrm{kc} / \mathrm{s}$. Errors due to misalignment of tuning capacitance (due to temperature variations, etc.) are negligible if the tuning capacitance never differs from its intended value by more than $1 \%$.

Aparticular arrangement of the Foster-Seeley discriminator circuit is shown in Fig. 1, and the object of this paper is to analyse it, with the help of mathematical methods where necessary, so that a creative understanding of the factors which significantly affect performance is gained; this is more important than the derivation of actual quantitative results. This type of analysis is greatly simplified by the use of suitable normalized units; the performance of one particular assembly will be briefly discussed so as to explain the relation between the normalized units and those customarily used.

A craftsman, such as a french-polisher, when at work often spends about nine-tenths of his time in preparation

[^3]and only about one-tenth on doing the actual job. There is a similar craftsmanship of mathematics, and normalization is part of it when our main object is creative understanding. The full power of mathematics is developed in calculations of this type. It is not so much that very complicated or advanced mathematics is required, but rather that the skilful and repeated application of reasonably elementary principles enables us not merely to understand one particular case (in this case, the performance of one particular discriminator) but the general pattern associated with many different cases. When mathematics is used for the derivation of particular numerical results, it may considerably reduce-perhaps halve-the time taken to obtain those results. When mathematics is used for the type of calculation developed
here, it can make all the difference between creative understanding and complete lack of understanding. The derivation of particular results is relatively easy once we have obtained this creative understanding, that is to say, once we have seen the problem as a whole and in detail, with nothing essential left out and nothing accidental left in. If possible, any particular problem should be related to other problems previously solved.

Our first steps may seem to take us further from a solution, just as the french-polisher's early preparatory activities may seem useless to the uninitiated. This is because we are apt to confuse the unfamiliar with the difficult.
In mechanics, normalization consists in replacing familiar quantities by what used to be called 'specific' quantities, e.g., pressure by stress (pressure per unit area), displacement by strain, etc. These normalized quantities, though less familiar, are more significant. Normalization does require an initial effort of memory for learning new quantities and symbols but, in the long run, it makes the work very much easier, just as new jigs or tools initially appear to hold up production, but in the long run lead to vastly increased production.

In Section 1 we shall show how the essential features of the discriminator can be expressed by means of the simplified circuit of Fig. 2. A reasonable justification of this simplification is given in the main text; a more mathematical justification is given in Appendix 3. Matrix methods are used where needed; in the main text only matrices having two rows and columns are involved but, in Appendix 3, matrices having four rows and columns appear. Although matrices in general need the attention of a mathematician, these specially simple types can be manipulated by means of techniques which an engineer can learn very quickly ${ }^{1}$. They are not at present very familiar to engineers, but they so greatly increase our powers of understanding and appreciating the significant phenomena associated with a system like the discriminator under discussion that the effort of learning to handle matrices is well worth making. In Section 2, the solution for the simplified coupled circuit of Fig. 2 is obtained; normalized units are used to simplify the algebra. The performance of a particular assembly is briefly discussed in Section 4, where the conversion from normalized units to the usual practical units and vice versa is explained. The behaviour of the discriminator output voltage as a function of frequency is discussed fully in Section 3; some of the mathematical detail is relegated to Appendix 2.

## 1. Derivation of Simplified Coupled Circuit

A particular arrangement of the Foster-Seeley discriminator circuit is shown in Fig. 1. Here $L_{1}$ is the
primary coil, supplied from the anode of a pentode valve and tuned by $C_{1} . L_{2}$ is closely coupled to $L_{1}$ and the secondary sections $L_{3}$ and $L_{4}$ are closely coupled to each other. The diode $D_{3}$ and the associated capacitance $C_{3}$ and load $r_{3}$ are supposed respectively to be similar to the diode $D_{4}$ and its associated capacitance $C_{4}$ and load $r_{4}$. $L_{3}$ and $L_{4}$ are supposed equal and equally coupled to $L_{1}$. The action of the diodes causes the output $V_{o}$ to be

$$
\begin{equation*}
V_{o}=\left|V_{2}+V_{3}\right|-\left|V_{2}+V_{4}\right| \tag{1}
\end{equation*}
$$

where the vertical lines indicate numerical values.
We could solve the circuit of Fig. 1 as it stands, but this would introduce unhelpful complexity. The justification for the simplifying assumptions we now make is contained in Appendix 3; a reasonable but less strict explanation of these assumptions follows.

Consider first the close-coupled coils $L_{1}$ and $L_{2}$ as a slight deviation from an ideal transformer, so that the coupling coefficient is $k_{12}=1-\mu$ where $\mu$ is of order 0.05 . On the other hand, the coupling coefficients $k_{13}$


Fig. 2. A simplified form of the discriminator circuit showing essential features of its performance
and $k_{14}$ between $L_{1}$ and the secondary coils $L_{3}$ and $L_{4}$ will be small, say of order 0.05 . We allow for the imperfect coupling by supposing that the circuit consists of the coil $L_{1}$ together with an ideal transformer whose turns ratio is nearly the square root of $L_{1} / L_{2}$ and an unwanted equivalent series (leakage) inductance in the circuit of $L_{2}$ whose value is ( $1-k^{2}{ }_{12}$ ) $L_{2}$ which is nearly $2 \mu L_{2}$. The effective value of $V_{2}$ reaching the diodes is reduced by the product of the effective series impedance due to the leakage inductance and the effective load current into the diode circuit; it thus becomes $(1-b) V_{2}$, where $b=2 \mu \omega L_{2} / r_{2}, \omega /(2 \pi)$ being the frequency and $r_{2}$ the total load on $L_{2}$. As in practice the leakage reactance $2 \mu \omega L_{2}$ is of the order 10 ohms while $r_{2}$ is of order $50 \mathrm{k} \Omega$, $b$ is of very minor importance, so we can regard $L_{1}$ and $L_{2}$ as forming an ideal transformer of ratio $\rho_{1}=\left(L_{2} / L_{1}\right)^{4}$. In (1) we can therefore replace $V_{2}$ by $\rho_{1} V_{1}$, and the equivalent load of the diode circuit on $L_{1}$ is $\rho^{2}{ }_{1}$ times the actual load of the diode circuit on $L_{2}$. This is explained in Appendix 1.

If we similarly consider the equal coils $L_{3}$ and $L_{4}$, they

Fig. 1. A particular arrangement of the Foster-Seeley discriminator circuit

can be effectively replaced by a single coil $L_{5}$ having inductance equal to $L_{1}$ and an ideal push-pull transformer of ratio $\pm \rho_{2}: 1$ where $\rho_{2}=\left(L_{3} / L_{1}\right)^{\frac{1}{2}}$, with the same precautions as to proper assignment of the diode circuit loading, Equ. (1) now becomes

$$
\begin{equation*}
V_{o}=\left|\rho_{1} V_{1}+\rho_{2} V_{5}\right|-\left|\rho_{1} V_{1}-\rho_{2} V_{5}\right| \tag{2}
\end{equation*}
$$

The essentials of the circuit are contained in Fig. 2 but we have to determine the appropriate values for the equivalent losses $g_{1}$ and $g_{5}$ shown across $L_{1}$ and $L_{5}$ respectively, and for the corresponding equivalent capacitances $C_{1}$ and $C_{5}$. The conductance $g_{1}$ includes
(a) the equivalent source conductance $g_{11}$
(b) coil losses $g_{12}$ in $L_{1}$ and $L_{2}$ (Fig. 1) adjusted to take account of the transformer of ratio $\rho_{1}$
(c) conductance $g_{13}$ deliberately added across $L_{1}$ or $L_{2}$, adjusted to take account of the transformer of ratio $\rho_{1}$ if necessary
(d) referred diode circuit load $g_{14}$

For (d) the usual convention is that if the diode load resistance is $r_{d} \mathrm{k} \Omega$, the equivalent diode load is taken as $2 / r_{d}$ mmho under peak rectifying conditions. In Fig. 1 the load on $L_{2}$ is thus the equivalent load due to both diodes in parallel or $4 / r_{d}$ mmho, $r_{d}$ being of the order $100 \mathrm{k} \Omega$. Allowing for the transformer of ratio $p_{1}, g_{14}$ becomes $4 / r_{d \rho}{ }^{2}{ }_{1}$. As all these conductances are in parallel, we finally have

$$
g_{1}=g_{11}+g_{12}+g_{13}+g_{14}
$$

(The computation of the equivalent total load $g_{1}$ from the separate parts is considered mathematically in Appendix 3 in a somewhat more general case.)

Similarly

$$
g_{5}=g_{52}+g_{53}+g_{54}
$$

where $g_{52}$ is the contribution from coil losses in $L_{3}$ and $L_{4}$ (Fig. 1) to the total loss across $L_{5}$ (Fig. 2) adjusted to take account of the transformer of ratio $\rho_{2}, g_{53}$ is conductance deliberately added across $L_{3}$ and $L_{4}$ in Fig. 1, and adjusted to take account of the transformer of ratio $\rho_{2}$ and $g_{54}$ is the referred diode circuit load $\rho^{2} 2 / r_{d}$. There is no source conductance affecting $L_{5}$. The capacitances $C_{1}$ and $C_{5}$ can be regarded as made up of stray capacitances and tuning capacitances deliberately added, but since the tuning capacitances can be adjusted, we can regard $C_{1}$ and $C_{5}$ simply as variable capacitances in parallel with $L_{1}$ and $L_{5}$ in Fig. 2 and we need not examine how they are made up. We shall see later what effective values of $C_{1}$ and $C_{5}$ are required for tuning.

## 2. Solution for the Simplified Circuit of Fig. 2. Normalization

At frequency $\omega_{0} /(2 \pi)$, the reactance of $L_{1}$ in Fig. 2 is $j \omega_{0} L_{1}$ ohms. At frequency $\omega /(2 \pi)$ the impedance of $L_{1}$ is $j \omega L_{1}$ ohms or $j \omega_{0}(1+\xi) L_{1}$ ohms, where $\xi$ is the fractional frequency deviation $\left(\omega-\omega_{0}\right) / \omega_{0}$. With an i.f. or mean frequency of $10.7 \mathrm{Mc} / \mathrm{s}$ and a maximum frequency deviation of $75 \mathrm{kc} / \mathrm{s}$, the maximum numerical value of $\xi$ is 0.007 . It is convenient to replace $\xi$ by $s x$, where $s$ is merely an abbreviation for 0.007 and $x$ varies between -1 and +1 . Thus we finally obtain that the impedance of $L_{1}$ or $L_{5}$ at frequency $\omega /(2 \pi)$, alternatively written $\omega_{0}(1+s x) /(2 \pi)$, is

$$
j \omega_{0}(1+s x) L_{1} \text { ohms. }
$$

We now normalize the unit of impedance so that this
quantity shall be numerically equal to unity when $\omega=\omega_{0}$ and $x=0$, that is to say, we take as our reactive unit an impedance of $\omega_{0} L_{1}$ ohms rather than an inductance of a henry or a capacitance of a farad. The impedance of $L_{1}$ or $L_{5}$ thus becomes $p$ in the normalized units where

$$
\begin{equation*}
p=j(1+s x) \tag{3}
\end{equation*}
$$

In the same units the quantities $g_{1}$ and $g_{5}$ become equivalent loss factors, the reciprocals of the corresponding equivalent $Q$-factors; the quantity we called $g_{13}$ is likewise the reciprocal of the $Q$ of coil 1 in these normalized units. The coupling coefficient $k$ between $L_{1}$ and $L_{5}$ will be of order 0.05 , like the quantities $g_{1}$ and $g_{5}$. With this notation, we have at frequency $\omega /(2 \pi)$

$$
\left.\begin{array}{l}
V_{1}=p i_{1}+p k i_{5}  \tag{4}\\
V_{5}=p k i_{1}+p i_{5}
\end{array}\right\} .
$$

where $i_{1}, i_{5}$ are the currents flowing in Fig. 2 on the assumption that the elements $g_{1}, C_{1}, g_{5}$ and $C_{5}$ are absent. In matrix notation this can be written

$$
\left[\begin{array}{l}
V_{1}  \tag{5}\\
V_{5}
\end{array}\right]=p\left[\begin{array}{ll}
1 & k \\
k & 1
\end{array}\right]\left[\begin{array}{l}
i_{1} \\
i_{5}
\end{array}\right]
$$

Equation (4) can be solved for $i_{1}$ and $i_{5}$ in terms of $V_{1}$ and $V_{5}$, and the result expressed in matrix notation in the form

$$
\left[\begin{array}{l}
i_{1} \\
i_{5}
\end{array}\right]=\frac{1}{p\left(1-k^{2}\right)}\left[\begin{array}{cc}
1 & -k \\
-k & 1
\end{array}\right]\left[\begin{array}{l}
V_{1} \\
V_{5}
\end{array}\right]
$$

As $k$ is of order 0.05 , we can neglect $k^{2}$ compared with unity so that

$$
\left[\begin{array}{l}
i_{1}  \tag{6}\\
i_{5}
\end{array}\right]=\frac{1}{p}\left[\begin{array}{cc}
1 & -k \\
-k & 1
\end{array}\right]\left[\begin{array}{l}
V_{1} \\
V_{5}
\end{array}\right] \cdots
$$

Now the capacitance $C_{1}$ carries a current $p C_{1} V_{1}$ and this current increases $i_{1}$ only. The equivalent loss $g_{1}$ also carries a current $g_{1} V_{1}$ which likewise increases $i_{1}$ only. Similarly for $C_{5}$ and $g_{5}$, so that, allowing for the elements $C_{1}, C_{5}, g_{1}$ and $g_{5}$ the relation between current and voltage is

$$
\left[\begin{array}{l}
i_{1}  \tag{7}\\
i_{5}
\end{array}\right]=\left[\begin{array}{cc}
1 / p+p C_{1}+g_{1} & -k / p \\
-k / p & 1 / p+p C_{5}+g_{5}
\end{array}\right]\left[\begin{array}{l}
V_{1} \\
V_{5}
\end{array}\right]
$$

for the actual circuit of Fig. 2, in which $i_{5}$ must be equated to zero since no further elements are connected to $L_{2}$.
For tuning we take $C_{1}=C_{5}=1$ (in normalized units). In effect, the primary is tuned with the secondary short-circuited and the secondary is tuned with the primary short-circuited and, at the mean frequency ( $p=j$ ), we have

$$
\left[\begin{array}{l}
i_{1}  \tag{8}\\
i_{5}
\end{array}\right]=\left[\begin{array}{ll}
g_{1} & k j \\
k j & g_{5}
\end{array}\right]\left[\begin{array}{l}
V_{1} \\
V_{5}
\end{array}\right]
$$

If $g_{1}$ and $g_{5}$ are small compared to $k$, Equ. (8) indicates that the primary current depends only upon the secondary voltage and vice versa, so that the circuit is behaving as a quarter-wave impedance inverter or Boucherot circuit. As will be seen later, short-circuiting either winding makes the other winding have maximum impedance. This inversion property is the key to understanding the whole arrangement.

Equations (6) and (8), and much of the treatment which now follows, can be regarded as a method of analysing coupled-coil circuits in general (apart from the present application to the discriminator) which presents
at a glance the essential and important features of such circuits. The normalization procedure takes adequate care of the detail associated with a particular application. Indeed, we could have started with (6) and only considered the normalization with concrete design details.

From (7) with $i_{5}=0$ we have, by 'inverting' the matrix, that is, finding $V_{1}$ and $V_{5}$ in terms of $i_{1}$ and $i_{5}$,

$$
\begin{align*}
& V_{1}=\left[p+1 / p+g_{5}\right] \cdot\left(i_{1} / \Delta\right) \\
& V_{5}=(-k / p) \cdot\left(i_{1} / \Delta\right) \tag{9}
\end{align*}
$$

where

$$
\begin{equation*}
\Delta=\left\{p+(1 / p)+g_{1}\right\}\left\{p+(1 / p)+g_{5}\right\}-\left(k^{2} / p^{2}\right)(10) \tag{15}
\end{equation*}
$$

But from (3)

$$
\begin{equation*}
p+(1 / p)=2 j s x\left(1+\frac{1}{2} s x\right) /(1+s x) \approx 2 j s x\left(1-\frac{1}{2} s x\right) \tag{11}
\end{equation*}
$$

so that if we take $p+(1 / p)$ as $2 j s x$, there is an error of $\frac{1}{2} s$ or $0.35 \%$ at $100 \%$ modulation $(x=1)$.

For the present we shall neglect this error, and the error of the same order of magnitude involved in replacing $p^{2}$ by -1 in the last term of (10). In Appendix 2, the effect of this approximation, which is only significant for second-harmonic distortion, is examined more fully.

Now in (9) all the quantities involved are of the same order of magnitude. We therefore write

$$
\begin{equation*}
g_{1}=2 s \alpha, \quad g_{5}=2 s \beta, \quad k=2 s \lambda \tag{12}
\end{equation*}
$$

where, as before, $s=0.007$; the variables $\alpha, \beta$ and $\lambda$ will then lie between 1 and 10 in practice, and with such variables it is much easier to see the significance of results obtained than is the case with the original variables $g_{1}, g_{5}$ and $k$. Equs. (9) and (10) now reduce to

$$
\left.\begin{array}{l}
V_{1} / i_{1}=\frac{\beta+j x}{2 s\left\{(\alpha+j x)(\beta+j x)+\lambda^{2}\right\}} \\
V_{5} / i_{1}=\frac{j \lambda}{2 s\left\{(\alpha+j x)(\beta+j x)+\lambda^{2}\right\}} \tag{13}
\end{array}\right\}
$$

and (13) is easier to understand with the aid of the following verbal definitions which in effect recapitulate (11) and (12): $\alpha$ and $\beta$ are the equivalent loss factors of primary and secondary divided by $2 s$ (i.e., 0.014 ), that is, measured relative to maximum fractional frequency deviation. $\lambda$ is the coupling coefficient between $L_{1}$ and $L_{5}$ (Fig. 2) measured likewise relative to maximum fractional frequency deviation. $x$ has the maximum numerical value unity at $100 \%$ modulation. In practice $\lambda$ is of order 3, according to the coupling, and $\alpha$ and $\beta$ are also of order 3 , according to the loading.

From (13), we could plot $\left|V_{1} / i_{1}\right|$ and $\left|V_{5} / i_{1}\right|$ against $x$. In effect we regard the input current $i_{1}$ as delivered through a high impedance. The curve of $\left|V_{5} / i_{1}\right|$ against $x$ can be made either concave upwards (with two maxima) or concave downwards (with one maximum) or very flat-topped by suitable choice of $\alpha, \beta$ and $\lambda$. The curve of $\left|V_{1}\right| i_{1} \mid$ against $x$ only differs from that for $\left|V_{5} / i_{1}\right|$ because of the factor $(\beta+j x)$ in the numerator of $V_{1}$ in (13). If $\left|V_{5} / i_{1}\right|$ is nearly flat-topped, $V_{1} / i_{5}$ is nearly linear in $x$; this important fact is not obvious from the curves.

Since in (13) we have used $\omega_{0} L_{1}$ as our unit of impedance, $V_{1} / i_{1}$ and $V_{5} / i_{1}$ must both be multiplied by $\omega_{0} L_{1}$ if they are to be expressed in volts/ampere on the assumption that $\omega_{0}$ is in radians $/ \mathrm{sec}$, and $L_{1}$ is in henrys. $V_{1} / i_{1}$ and $V_{5} / i_{1}$ will, however, be in $\mathrm{V} / \mathrm{mA}$ if $L_{1}$ is in mH

and $\omega_{0} / 2 \pi$ in $\mathrm{Mc} / \mathrm{s}$. For the particular assembly discussed below (Section 5) the sensitivity thus turns out to be about $1.4 \mathrm{~V} / \mathrm{mA}$.

Now from (10) we have $\Delta=4 s^{2} \Delta_{0}$, where

$$
\begin{equation*}
\Delta_{0}=(\alpha+j x)(\beta+j x)+\lambda^{2} \tag{14}
\end{equation*}
$$

The discriminator output voltage $V_{o}$ is therefore found by substitution in (2) to be

$$
V_{o}=\frac{i_{1}}{2 s\left|\Delta_{0}\right|}\left\{\left|\rho_{1}(\beta+j x)+j \rho_{2} \lambda\right|-\left|\rho_{1}(\beta+j x)-j \rho_{2} \lambda\right|\right\}
$$

where, as in (2), vertical bars denote numerical values.

## 3. Behaviour of the Discriminator Output Voltage

To understand the significance of (15), we need to expand the numerator and denominator in powers of $x$; here we shall consider powers of $x$ up to and including $x^{5}$ in the numerator and $x^{4}$ in the denominator. The result, derived more fully in Appendix 2, is

$$
V_{o}=\frac{i_{1} \rho_{2} \lambda}{s K^{\frac{1}{2}} N} .
$$

where

$$
\begin{equation*}
\sigma=\rho_{2} / \rho_{1} ; K=\beta^{2}+\lambda^{2} \sigma^{2} \text { and } N=\alpha \beta+\lambda^{2} \tag{17}
\end{equation*}
$$

Now in the special case when $\alpha=\beta=\lambda=3$, the $x^{2}$ term in the denominator of (16) is absent, and the $x^{4}$ term reduces to $1 /\left(2 \times 18^{2}\right)$, so that there is only $0 \cdot 15 \%$ of fourth-power deviation from constancy in this denominator. The curve showing $\left\{\Delta_{0} \mid\right.$ as a function of $x$ could be made still flatter by keeping $\alpha, \beta$ and $\lambda$ equal and increasing their common value; the discriminator would thus be made broader at the expense of output. The influence of $\left|\Delta_{0}\right|$ on (16) can be considered as if $\left|\Delta_{0}\right|$ were the response curve of a preceding section of the i.f. amplifier; $\left|\Delta_{0}\right|$ behaves like such a response. We can think of $\left|\Delta_{0}\right|$ as constant, and suppose that $i_{1}$ contains the nonlinearity of $\left|\Delta_{0}\right|$ as if it came from a preceding stage.

If for the time being we neglect the variations in $\left|\Delta_{0}\right|$, we notice in (13) that $V_{1}$ varies linearly with $x$ while $V_{5}$ is constant, and in (16) the leading term of the numerator is proportional to $x$. If $V_{1}$ itself were being detected by a diode, a change in the sign of the modulation $x$ would not be detected; it is the addition and subtraction of the $V_{5}$-term in phase with the $x$-term that allows the output voltage $V_{o}$ in (16) to be linear in $x$ to a high degree of accuracy. The $\beta$-term in $V_{1}$ at first sight would seem to endanger the precision, but $V_{5}$ only has to be about $50 \%$ greater than $V_{1}$ in order to achieve satisfactory precision (as will be shown in Appendix 2).
If we now consider (16) as a whole, instead of considering the behaviour of the numerator and the denominator separately as hitherto, it is clear that the sensitivity of the discriminator is controlled by the coefficient of $x$ when $V_{o} / i_{1}$ is derived from (16). Allowing for our normalization, the sensitivity is

$$
\frac{\rho_{2} \lambda}{s K^{\frac{1}{2}} N} \cdot \omega_{0} L_{1} \quad \mathrm{~V} / \mathrm{mA} \text { at } 100 \% \text { modulation }
$$

$L_{1}$ being in mH . For the particular values of $\alpha, \beta, \lambda$ and $\sigma$
given in (22), this gives a sensitivity of $1.4 \mathrm{~V} / \mathrm{mA}$ assuming $\rho_{2}=1 / \sqrt{ } 5 \approx 0.45$.

There will be no third-harmonic distortion if the ratio of the coefficient of $x^{3}$ to that of $x$ in the numerator equals the ratio of the coefficient of $x^{2}$ to the constant term in the denominator. If this is arranged, there will only be fifth-harmonic distortion; the relevant coefficient of $x^{5}$ ( $2^{5-1}$ times the fifth-harmonic distortion) will then be the difference between the ratio of the coefficient of $x^{5}$ in the numerator to that of $x$, and the ratio of the coefficient of $x^{4}$ in the denominator to the constant term. It is not profitable to derive general formulx for third- and fifth-harmonic distortion from (16) because we have somewhat over-simplified the problem by assuming that the capacitances $C_{1}$ and $C_{2}$ could be made to have exactly the values unity we desired; in fact these capacitances may vary relative to one another in a manner which can change with time and is not under our control. We shall see later that errors from this cause are minimized by making $\beta=\lambda$. Our object is not primarily to determine the distortion terms in the general case but to find rough ranges of values of the parameters $\alpha, \beta, \lambda, \sigma$ (which are under our control) so that the discriminator performance shall be thoroughly satisfactory. But, first, it is desirable to consider more closely what has been achieved hitherto.

We wish to derive an output proportional to a frequency deviation which is a small fraction of the mean frequency. If we try to use a pure inductance $L_{a} \mathrm{mH}$ for this purpose, the voltage per milliampere would be $j \omega L_{a}$ at frequency $\omega /(2 \pi)$ which in the notation of (3) is $j \omega_{0} L_{a}(1+x s)$, and since $s=0.007$, the output thus obtained is not sufficiently sensitive to the variations in $x$ in which we are interested. If now a tuning capacitance is connected in series with $L_{a}$, the output becomes

$$
V=\left(R_{1}+j 2 s x\right) \omega_{0} L_{a}
$$

where $R_{1}$ represents the effective series losses of the circuit. This expression is, as required, linear in $x$, but $L_{a}$ would have to be very large to obtain adequate sensitivity, and self-capacitance of the windings makes it impracticable to have $L_{a}$ large. If we try a parallel tuned circuit, high impedances are easily obtained, but the output voltage is of the form

$$
V=A /(\beta+j x)
$$

so that $x$ is not linearly related to $V$; this makes precise discrimination difficult. In (13), however, $V_{1}$ had a numerator $(\beta+j x)$ and a nearly constant denominator, and we were thus able to obtain from (16) an output almost linear in $x$. This numerator of (13), which has the same form as applies to a series tuned circuit, arises because the circuit of Fig. 2 is in essence an inverter; the $(\beta+j x)$ is in fact the secondary admittance inverted by the circuit to give the primary impedance.

In order that the distortion terms in the numerator of (16) may be reasonably small, we need to make $K$ relatively large; it is sufficient to have $\lambda \sigma / \beta$ greater than say 1-5. But this requires high values of $L_{3}$ and $L_{4}$ in Fig. 1, which are inconvenient because the high coupling between $L_{3}$ and $L_{4}$ will then involve high winding capacitance. As we have allowed for the effective presence in the circuit of Fig. l of an ideal transformer of ratio $\rho_{1}$, we can choose $L_{1}$ to have the value most appropriate to
the anode and stray-capacitances. This means that $\omega_{0} L_{1}$ should be of order 1000 ohms, and $C_{1}$, including all strays and anode capacitance, should be of order 20 pF . Similarly, the highest appropriate value of $\omega_{0} L_{3}$ and $\omega_{0} L_{4}$ will be of order 200 ohms. Hence $\rho_{2}$ should be of order $1 / \sqrt{ } 5$, and to make $\rho_{2} \lambda /\left(\rho_{1} \beta\right)=1.5$ then requires $\rho_{1}$ to be about $1 / 1 \cdot 5 \sqrt{ } 5$, say $1 / 3 \cdot 5, \beta$ and $\lambda$ being approximately equal to minimize errors due to drift or initial misalignment of tuning capacitance as explained immediately below.

We have now determined the sensitivity of the discriminator, and the third- and fifth-harmonic distortion terms, and analysed the essential behaviour of the discriminator and the reasons for its effectiveness, but hitherto we have made two assumptions which are oversimplifications; we assumed that $C_{1}$ and $C_{5}$ could be made equal to unity in normalized units, and we assumed that $[p+(1 / p)]$ could be replaced by $2 j s x$ in (11). Now since in (15), $V_{o}$ is clearly zero when $x$ is zero, and $(\beta+j x)$ is in essence secondary admittance inverted, we can regard zero d.c. output as an accurate indication of secondary tuning. If the receiver is fitted with some kind of tuning indicator, it may be assumed that in use the secondary tuning is accurate. The accuracy of the primary tuning will then depend on the accuracy of the initial alignment and any subsequent change of capacitances due to temperature, etc. We propose to allow for all such errors by assuming an effective $1 \%$ error at most in primary tuning. This means that the term $p$ representing primary tuning capacitance in (7) must be replaced by $p(1+e)$ where $|e|<0 \cdot 01$. Equations (9) are unaffected except in so far as the value of $\Delta_{0}$ given by (14) is altered: $\Delta_{0}$ becomes $\Delta^{\prime}$ where

$$
\Delta^{\prime}=(\alpha+j x+j \epsilon)(\beta+j x)+\lambda^{2}
$$

and $\epsilon=e / 2 s$ in the fractional capacitance tuning error measured relative to the fractional frequency deviation, so that $|\epsilon|<0 \cdot 7$. We then find that

$$
\begin{align*}
& \left|\Delta^{\prime}\right|^{2}=\left(\alpha \beta+\lambda^{2}-\epsilon x-x^{2}\right)+\{(\alpha+\beta) x+\epsilon \beta\}^{2} \\
& =\left\{\left(\alpha \beta+\lambda^{2}\right)^{2}+\epsilon^{2} \beta^{2}\right\}^{2}+2 \epsilon\left(\beta^{2}-\lambda^{2}\right) x \\
& +\left(\alpha^{2}+\beta^{2}+\epsilon^{2}-2 \lambda^{2}\right) x^{2}+2 \epsilon x^{3}+x^{4} \tag{18}
\end{align*}
$$

so that if we make $\beta=\lambda$, there will be no secondharmonic distortion due to capacitance mistuning. In the special case $\alpha=\beta=\lambda=3$, which we considered before to appreciate the orders of magnitude of the various distortion terms involved, the $x^{2}$ term due to the presence of $\epsilon$ in the expansion of $\left|\Delta^{\prime}\right|$ is $\epsilon^{2} / 648$, giving thirdharmonic distortion of $\epsilon^{2} /\left(648 \times 2^{3-1}\right)$, while the fourthharmonic distortion is $2 \epsilon /\left(648 \times 2^{4-1}\right)$; these are both very small even with the maximum value of $\epsilon$. We conclude that the discriminator can tolerate errors of up to $1 \%$ on alignment of primary capacitance without more than $0.1 \%$ resultant distortion, that is to say, if the final output is expressed as

$$
\begin{equation*}
V_{0}=A x\left(1+B x+C x^{2}+D x^{2}+E x^{4}\right) \tag{19}
\end{equation*}
$$

the capacitance errors do not change $B, C, D$ and $E$ by more than 0.001 at most from the values associated with (16).

This also implies that mistuning by an amount not large compared with $75 \mathrm{kc} / \mathrm{s}$ will produce little distortion. If the receiver were mistuned by $75 \propto \mathrm{kc} / \mathrm{s}$, we should have to replace $x$ by $x+\alpha$ in (19), and therefore $V_{o}$
would become $V^{\prime}$ o where

$$
\begin{align*}
V_{\circ}^{\prime}= & \left(A \alpha+B \alpha^{2}+C \alpha^{3}+D \alpha^{4}+E \alpha^{5}\right) \\
& +x\left(A+2 B \alpha+3 C \alpha^{2}+4 D \alpha^{3}+5 E \alpha^{4}\right) \\
& +x^{2}\left(B+3 C \alpha+6 D \alpha^{2}+10 E \alpha^{3}\right) \\
& +x^{3}\left(C+4 D \alpha+10 E \alpha^{2}\right) \\
& +x^{4}(D+5 E \alpha)+E x^{5} \quad \ldots \quad \ldots \tag{20}
\end{align*}
$$

and clearly if $\alpha$ is sufficiently small (that is, the mistuning is sufficiently small compared with $75 \mathrm{kc} / \mathrm{s}$ ) the coefficients of the various powers of $x$ in (20) will differ little from those in (19).

When $p+(1 / p)$ was taken as $2 j s x$, the strict truth was

$$
p+1 / p=2 j s x\left[1-\frac{1}{2} s+\frac{\frac{1}{2} s^{2} x^{2}}{1+s x}\right]
$$

and as $s$ is 0.007 , we are perfectly justified in neglecting the last term, as in (11). This will introduce additional terms involving $s$ into $\Delta$ in (10) as well as into the expression for $V_{1}$ in (9). Hence (13) and (16) will also contain additional $s$-terms. The expansion of $V_{0}$ in powers of $x$ can be carried out in the manner indicated in Appendix 2, but the presence of the additional $s$-terms complicates the procedure. Only the contribution of the $s$-terms to second-harmonic distortion, however, need be calculated, because for higher-order distortions the contribution of the $s$-terms is clearly small compared with the distortions already discussed in relation to (16) and (18), owing to the small value of $s$. When the $s$-terms are taken into account, the relative value of the coefficient of $x^{2}$ in the expansion of $V_{o}$ to that of $x$ is, as explained in Appendix 2,

$$
\begin{equation*}
s\left[\frac{\lambda^{2}-\alpha \beta}{\lambda^{2}+\alpha \beta}+\frac{1}{2} \frac{\lambda^{2} \rho^{2}{ }_{2}-\beta^{2} \rho_{1}^{2}}{\lambda^{2} \rho^{2}{ }_{2}+\beta^{2} \rho^{2}{ }_{1}}\right] \tag{21}
\end{equation*}
$$

so that if $\alpha=\beta=\lambda=3, \rho_{2}=1.5 \rho_{1}$, the relative $x^{2}$ term in the expansion of $V_{o}$ is 0.00135 , and the secondharmonic distortion is half this or $0.07 \%$; clearly from (21) values of $\alpha, \beta, \lambda, \rho_{1}$ and $\rho_{2}$ can easily be found such that this type of distortion is less than say $0.2 \%$.

## 4. The Performance of a Particular Assembly

We have seen that by proper choice of the parameters $\lambda, \rho_{1}, \rho_{2}, \alpha$ and $\beta$ (which were defined in the last section, and which are under our control) and by due regard to Equations (16) and (21), we can control the distortion terms associated with powers of $x$ (the parameter representing modulation) up to $x^{5}$. By making $\lambda$ and $\beta$ equal, we can minimize the effect of tuning-capacitance misalignment. For the particular set of values

$$
\begin{equation*}
\alpha=3 ; \beta=\lambda=3.79 ; \rho_{2} / \rho_{1}=1.5 \tag{22}
\end{equation*}
$$

the second-harmonic distortion percentage is found from (21) to be $0 \cdot 108$, there is no third harmonic, the fourthharmonic distortion percentage (for maximum tuningcapacitance misalignment of $1 \%$ ) is about $0.02 \%$ and the fifth-harmonic distortion is about $-0.005 \%$. To make up an assembly having parameter-values as near (22) as practicable, the coils are first wound so spaced as to get $\lambda$ within $10 \%$ of the required value $3 \cdot 79$, which means from (12) that the coupling coefficient $k$ is within $10 \%$ of $0.014 \times 3.79=0.053$. The secondary split coil should have as high an inductance as is possible so that the self-capacitance is not too large; this means that the impedance at $10.7 \mathrm{Mc} / \mathrm{s}$ must be of order 1000 ohms . The
tuning capacitance must exceed this self-capacitance by an amount which can be added with reasonable accuracy. There is no difficulty about ensuring that $\rho_{1} / \rho_{2}$ is of the right order. To obtain values of $\alpha, \beta$ of the required order, the conductance $g_{1}$ must be about 0.042 in our normalized units and the conductance $g_{5}$ about 0.053 ; these values must be divided by the impedance of the primary at $10.7 \mathrm{Mc} / \mathrm{s}$ to express them in mhos. It will then be found that the required conductances are several times those provided by the coil losses and diode loads, so that shunt resistances across the primary and secondary must be added. A discrepancy of the order of $10 \%$ can be tolerated in any of the parameters (22) as performance does not depend critically on these parameters; the equality of $\beta$ and $\lambda$ is somewhat more critical than the values of any of the parameters. The errors for the parameter values (22) due to mistuning or to misalignment of tuning capacitance are of the same order as in the case already discussed when $\alpha, \beta$ and $\lambda$ were all equal to 3 .

## APPENDIX I

Intuitive Derivation of the Equivalent Load of the Diode Circuit
The coils $L_{1}$ and $L_{2}$ in Fig. 1, which have coupling $1-\mu$, must therefore have mutual inductance $M=(1-\mu) \sqrt{ }\left(L_{1} L_{2}\right)$. For these coils alone, the $A$-matrix relating input voltage $V_{1}$ and current $I_{1}$ to output voltage $V_{2}$ and current $I_{2}$ is given by

$$
\left[\begin{array}{c}
V_{1} \\
I_{1}
\end{array}\right]=\left[\begin{array}{lc}
L_{1} / M & p\left(L_{1} L_{2}-M^{2}\right) / M \\
1 /(p M) & L_{2} / M
\end{array}\right]\left[\begin{array}{c}
V_{2} \\
I_{2}
\end{array}\right]
$$

Now $L_{1} L_{2}-M^{2}=\mu L_{1} L_{2}$; ir $\rho_{1}=L_{1} / M=\sqrt{ }\left\{L_{1} / L_{2}(1-\mu)\right\}$ so that $\rho_{1} \approx\left(L_{1} / L_{2}\right)^{1 / 2}$, we have

$$
\begin{aligned}
{\left[\begin{array}{c}
V_{1} \\
I_{1}
\end{array}\right] } & =\left[\begin{array}{cc}
L_{1} / M & 0 \\
0 & M / L_{1}
\end{array}\right]\left[\begin{array}{cc}
M / L_{1} & 0 \\
0 & L_{1} / M
\end{array}\right]\left[\begin{array}{cc}
L_{1} / M & p \mu L_{1} L_{2} / M \\
1 /(p M) & L_{2} / M
\end{array}\right]\left[\begin{array}{l}
V_{2} \\
I_{2}
\end{array}\right] \\
& =\left[\begin{array}{ll}
\rho_{1} & 0 \\
0 & 1 / \rho_{1}
\end{array}\right]\left[\begin{array}{cc}
1 & p \mu L_{2} \\
1 / p L_{2}(1-\mu) & 1 /(1-\mu)
\end{array}\right]\left[\begin{array}{c}
V_{2} \\
I_{2}
\end{array}\right] \\
& =\left[\begin{array}{ll}
\rho_{1} & 0 \\
0 & 1 / \rho_{1}
\end{array}\right]\left[\begin{array}{cc}
1 & 0 \\
1 / p L_{2}(1-\mu) & 1
\end{array}\right]\left[\begin{array}{cc}
1 & p \mu L_{2} \\
0 & 1
\end{array}\right]\left[\begin{array}{l}
V_{2} \\
I_{2}
\end{array}\right] \\
& =\left[\begin{array}{cc}
\rho_{1} & 0 \\
1 / p \rho_{1} L_{2}(1-\mu) & 1 / \rho_{1}
\end{array}\right]\left[\begin{array}{cc}
1 & p \mu L_{2} \\
0 & 1
\end{array}\right]\left[\begin{array}{c}
V_{2} \\
I_{2}
\end{array}\right] \\
& =\left[\begin{array}{cc}
1 & 0 \\
1 / p L_{1} & 1
\end{array}\right]\left[\begin{array}{ccc}
\rho_{1} & 0 \\
0 & 1 / \rho_{1}
\end{array}\right]\left[\begin{array}{cc}
1 & p \mu L_{2} \\
0 & 1
\end{array}\right]\left[\begin{array}{c}
V_{2} \\
I_{2}
\end{array}\right]
\end{aligned}
$$

The third of these equations shows that the coils $L_{1}$ and $L_{2}$ are equivalent to the network of Fig. 3, while the last shows that they are also equivalent to the circuit of Fig. 4.

Figs. 3 and 4. Networks equivalent to the coils $L_{1}$ and $L_{2}$ of Fig. I


## APPENDIX ${ }_{2}$

## Expansion of $V_{o}$ in Powers of $x$

For the numerator, the expression requiring expansion is

$$
\left\{\rho^{2} \beta^{2}+\left(\rho_{1} x+\rho_{2} \lambda\right)^{2}\right\}^{1 / 2}-\left\{\rho^{2} \beta^{2}+\left(\rho_{1} x-\rho_{2} \lambda\right)^{2}\right\}^{1 / 2}
$$

or

$$
A^{1 / 2}\left\{\left(1+B x+C x^{2}\right)^{1 / 2}-\left(1-B x+C x^{2}\right)^{1 / 2}\right\}
$$

where

$$
A=\rho^{2}{ }_{1} \beta^{2}+\rho_{2}^{2} \lambda^{2} \quad B=2 \rho_{1} \rho_{2} \lambda / A \quad C=\rho^{2}{ }_{1} / A
$$

and this reduces, neglecting powers of $x$ above the fifth, to

$$
\left.\begin{array}{l}
A^{1 / 2}\left(1+C x^{2}\right)^{1 / 2}\left\{\frac{B x}{1+C x^{2}}+\frac{1}{8} \frac{B^{3} x^{3}}{\left(1+C x^{2}\right)^{3}}+\frac{7}{128} \frac{B^{5} x^{5}}{\left(1+C x^{2}\right)^{5}}\right\} \\
=A^{1 / 2} B x\left\{\left[1-\frac{1}{2} C x^{2}+\frac{3}{8} C^{2} x^{4}\right]+\left[\frac{1}{8} B^{2} x^{2}-\frac{5}{16} B^{2} C x^{4}\right]\right. \\
\\
\left.+\frac{7}{128} B^{4} x^{4}\right\}
\end{array}\right\}
$$

For the denominator, we have

$$
\begin{aligned}
\left|\Delta_{0}\right|= & \left\{\left(\alpha \beta+\lambda^{2}-x^{2}\right)^{2}+(\alpha+\beta)^{2} x^{2}\right\}^{1 / 2} \\
= & \left\{\left(\alpha \beta+\lambda^{2}\right)^{2}+\left(\alpha^{2}+\beta^{2}-2 \lambda^{2}\right) x^{2}+x^{4}\right\}^{1 / 2} \\
= & \left(\alpha \beta+\lambda^{2}\right)\left\{1+\frac{\alpha^{2}+\beta^{2}-2 \lambda^{2}}{2\left(\alpha \beta+\lambda^{2}\right)^{2}} x^{2}+\frac{x^{4}}{2\left(\alpha \beta+\lambda^{2}\right)^{2}}\right. \\
& \left.\quad-\frac{1}{8} \frac{\left(\alpha^{2}+\beta^{2}-2 \lambda^{2}\right)^{2}}{\left(\alpha \beta+\lambda^{2}\right)^{4}} x^{4}-\ldots\right\} \\
= & \left(\alpha \beta+\lambda^{2}\right)\left\{1+\frac{\alpha^{2}+\beta^{2}-2 \lambda^{2}}{2\left(\alpha \beta+\lambda^{2}\right)^{2}} x^{2}\right. \\
& \left.+\frac{(\alpha+\beta)^{2}\left\{4 \lambda^{2}-(\alpha-\beta)^{2}\right\}}{8\left(\alpha \beta+\lambda^{2}\right)^{4}} x^{4}+\ldots\right\}
\end{aligned}
$$

If we now take account of $s$-terms but consider only secondharmonic distortion, that is to say, the $x$ and $x^{2}$ terms in the numerator of $V_{0}$ and the numerical and $x$ term in the denominator, we have, instead of (15),
Numerator $=\left|\rho_{1} \beta_{1}+j \rho_{1} x\left(1-\frac{1}{2} s x\right)+j \rho_{2} \lambda(1-s x)\right|$

$$
\begin{aligned}
& -\left|\rho_{1} \beta+j \rho_{1} x\left(\mathrm{I}-\frac{1}{2} s x\right)-j \rho_{2} \lambda(\mathrm{I}-s x)\right| \\
= & \sqrt{ }\left\{\rho^{2}{ }_{1} \beta^{2}+\left[\rho_{2} \lambda+\left(\rho_{1}-\lambda s \rho_{2}\right) x-\frac{1}{2} s \rho_{1} x^{2}\right]^{2}\right\} \\
& -\sqrt{ }\left\{\rho^{2}{ }_{1} \beta^{2}+\left[\rho_{2} \lambda-\left(\rho_{1}+\lambda s \rho_{2}\right) x+\frac{1}{2} s \rho_{1} x^{2}\right]^{2}\right\} \\
= & A^{1 / 2}\left\{1+\frac{2 \rho_{2} \lambda x}{A}\left(\rho_{1}-\lambda s \rho_{2}\right)+\frac{x^{2}}{A}\left(\rho^{2}{ }_{1}-3 \lambda s \rho_{1} \rho_{2}\right)\right\}^{1 / 2} \\
- & A^{1 / 2}\left\{1-\frac{2 \rho_{2} \lambda x}{A}\left(\rho_{1}+\lambda s \rho_{2}\right)+\frac{x^{2}}{A}\left(\rho_{1}+3 \lambda s \rho_{1} \rho_{2}\right)\right\}^{1 / 2}
\end{aligned}
$$

neglecting $s^{2}$. Expanding this as far as the $x^{2}$ term only, it reduces to

$$
A^{1 / 2}\left\{B x-\left(3 \lambda s \rho_{1} \rho_{2} x^{2} / A\right)+\left(2 \lambda^{3} \rho_{1} \rho^{3} s x^{2} / A^{2}\right)\right\}
$$

where $A$ and $B$ have the same meaning as before in this Appendix. The denominator $|\Delta|$ is given by ( 10 ) ; we have

$$
\Delta=4 s^{2}\left[\left\{j x\left(1-\frac{1}{2} s x\right)+\alpha\right\}\left\{j x\left(1-\frac{1}{2} s x\right)+\beta\right\}+\lambda^{2}(1-2 s x)\right]
$$

so that

$$
|\Delta|=4 s^{2}\left[\left\{\left(\alpha \beta+\lambda^{2}\right)-2 s \lambda^{2} x+\ldots\right\}^{2}+x^{2}\left\{1-\frac{1}{2} s x\right\}^{2}(\alpha+\beta)^{2}\right]^{1 / 2}
$$

and therefore the sole contribution of $|\Delta|$ to second-harmonic distortion is a term $+2 s \lambda^{2} /\left(\alpha \beta+\lambda^{2}\right)$ since all other terms in $|\Delta|$ involve at least $x^{2}$, and the total $x^{2}$-term relative to the $x$-term in the expansion of $V_{o}$ is

$$
s\left[\frac{2 \lambda^{2}}{\alpha \beta+\lambda^{2}}-\frac{3}{2}+\frac{\lambda^{2} \rho^{2}{ }_{2}}{\rho^{2}{ }_{1} \beta^{2}+\rho^{2}{ }_{2} \lambda^{2}}\right]=s\left[\frac{\lambda^{2}-\alpha \beta}{\lambda^{2}+\alpha \beta}+\frac{1}{2} \cdot \frac{\lambda^{2} \rho^{2}{ }_{2}-\beta^{2} \rho^{2}{ }_{1}}{\lambda^{2} \rho^{2}{ }_{2}+\beta^{2} \rho^{2}{ }_{1}}\right]
$$

## APPENDIX 3

## Justification of Simplifying Assumptions in Main Text

The significant essentials of the Foster-Seeley discriminator circuit are contained in Fig. 1, in which the coils $L_{1}$ and $L_{2}$ are closely coupled, and the coils $L_{3}$ and $L_{4}$ are also closely coupled. It is convenient to call the coupling coefficient between coils 1 and 2 , $1-\mu_{12}$, where $\mu_{12}$ is small (of order 0.05 ), and the coupling coefficient
between 3 and $41-\mu_{34}$, where $\mu_{34}$ is similarly small. The remaining coupling coefficients are small (of order 0.05 ), and we shall denote the coupling coefficient between coil $k$ and coil $j$ by $\lambda_{k j}$ except in the cases of close coupling already specified. We can then expect to find

$$
\left.\begin{array}{ll}
\left|\lambda_{1 k}-\lambda_{2 k}\right|<\mu_{12} \lambda_{k} & (k=3,4)  \tag{3.1}\\
\left|\lambda_{j 3}-\lambda_{j_{1}}\right|<\mu_{34} \lambda_{j} & (j=1,2)
\end{array}\right\}
$$

where $\lambda_{k}$ is the average of $\lambda_{1 k}$ and $\lambda_{2 k}$ and $\lambda_{j}$ is the average of $\lambda_{j_{3}}$ and $\lambda_{j_{4}}$.

The reason for the inequalities (3.1) is that the high coupling coefficient between coils I and 2 can only be obtained if these coils are close together, and therefore at approximately the same distance from coil 3 and from coil 4 ; similarly, the coils 3 and 4 must be close together and therefore at approximately the same distance from coils I and 2. The inequalities (3.1) signify that there can only be slight asymmetry.

Matrix methods are used throughout this Appendix. We first derive the impedance matrix expressing the voltages $V_{k}$ across the coils in terms of the currents $I_{k}$ in them as if the other elements of Fig. 3 were absent, and obtain, with the normalized units of the main text,

$$
\left[\begin{array}{l}
V_{1}  \tag{3.2}\\
V_{2} \\
V_{3} \\
V_{4}
\end{array}\right]=p\left[\begin{array}{llll}
1 & 1-\mu_{12} & \lambda_{13} & \lambda_{14} \\
1-\mu_{12} & 1 & \lambda_{23} & \lambda_{24} \\
\lambda_{13} & \lambda_{23} & 1 & 1-\mu_{34} \\
\lambda_{14} & \lambda_{24} & 1-\mu_{34} & 1
\end{array}\right]\left[\begin{array}{c}
I_{1} \\
I_{2} \\
I_{3} \\
I_{4}
\end{array}\right]
$$

Now, in view of (3.1) it is clear that the second row of the square matrix in (3.2) is very similar to the first, and the fourth row is very similar to the third. It follows that $\left|V_{1}-V_{2}\right|$ is small compared to $V_{1}$ and $V_{2}$, and $\left|V_{3}-V_{4}\right|$ is small compared to $V_{3}$ and $V_{4}$, and similarly with the $I \mathrm{~s}$. We therefore introduce new voltage variables

$$
\left.\begin{array}{ll}
v_{1}=\frac{1}{2}\left(V_{1}-V_{2}\right) ; \quad v_{2}=\frac{1}{2}\left(V_{1}+V_{2}\right) ;  \tag{3.3}\\
v_{3}=\frac{1}{2}\left(V_{3}+V_{4}\right) ; \quad v_{4}=\frac{1}{2}\left(V_{3}-V_{4}\right)
\end{array}\right\}
$$

and new current variables

$$
\begin{equation*}
i_{1}=\left(I_{1}-I_{2}\right) ; i_{2}=I_{1}+I_{2} ; i_{3}=I_{3}+I_{4} ; i_{4}=I_{3}-I_{4} \tag{3.4}
\end{equation*}
$$

so that

$$
\left.\begin{array}{ll}
v_{2} \approx V_{1} \text { or } V_{2} ; \quad v_{3} \approx V_{3} \text { or } V_{4} ; \quad v_{1} \text { and } v_{4} \text { are small }  \tag{3.5}\\
i_{2} \approx 2 I_{1} \text { or } 2 I_{2} ; \quad i_{3} \approx 2 I_{3} \text { or } 2 I_{4} ; \quad i_{1} \text { and } i_{4} \text { are small }
\end{array}\right)
$$

Our matrix equation (3.2) now becomes

$$
\left[\begin{array}{l}
v_{1}  \tag{3.6}\\
v_{2} \\
v_{3} \\
v_{4}
\end{array}\right]=p\left[\begin{array}{llll}
\frac{1}{2} \mu_{12} & 0 & \sigma^{\prime} & \sigma^{\prime \prime} \\
0 & 1-\frac{1}{2} \mu_{12} & \rho & \sigma \\
\sigma^{\prime} & \rho & 1-\frac{1}{2} \mu_{34} & 0 \\
\sigma^{\prime \prime} & \sigma & 0 & \frac{1}{2} \mu_{34}
\end{array}\right]\left[\begin{array}{l}
i_{1} \\
i_{2} \\
i_{3} \\
i_{4}
\end{array}\right]
$$

where

$$
\left.\begin{array}{l}
\rho=\frac{1}{4}\left(\lambda_{13}+\lambda_{14}+\lambda_{23}+\lambda_{24}\right) ; \quad \sigma=\frac{1}{4}\left(\lambda_{13}-\lambda_{14}+\lambda_{23}-\lambda_{24}\right)  \tag{3.7}\\
\sigma^{\prime}=\frac{1}{4}\left(\lambda_{13}+\lambda_{14}-\lambda_{23}-\lambda_{24}\right) ; \quad \sigma^{\prime \prime}=\frac{1}{4}\left(\lambda_{13}-\lambda_{14}-\lambda_{23}+\lambda_{24}\right)
\end{array}\right\}
$$

It follows from Equ. (3.1) that $\sigma, \sigma^{\prime}$ and $\sigma^{\prime \prime}$ (which may be positive or negative) are all of order $\frac{1}{2} \rho\left(\mu_{12}+\mu_{34}\right)$ at most; in other words, if we regard $\mu_{12}, \mu_{34}$ and $\rho$ as small quantities of the first order, say 0.05 or so, then $\sigma, \sigma^{\prime}$ and $\sigma^{\prime \prime}$ are of the second order.

We now require to invert the matrix (3.6) so that the quantities $i_{1}, i_{2}, i_{3}$ and $i_{4}$ are expressed in terms of the quantities $v_{1}, v_{2}, v_{3}$ and $v_{4}$.

To do this, we make use of a special result applicable to matrices having any number of rows and columns, where the principaldiagonal terms are at least an order of magnitude greater than the remainder. For the four-row and four-column matrices with which we are here concerned, this result is perhaps best expressed in the form

$$
\left[\begin{array}{cccc}
l & a & b & c  \tag{3.8}\\
d & \mathrm{I} & e & f \\
g & h & 1 & k \\
l & m & n & \mathrm{I}
\end{array}\right]\left[\begin{array}{rrrr}
\mathrm{I} & a & -b & -c \\
-d & \mathrm{I} & -e & -f \\
-g & -h & 1 & -k \\
-l & -m & -n & \mathrm{l}
\end{array}\right]=I
$$

where $I$ is the unit matrix, having its four principal-diagonal elements unity and the remaining elements zero; this result is true provided that we can neglect all products of $a, b, c$, etc. To apply this result we rewrite (3.6) in the form

$$
\left.\begin{array}{l}
{\left[\begin{array}{l}
v_{1} \\
v_{2} \\
v_{3} \\
v_{4}
\end{array}\right]=p\left[\begin{array}{llll}
1 & 0 & \sigma^{\prime} /\left(1-\frac{1}{2} \mu_{34}\right) & 2 \sigma^{\prime \prime} / \frac{1}{2} \mu_{34} \\
0 & \mathrm{I} & \rho /\left(1-\frac{1}{2} \mu_{34}\right) & 2 \sigma / \frac{1}{2} \mu_{34} \\
2 \sigma^{\prime} / \mu_{12} & \rho /\left(1-\frac{1}{2} \mu_{12}\right) & \mathrm{I} & 0 \\
2 \sigma^{\prime \prime} / \mu_{12} & \sigma /\left(\mathrm{I}-\frac{1}{2} \mu_{12}\right) & 0 & 1
\end{array}\right]} \\
\times\left[\begin{array}{lllll}
\frac{1}{2} \mu_{12} i_{1} \\
\left(1-\frac{1}{2} \mu_{12}\right) i_{2} \\
\left(1-\frac{1}{2} \mu_{34}\right) i_{3}
\end{array}\right]  \tag{3.9}\\
\\
\frac{1}{2} \mu_{34^{4} i_{4}}
\end{array}\right] \quad \ldots \quad \ldots \quad . \begin{array}{llll}
\end{array}
$$

It will be convenient to define

$$
\begin{equation*}
q_{1}=\frac{1}{2} \mu_{12} \quad q_{2}=1-\frac{1}{2} \mu_{12} \quad q_{3}=1-\frac{1}{2} \mu_{34} \quad q_{4}=\frac{1}{2} \mu_{34} \tag{3.10}
\end{equation*}
$$

simply in order to save space; $q_{1}$ and $q_{4}$ are then small quantities of the first order while $q_{2}$ and $q_{3}$ are nearly unity. Inverting (3.9) by means of (3.8) and expressing the result in terms of $q$ not $\mu$ we have

$$
\left[\begin{array}{l}
q_{1} i_{1}  \tag{3.11}\\
q_{2} i_{2} \\
q_{3} i_{3} \\
q_{4} i_{4}
\end{array}\right]=\frac{1}{p}\left[\begin{array}{llll}
1 & 0 & -\sigma^{\prime} / q_{3} & -\sigma^{\prime \prime} / q_{4} \\
0 & 1 & -\rho / q_{3} & -\sigma / q_{4} \\
-\sigma^{\prime} / q_{1} & -\rho / q_{2} & 1 & 0 \\
-\sigma^{\prime \prime} / q_{1} & -\sigma / q_{2} & 0 & 1
\end{array}\right]\left[\begin{array}{l}
v_{1} \\
v_{2} \\
v_{3} \\
v_{4}
\end{array}\right]
$$

or

$$
\left[\begin{array}{l}
i_{1}  \tag{3.12}\\
i_{2} \\
i_{3} \\
i_{4}
\end{array}\right]=\frac{1}{p}\left[\begin{array}{llll}
1 / q_{1} & 0 & -\sigma^{\prime} / q_{1} q_{3} & -\sigma^{\prime \prime} / q_{1} q_{4} \\
0 & 1 / q_{2} & -\rho / q_{2} q_{3} & -\sigma / q_{2} q_{4} \\
-\sigma^{\prime} / q_{1} q_{3}-\rho / q_{2} q_{3} & 1 / q_{3} & 0 \\
-\sigma^{\prime \prime} / q_{1} q_{4}-\sigma / q_{2} q_{4} & 0 & 1 / q_{4}
\end{array}\right]\left[\begin{array}{l}
v_{1} \\
v_{2} \\
v_{3} \\
v_{4}
\end{array}\right]
$$

and if the values of $i_{1}$, etc., derived from (3.12) are substituted back into (3.6), the error is at worst of the second order.

Now consider the capacitances alone. We assume that these are effectively as in Fig. 1. $C_{1}$ may be made up partly of stray primary capacitance and partly of tuning capacitance deliberately added; there is no need to distinguish between these two parts as long as $C_{1}$ has the correct total value. $C_{2}, C_{3}$ and $C_{4}$ are all stray capacitances; the secondary tuning capacitance $C$ is placed across the whole secondary. Mutual capacitances between the coils are here neglected; they can if necessary be allowed for by some adjustment in the effective values of the coupling coefficients or replacing some of the zeros in the matrix (3.13) below by small quantities, but the procedure would be unaltered. For our present purpose of general understanding, these capacitances are merely an irrelevant complication. The matrix expressing currents in terms of voltages for the capacitances alone, in terms of the original variables, is

$$
\left[\begin{array}{l}
I_{1}  \tag{3.13}\\
I_{2} \\
I_{3} \\
I_{4}
\end{array}\right]=\left[\begin{array}{cccc}
p C_{1} & 0 & 0 & 0 \\
0 & p C_{2} & 0 & 0 \\
0 & 0 & p\left(C_{3}+C\right) & p C \\
0 & 0 & p C & p\left(C_{4}+C\right)
\end{array}\right]\left[\begin{array}{l}
V_{1} \\
V_{2} \\
V_{3} \\
V_{4}
\end{array}\right]
$$

In terms of the variables $i$ and $v(3.13)$ becomes

$$
\left[\begin{array}{l}
i_{1}  \tag{3.14}\\
i_{2} \\
i_{3} \\
i_{4}
\end{array}\right]=\left[\begin{array}{cccc}
p\left(C_{1}+C_{2}\right) p\left(C_{1}-C_{2}\right) & 0 & 0 \\
p\left(C_{1}-C_{2}\right) p\left(C_{1}+C_{2}\right) & 0 & 0 \\
0 & 0 & p\left(4 C+C_{3}+C_{4}\right) & p\left(C_{3}-C_{4}\right) \\
0 & 0 & p\left(C_{3}-C_{4}\right) & p\left(C_{3}+C_{4}\right)
\end{array}\right]\left[\begin{array}{l}
v_{1} \\
v_{2} \\
v_{3} \\
v_{4}
\end{array}\right]
$$

To obtain the currents in terms of the voltages for coils and capacitances only, it is merely necessary to add the matrices on the right-hand sides of (3.12) and (3.13), but we need to consider how to allow for the coil losses and the diode loads before we can decide on the correct values of $C_{1}$ and $C$, which are under our control. The coil losses give rise to a matrix analogous to that in (3.14) in which $p C_{1}$ is replaced by $G_{1}$, the total loss across the primary, including resistance deliberately added, and $p C_{2}$ by $g_{2}, p C_{3}$ by $g_{3}$ and $p C_{4}$ by $g_{4}$. $p C$ must be replaced by $G_{s}$, the resistance deliberately added across the secondary. This matrix must be added to those of (3.14) and (3.12) to give currents in terms of voltages lor the combined system of coils, capacitances and losses, but we have still the diodes to take into account. Let us therefore consider the diode loads alone. With our original variables, the relations expressing current in terms of voltage could be written

$$
\left.\begin{array}{l}
I_{1}=0 \\
I_{2}=d_{3}\left(V_{2}+V_{3}\right)+d_{4}\left(V_{2}-V_{4}\right)  \tag{3.15}\\
I_{3}=d_{2}\left(V_{2}+V_{3}\right) ; \quad I_{4}=-d_{4}\left(V_{2}-V_{4}\right)
\end{array}\right\}
$$

These, rearranged in terms of our new variables, become

$$
\left[\begin{array}{l}
i_{1}  \tag{3.16}\\
i_{2} \\
i_{3} \\
i_{4}
\end{array}\right]=\left[\begin{array}{rrrr}
\left(d_{3}+d_{4}\right) & -\left(d_{3}+d_{4}\right) & -\left(d_{3}-d_{4}\right) & -\left(d_{3}+d_{4}\right) \\
-\left(d_{3}+d_{4}\right) & \left(d_{3}+d_{4}\right) & \left(d_{3}-d_{4}\right) & \left(d_{3}+d_{4}\right) \\
-\left(d_{3}-d_{4}\right) & \left(d_{3}-d_{4}\right) & \left(d_{3}+d_{4}\right) & \left(d_{3}-d_{4}\right) \\
-\left(d_{3}+d_{4}\right) & \left(d_{3}+d_{4}\right) & \left(d_{3}-d_{4}\right) & \left(d_{3}+d_{4}\right)
\end{array}\right]\left[\begin{array}{l}
v_{1} \\
v_{2} \\
v_{3} \\
v_{4}
\end{array}\right]
$$

As the various types of element we have hitherto considered separately are in parallel, the admittance matrix for the whole system is obtained by adding the admittance matrices already obtained for the various parts. We thus obtain for the whole system of Fig. 1

$$
\begin{equation*}
[i]=[Y][v] \tag{3.17}
\end{equation*}
$$

where [ $i$ ], [ $v$ ] are the column matrices with elements $i_{1}, i_{2}, i_{3}, i_{4}$ and
$v_{1}, v_{2}, v_{3}, v_{4}$ respectively, as in (2.16), and [ $Y$ ] is a square matrix with four rows and columns having elements $y_{i j}(i, j=1,2,3,4)$ defined as follows:

$$
\begin{align*}
y_{11} & =\frac{1}{p q_{1}}+p\left(C_{1}+C_{2}\right)+\left(G_{1}+g_{2}\right)+\left(d_{3}+d_{4}\right) \\
y_{12}=y_{21} & =p\left(C_{1}-C_{2}\right)+\left(G_{1}-g_{2}\right)-\left(d_{3}+d_{4}\right) \\
y_{13}=y_{31} & =\frac{\sigma^{\prime}}{p q_{1} q_{3}}-\left(d_{3}-d_{4}\right) \\
y_{14}=y_{41} & =-\frac{\sigma^{\prime \prime}}{p q_{1} q_{4}}-\left(d_{3}+d_{4}\right) \\
y_{22} & =\frac{1}{p q_{2}}+p\left(C_{1}+C_{2}\right)+\left(G_{1}+g_{2}\right)+\left(d_{3}+d_{4}\right) \\
y_{23}=y_{32} & =-\frac{\rho}{p q_{2} q_{3}}+\left(d_{3}-d_{4}\right) \\
y_{24}=y_{42} & =-\frac{\sigma}{p q_{2} q_{4}}+\left(d_{3}+d_{4}\right) \\
y_{33} & =\frac{1}{p q_{3}}+p\left\{4 C+C_{3}+C_{4}\right\}+\left\{4 G_{5}+g_{3}+g_{4}\right\}+\left(d_{3}+d_{4}\right) \\
y_{34}=y_{43} & =p\left(C_{3}-C_{4}\right)+\left(g_{3}-g_{4}\right)+\left(d_{3}-d_{4}\right) \\
y_{44} & =\frac{1}{p q_{4}}+p\left(C_{3}+C_{4}\right)+\left(g_{3}+g_{4}\right)+\left(d_{3}+d_{4}\right) \tag{3.18}
\end{align*}
$$

Now when the discriminator is in operation, since only $L_{1}$ has an external current supply, we have

$$
\begin{equation*}
I_{2}=0 \text { (i.e., } i_{1}=i_{2} \text { ) } i_{3}=i_{4}=0 \tag{3.19}
\end{equation*}
$$

and (3.17) can be written in full

$$
\begin{align*}
& i_{1}=y_{11} v_{1}+y_{12} v_{2}+y_{13} v_{3}+y_{14} v_{4} \\
& i_{2}=y_{12} v_{1}+y_{22} v_{2}+y_{23} v_{3}+y_{24} v_{4}  \tag{3.20}\\
& i_{33}=y_{13} v_{1}+y_{23} v_{2}+y_{33} v_{3}+y_{34} v_{4} \\
& i_{4}=y_{14} v_{1}+y_{24} v_{2}+y_{34} v_{3}+y_{44} v_{4}
\end{align*}
$$

Subiract the second of (3.20) from the first, and then use the last of (3.20) to eliminate $v_{4}$. The left-hand side is zero from (3.19) so that

$$
\begin{align*}
& 0=\left\{y_{11}-y_{12}-\frac{y_{14}\left(y_{14}-y_{24}\right)}{y_{44}}\right\} v_{1}+\left\{y_{12}-y_{22}-\frac{y_{24}\left(y_{14}-y_{24}\right)}{y_{44}}\right\} v_{2} \\
& +\left\{y_{13}-y_{23}-\frac{y_{34}\left(y_{14}-y_{24}\right)}{y_{44}}\right\} v_{3} \ldots \ldots \tag{3.21}
\end{align*} \ldots \quad \ldots \quad(3.21) \text {... }
$$

Now in (3.18), before any allowance is made for tuning, $y_{11}$ and $y_{44}$ are of order $-1, y_{12}, y_{22}, y_{14}, y_{33}$ are of order zero, and $y_{13}, y_{23}, y_{24}$ and $y_{34}$ are of order 1. Hence $v_{1}$ from (3.21) is of the first order of small quantities compared to $v_{2}$ and $v_{3}$, for the cocfficient of $v_{1}$ in (3.21) contains $y_{11}$ in the numerator, whereas the other coefficients are at most of order zero. It then follows by substitution in the last of (3.20) (with $i_{4}$ zero) that $v_{4}$ is of the second order compared with $v_{2}$ and $v_{3}$, since $y_{41}$ is of order -1 . We may therefore omit $v_{4}$ and the last of (3.20) from now on.

Now multiply the first of (3.20) by $y_{12} / y_{11}$ and subtract from the second, and multiply the first of $(3.20)$ by $y_{13} / y_{11}$ and subtract from the third. (3.20) become, in view of (3.19),

$$
\begin{align*}
{\left[1-\frac{y_{12}}{y_{11}}\right] i_{1} } & =\left[y_{22}-\frac{y^{2}{ }_{12}}{y_{11}}\right] v_{2}+\left[y_{23}-\frac{y_{12} y_{13}}{y_{11}}\right] v_{3} \\
-\frac{y_{13}}{y_{11}} i_{1} & =\left[y_{23}-\frac{y_{12} y_{13}}{y_{11}}\right] v_{2}+\left[y_{33}-\frac{y^{2}}{y_{13}}\right] v_{3} \tag{3.22}
\end{align*}
$$

Now (3.22) are of the same form as (7) in the main text, for $y_{13} / y_{11}$ is of the second order so that the left-hand side of the second of (3.22) is effectively zero and $i_{5}$ is zero in (7). Thus the imperfections of coupling considered in this Appendix can be allowed for by replacing the circuit of Fig. 1 by that of Fig. 2, the coupling $k / p$ being replaced by $y_{23}-\left(y_{12} y_{13} / y_{11}\right)$. The tuning conditions become that the imaginary parts of
$y_{22}-\left(y^{2}{ }_{12} / y_{11}\right)$ and $y_{33}-\left(y^{2}{ }_{13} / y_{11}\right)$
must be zero respectively for the primary and secondary tuning. The term $y^{2}{ }_{13} / y_{11}$ is of the third order-completely negligible.

## REFERENCE

${ }^{1}$ See 'Basic Mathematics for Radio Engineers', by F. M. Colebrook and J. W. Head, Iliffe \& Sons, London, revised edition 1957. [See also p. 67 of this issue. Ed.]

# THE LAMB SHIFT-1: The Electron and its Self-Energy 

What we believe as hard facts about the electron are that it has a charge $e$ of $-4.8 \times 10^{-10}$ absolute e.s.u., and a mass $m$ which has the value $m_{0}=9.1 \times 10^{-28} \mathrm{gm}$ when it is at rest or moving slowly, increasing to $m_{0}\left(1-v^{2} / c^{2}\right)^{-1}$ when its velocity $v$ is appreciable compared with $c$, the velocity of light. The energy equivalent of its rest-mass, $m_{0} c^{2}$, is about $8 \times 10^{-7} \mathrm{ergs}$, or say 0.5 MeV .

As often happens with vital statistics, the length measurements associated with it are less precise, in the sense that we are not quite sure what is really being measured. If it is a little round particle, then classical theory assigns it a radius $r_{c}=e^{2} / m_{0} c^{2}=2.82 \times 10^{-13} \mathrm{~cm}$. If it acts as a wave, as diffraction experiments suggest, then its 'Compton wavelength' is $\lambda_{c}=h / m_{0} c$, (where $h$ is $6.5 \times 10^{-27}$ units), which gives $2.4 \times 10^{-10} \mathrm{~cm}$. For most purposes of modern theory, people do not worry very much about its dimensions. You will see why in a minute.

But the really uncertain quantity about the electron is its self-energy. This may be defined as the energy which the electron itself contributes to the field in which it is situated. According to classical theory, the electrostatic energy of the whole of the field surrounding a sphere of charge $e$ and radius $r$ is $0.6 e^{2} / r$. If this is equated to the mass-energy $m_{0} c^{2}$, then $r$ works out to be $0.6 r_{c}$.

Unfortunately, whatever properties may be ascribed to the electron at the beginning or end of the process, the operations of wave-mechanics are performed on wavefunctions which are, like other mathematical functions, expressed in terms of the space co-ordinates of points. It is true that the uncertainty principle forbids the determination of the position of a point with ideal mathematical accuracy, but it does not vitiate arguments that stop short of the act of measurement. The electron, it appears, is being treated as if it were a point-charge. If this be so, then $0.6 e^{2} / r$ is infinitely great, and if this classical self-energy is equated to $m c^{2}$, then it follows that $m$ (the self-mass) must be infinitely great as well.

Now, the ideas of infinitely great self-energy and an infinite electron mass seem very strange; but, when you come to think of it, not so much stranger than that of a mathematical point. We can regard the two extremes as complementary unobservables, which the mathematicians of 'infinite-resource-and-sagacity' can control with equal impartiality. After all, the whole art in their projective geometry consists of hurling the problem to infinity and fetching it back again solved; and so long as they remember to renormalize the mass at the end of the sum it is perfectly reasonable to use similar tactics in mathematical physics. But it seems really that, as with potential energy in more familiar problems, the absolute value of the self-energy of an electron in any situation is almost uninteresting even if it can be determined; the important
quantity is the change in self-energy that accompanies a change in situation. This, if it is to mean anything at all, must necessarily be finite.

The real point at issue is whether or not differences in self-energy contribute appreciably to the total energy difference between the levels available to a bound electron in the Coulomb field surrounding the nucleus of an atom. In the early Bohr-Sommerfeld theory, only the Coulomb-field potential energy and the kinetic energy of the circulating electron (with due regard to relativity effects) were counted. The Dirac theory of 1928 attributed a good deal more to the electron in the way of spin, magnetic moment, and relativistic behaviour; and it gave a quite complete calculation of the levels of the one-electron system of the hydrogen atom. The accuracy was so high that any clearly observed disagreement of the order of a few parts in a million would have been taken up for investigation and possible discrepancies have indeed been discussed all the time. The Dirac theory did not take the effect of self-energy into account; it was suspected from about 1938 that there might be at least two processes, which were quite unforeseen by the theory, leading to differences in self-energy for different energy levels and, in particular, causing the symmetrical wavefunction (or ' $S$ ') levels in the hydrogen atom to be a little higher than they were thought to be.

It was very difficult indeed to establish this by optical spectroscopy. The difference, expressed in wave-numbers, is only about $0.033 \mathrm{~cm}^{-1}$; this is of about the same order as the Doppler broadening of spectral lines, and even when that is reduced by using a low-temperature source it would require a resolving power (or spectroscopic $Q$ ) of about a quarter of a million to detect such a shift and measure it. This has been done, but the first really conclusive measurements were made as late as 1948 by Kuhn and Series.

A wave-number of $0.033 \mathrm{~cm}^{-1}$ corresponds to a frequency of about $1,000 \mathrm{Mc} / \mathrm{s}$ and a radio wavelength of 30 cm , or so-which is right within the radio-frequency spectroscopy range. And in 1947, using radio techniques, the now famous 'Lamb Shift' was observed by W. E. Lamb and R. C. Retherford. It will take the whole of the March 'Fringe' to try to explain this work. The present article deals only with the shift itself, and the reasons advanced for it.

## The Dirac Electron and the Vacuum

The expression for the kinetic energy of an electron obtained by Dirac admitted of both positive and negative values. Using the exclusion principle, he suggested that the negative values were states already filled with positive electrons; and that a vacuum is not just emptiness, but stored with an infinite number of positive electrons.

(a)

(b)

Fig. 1. (a) Short-range repulsion between electrons 1 and 2, pictured as the emission and absorption of viriual photon, or photons
(b) Change in the self-energy of an electron when in a fluctuating field, during the interval between the emission of a virtual photon and its subsequent re-absorption. Here $\left(m_{b}+\Delta n\right)$ is what is ordinarily measured as the mass; and $m_{b}$, called the 'bare' mass, is what remains after $\Delta m$ has been parked temporarily as a virtual photon

One consequence of this picture, which has only more recently been suggested, is that the presence of an ordinary electron induces polarization of the infinite vacuum, similar to that to be expected in a dielectric, but far more extensive. Again, the possibility of infinite self-energy appears, though this time without involving any $r$. In the hydrogen atom, there is a polarization effect due to the proton charge also. But the overall result of polarization is only about $3 \%$ of the total Lamb Shift.

## Interaction with Radiation

Matters become even more difficult to visualize when the electromagnetic field in the neighbourhood of an electron is itself regarded as being composed of quanta which are subject to statistical fluctuations. Even if the field is nominally zero, this simply means that it fluctuates about a zero value; and an electron in such a situation is provoked, if it is in an excited state, to emit radiation itself. If it is not in an excited state, so that the energy for real radiation is lacking, it has to make do with virtual radiation! The Coulomb-law repulsion between two electrons when they are very close together can be pictured (if that is a fair term) as a chain of operations in which the field of each stimulates the other to emit radiation, which is in in turn absorbed by the original 'each'. The radiation is, however, only virtual-the so-called 'virtual photon'. One property of the virtual photon will not surprise you. It may carry infinite energy. Things seem to have reached a stage at which it would be refreshing to find something that doesn't.

The same kind of thing happens when we consider a single electron in a fluctuating radiation field. Provoked to emit a virtual photon, it duly obliges; having no partner to trade with, it re-absorbs the thing itself [Fig. 1 (b)]. This diagram is hard to interpret literally, for it looks as though the virtual photon has to wait about for the more leisurely moving electron. It really means simply that part of the self-energy of the electron is temporarily loaned to the surrounding vacuum, to be recalled later. If $\Delta E$ is the energy of the photon, and $\Delta t$ the time for which it is out, then $\Delta E \times \Delta t=h / 2 \pi$. If
$\Delta E$ is large, than $\Delta t$ must be very small. But, if $\Delta t$ is very small, so must be the distance represented in Fig. 1 (b). This kind of thing, then, may well be relevant to very short-range actions, incredible though it looks when drawn in a diagram.

But a temporary change of energy $\Delta E$ means also a temporary change of mass $\Delta m$; so for the duration $\Delta t$ the mass of the electron is altered. If it is not subjected in the meantime to any external force, then the temporary change of $\Delta m$ does not matter. If, however, it is in an accelerating electromagnetic field, or is in a bound state in the field due to an atomic nucleus, then things can happen to the electron during the interval while the $\Delta m$ is out and about; the total energy of the reunited system will then differ from that which would have resulted if there had been no virtual photon process.

If the law of conservation of energy holds for Fig. 1 (b), then

$$
m=m_{b}+\Delta m
$$

Here $m$ is the ordinary finite observed electron mass; $\Delta m$ probably infinite and certainly unobservable; $m_{b}$, called the 'bare mass' has to be probably infinite, certainly unobservable, slightly different from $\Delta m$, and negative in sign. Becoming acclimatized to this world "of infinite jest, of most excellent fancy", one can accept the items term by term. It is rather harder to understand the equation, though, since violations of the law of conservation of energy would seem to be permissible in this set-up.

Perhaps all that I have really made intelligible in the course of these last two sections is that both the polarization of the vacuum, and the interaction between the electron and radiation, modify the self-energy of the electron; that because of this the energy levels within, say, the hydrogen atom are not quite what they are made

Fig. 2. Sommerfeld orbits of the hydrogen atom, for $n=1,2$, and 3. Taken from his "Atomic Structure and Spectral Lines", 1923 edition. The eccentricity of the $2 p$ ellipse is $\sqrt{3} / 2$; that of the $3 p$ ellipse $\sqrt{5} / 3$, and of the 3 d ellipse $\sqrt{8} / 3$. The only transitions allowed in this rudimentary scheme are shown by vertical lines. Since the greatest energy separation is that between $2 s$ and $2 p$, the lines 1 and 3 are fairly close together, and the main $H_{\alpha}$ doublet separation is between this pair and 2


(a)


Fig. 3. The $n=2$ and $n=3$ levels of hydrogen (a) according to the Dirac theory, and (b) including the self-energy effect. The separations are not drawn to scale. In (a) there are five distinct components only to the $H_{\alpha}$ line, as both sets of ${ }^{2} S_{\frac{1}{2}}$ and ${ }^{2} P_{1}$ levels are degenterate. In $(b)$ the $2^{2} S_{\frac{1}{2}}$ and $2^{2} P_{\frac{1}{3}}$ levels are separated by $0.033 \mathrm{~cm}^{-1}$, and there is a smaller separation between the $3^{2} S_{\frac{1}{2}}$ and $3^{2} P_{\frac{1}{2}}$ levels. The $H_{\alpha}$ line has seven components, the additional two coming from the splitting of 2 into $2 a$ and $2 b$, and of 3 into $3 a$ and $3 b$. The " $H_{\alpha}$ doublet" separation that figured so prominently in Sommerfeld's discussion is that between the $2^{2} P_{\frac{1}{2}}$ and $2^{2} P_{3 / 2}$ levels. The arrowed lines on each diagram indicate the transitions giving rise to radiation
out to be; and that a rather fanciful-seeming mechanism has been advanced to explain this. The reason why the whole thing is important is that it may eventually lead to a better understanding of the operation of short-range forces between particles; the Lamb Shift can be regarded as the first clear experimental justification for this approach. Actually, the mechanism affects the magnetic moment of the electron as well; and this anomalous magnetic moment fits into the picture. But that is another story, to be dealt with next month.

The next stage in the discussion is to identify the hydrogen-atom levels that are concerned in the originally observed $0.033 \mathrm{~cm}^{-1}$ Lamb Shift. This is most easily done by stepping back to the ideas and terms of more than thirty years ago.

## Energy Levels in the Hydrogen Atom

In the earliest Bohr theory of the hydrogen atom, the electron could circulate round the proton in any one of a series of non-radiating circular orbits, such that the angular momentum equalled $n h / 2 \pi$, where $n=1,2,3 \ldots$ is an integer now called the principal quantum number for the orbit. The total energy $E_{n}$ in the $n$th orbit, the sum of the kinetic energy of rotation and the Coulombfield potential energy, worked out to $E_{n}=-\frac{2 \pi^{2} m e^{4}}{n^{2} h^{2}}$ ergs, the negative sign indicating that $E_{n}$ is taken as zero when $n$ is infinitely great. The radius of each orbit, and the velocity of the electron are calculated from the ordinary

TABLE

| Quantum <br> number <br> $n$ | Orbit radius | Velocity <br> expressed as <br> fraction $v / c$ <br> of velocity <br> of light | Total energy <br> $E$, in <br> electron-volts |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 1 | $a_{1}=0.53 \times 10^{-8} \mathrm{~cm}$ | $1 / 137$ | -13.53 eV |
| 2 | $4 a_{1}=2.12 \times 10^{-8} \mathrm{~cm}$ | $1 /(2 \times 137)$ | -3.38 eV |
| 3 | $9 a_{1}=4.77 \times 10^{-8} \mathrm{~cm}$ | $1 /(3 \times 137)$ | -1.50 eV |
| $-n$ | $\overline{n^{2} a_{1}}$ | $1 /(n \times 137)$ | $-\mathrm{E}_{1} / n^{2} \mathrm{eV}$ |

(b)
formulæ for circular motion, and specimen figures shown in Table 1.

The figure $1 / 137$ in the third column is, I believe, the origin of the expression "a smashing little number". It is the value of the fine-structure constant $2 \pi e^{2} / h c$, which seems to turn up in many important calculations.

The lowest state is $n=1$; from any higher state, originally excited by absorbing the appropriate energy

| Principal quantum number <br> $n$ | Azimuthal quantum number $l$ | Symbol | Energy difference due to relativity effect |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & 2 \\ & 2 \end{aligned}$ | $\begin{aligned} & 0 \\ & 1 \end{aligned}$ | $\begin{aligned} & 2 \mathrm{~s} \text { (circle) } \\ & 2 \mathrm{p} \end{aligned}$ | $\} 0.365 \mathrm{~cm}^{-1}$ |
| 3 3 3 | $\begin{aligned} & 0 \\ & 1 \\ & 2 \end{aligned}$ | $\left.\begin{array}{l} 3 \mathrm{~s} \text { (circle) } \\ 3 \mathrm{p} \\ 3 \mathrm{~d} \end{array}\right\}$ | $\begin{aligned} & 0.0036 \mathrm{~cm}^{-1} \\ & 0.0107 \mathrm{~cm}^{-1} \end{aligned}$ |

difference, return to a lower state happens with the emission of the energy difference $\Delta E$ as a quantum of radiation of frequency $\nu$ given by $\Delta E=h \nu$; the wavelength $\lambda=c / \nu$, or the wave-number $1 / \lambda$ can be used to denote this. The series of emissions which end up with the electron on $n=2$ give lines in the visible spectrum, the Balmer series for which the wave-numbers are given successively by inserting $n=3,4,5 \ldots$ in the formula

$$
\frac{1}{\lambda}=\frac{2 \pi^{2} m e^{4}}{c h^{3}}\left(\frac{1}{2^{2}}-\frac{1}{n^{2}}\right)
$$

The first of these, the red $\mathrm{H}_{\alpha}$ line, for which $n=3$, has wave-number $15,237 \mathrm{~cm}^{-1}$, wavelength $6.563 \times 10^{-5} \mathrm{~cm}$, and quantum energy 1.88 eV .

But the Balmer series lines are really pairs of lines very close together (doublets) with a separation between the lines of $0.365 \mathrm{~cm}^{-1}$, suggesting that the $n=2$ level really consists of two which differ slightly in energy. The members of the doublets themselves can be further resolved, due to multiplicity of the higher levels also. The Sommerfeld explanation of this is that there are $n$
different types of possible orbit for each principal quantum number, specified by an azimuthal quantum number $l$, which can have the values $0,1,2 \ldots$ up to $(n-1)$. For $l=0$, the orbit is still a circle; $l=1, l=2$, etc., denotes ellipses of progressively greater eccentricity (Fig. 2). The code letters $\mathrm{s}, \mathrm{p}, \mathrm{d}, \mathrm{f}$ are used for $l=0$, $l=1, l=2, l=3$ respectively. While the total energy for all orbits of the same $n$ should be the same in the absence of relativity effects, the variation of mass with velocity operates differently on ellipses of different eccentricity, as calculated in Table 2. This old-fashioned approach is just as good as more recent theory for the purpose of classifying energy levels; and the symbols are still in use, though they do not nowadays stand for Kepler ellipses but for wave-equations called orbitals.

It looks as if there should be six independent ways of generating the $\mathrm{H}_{\alpha}$ line; in fact, there are here only three, because $l$ can only change by $\pm 1$; other transitions are forbidden. As Fig. 3 illustrates, there are really more levels than in Fig. 2, and seven possible ways in all!

Further quantum numbers, the inner quantum number $j$, and a magnetic quantum number $m$, were introduced by Sommerfeld to deal with the complex spectra observed when the source was in a magnetic field. The modern theory, although it does not regard the energy levels or states as orbits in which a little round particle circulates, still preserves this notation. Nowadays, $j$ is the vector resultant of the orbital and spin angular momenta, compounded in a definite way; and $m$, which can only have the value $+\frac{1}{2}$ or $-\frac{1}{2}$, represents the electron spin. Energy levels are repre-
sented by code symbols which give the principal quantum number ; the letter for the orbital angular momentum, usually as a capital; a subscript which gives the value of $j$; and a superscript representing the maximum multiplicity of the term. Thus, $2^{2} \mathrm{~S}_{\frac{1}{2}}$ means $n=2, l=0$, $j=\frac{1}{2}$, and that the term is a doublet; similarly, $2^{2} \mathrm{P}_{\text {}}$ means $n=2, l=1, j=\frac{1}{2}$, and a doublet.

The full multiplicity of a level is only revealed as a rule in the presence of a strong electric or magnetic field; in the ordinary way, two or more levels may coalesce, when they are said to be degenerate.

Fig. 3 shows the pattern of the lower energy levels of the hydrogen atom, from which components of the $\mathrm{H}_{\alpha}$ line could arise. According to the Dirac theory of the electron, the $2^{2} \mathrm{~S}_{\frac{1}{4}}$ and $2^{2} \mathrm{P}_{\frac{1}{2}}$ should be degenerate-that is, coincident-, and there should be only five components. If, however, the self-energy effects operate to raise the $2^{2} \mathrm{~S}_{\frac{1}{2}}$ level, there should be seven components. Since the theory can predict the probability of each transition, it also enables the intensity of each component to be forecast; and (though this is one of the most difficult things of all to verify experimentally) there should be differences in intensity as well as in wavelength and number present. (All S levels are affected; $2^{2} \mathrm{~S}_{\ddagger}$ considerably more than $3^{2} S_{\frac{1}{2}}$.)

This article has really done little more than state the problem. If self-energy effects operate, then the $2^{2} \mathrm{~S}_{\frac{1}{2}}$ and $2^{2} \mathrm{P}_{\frac{1}{2}}$ levels are distinct, the former lying about 0.033 $\mathrm{cm}^{-1}$ above the latter. The direct attack on this very significant little difference, made with all the resources of radio-frequency technique by Lamb and Retherford, will be described next time.

## the twistor-a new magnetic memory device

A new memory device has emerged from exploratory work by A. H. Bobeck at Bell Telephone Laboratories. This device, which has been named the 'Twistor', is expected to make possible memory systems which are simpler to fabricate and more economical to manufacture than existing units.

The new device gets its name from a characteristic of wire made of magnetic material. Torsion applied to such a wire shifts the preferred direction of magnetization from a longitudinal to a helical path. The helical path has both longitudinal and circular components, and the coincidence of a circular and longitudinal magnetic field can thus be used to insert information into the wire.

In practice, the circular magnetic field is provided by a current pulse through the magnetic wire, and the longitudinal field by a current pulse through a copper wire coiled round the magnetic wire. Storing a binary digit requires two coincident current pulses. Readout is accomplished by passing a large current through the copper-wire coil in the reverse direction, a readout signal being taken from the magnetic wire. Because the lines of magnetic flux along the helical path encircle the magnetic conductor many times, an appreciable output signal is obtained.

Investigations are now under way to determine optimum size and composition for the magnetic wires. It appears that a conductor plated with magnetic material may have some advantages. Diameters as small as one-thousandth of an inch appear to be feasible. At least 10 bits per inch may then be stored without adverse interaction.

In conventional magnetic-core memory devices, conductors must be threaded through the cores to make up a suitable matrix. When a ferrite sheet is employed, either a threading or a plating operation

An experimental magnetic memory array which has been set up at Bell Telephone Laboratories to evaluate the 'Twistor' device. In this experimental set-up, the longitudinal magnetic field for the magnetic wires is provided by small solenoids wound around glass tubes. Such an arrangement facilitates the testing of various magnetic wires
is necessary to locate the conductors suitably. However, with the 'Twistor', the ferrite material is completely eliminated and no threading or plating is necessary. Speed of operation and output of the 'Twistor' are comparable to ferrite memory systems.

It is thought that the drive circuits for a 'Twistor' array can be readily transistorized. Thus, a memory system using the 'Twistor' concept will retain all the advantages of ferrite core or sheet systems, and will be much simpler and more economical to fabricate.


# THE REFLEX-MONITOR SYSTEM 

By D. J. R. Martin, B.Sc., A.Inst.P.*


#### Abstract

summary. The cascade-balance principle, described in Part 1, is now revised and embodied in a direct-coupled amplifier of the type using overall drift-correction. Contrary to normal practice, the correcting amplifier, or monitor, is not inherently drift-free but is itself direct-coupled and is a replica of the first stage of the main amplifier; it corrects alternately its own drift and the drift of the main amplifier. The residual effects of supply-voltage and temperature fuctuations are balanced between the two amplifers, which are effectively in cascade during the overall-correction phase.

Whereas the simple cascade-balance system is best suited to amplifiers with a single-ended input, this later development automatically provides for a differential input, with a very high rejection factor against in-phase components. Apart from certain incidental advantages the performance capabilities are similar, an overall zero-stability of $100 \mu \mathrm{~V}$ being readily obtained without recourse to stabilized heater-supplies. $\dagger$


It will be recalled that the straightforward cascadebalance system, described in Part 1, essentially comprises a two-stage direct-coupled amplifier in which drift correction is applied to the first stage only. The drift in that stage is thereby reduced to a level which is comparable in its effect, but opposite in sense, to that of the second stage, and balancing becomes possible. The method of drift correction employed-the Owen-Prinz method-necessitates the duplication of the first stage if bandwidth is to be preserved; the complete amplifier therefore contains three individual amplifying stages which must be identical if the full benefits of the system are to be obtained.
Against the major advantages of high stability and wide frequency response, the possible drawbacks to the system seem to be as follows:
(1) it involves moving parts;
(2) the primary balance is a double one, somewhat complicating initial installation;
(3) the first and second stages must be similar in design, possibly restricting the scope of the system;

[^4]

Fig. 1. The cascade-balance system
(4) the output may contain a small square-wave component (up to $50 \mu \mathrm{~V}$ ) at the switching frequency, as the result of a residual unbalance between the input stages;
(5) if a differential input is required the switching tends to become cumbersome.
The first of these is generally accepted as being unavoidable where maximum stability is required. The others have been eliminated by applying the basic cascade-balance principle to an entirely new form of drift-corrected amplifier, which it is the purpose of this article to describe.

## The Reflex-Monitor System

The simple cascade-balance amplifier is illustrated in Fig. 1, which is reproduced from Fig. 2 of Part 1. A, B and C are the three identical stages of gain $\mu$. A and B serve as the first amplifying stage alternately, with a sufficient overlap to ensure continuity of the signal channel. While out of service, each of these stages is drift-corrected by the Owen-Prinz method, which reduces the drift by a factor $(\mu+1)$. Referred to the input of the amplifier, the residual drift in the first stage is comparable to the drift introduced by the second stage, and components attributable to common disturbances may be balanced.

The essential difference in the new system (illustrated in Fig. 2) is that the twin input stages are not operated on a time-shared basis. Instead, one stage (A) is permanently allocated to the signal channel, which is now never diverted. The other (B) serves as a monitor, and alternates between two conditions: in the first of these, which may be termed the 'self-correcting' condition, the stage is isolated from the rest of the amplifier and its drift checked and corrected by the Owen-Prinz capacitorstorage method; in the other, the 'monitoring' condition,


Fig. 2. The reflex-monitor system
it is used to check and correct the drift in the main amplifier, again with the use of a storage capacitor.

During the monitoring condition, the main amplifier and the monitor stage are connected in cascade as far as drift considerations are concerned; the cascade-balance principle applies, not between successive stages in the amplifier, as in the original system, but between the entire main amplifier and the monitor stage. In the main amplifier it is the first stage only which is important from considerations of drift, and it is this stage only which need be identical to the monitor stage. Whatever form the rest of the amplifier may take, the additional drift introduced by it will be small by comparison and easily taken up in the balancing adjustment.

It will be seen that since bandwidth is not a prior consideration in the monitor stage there is no need for further duplication of this part, even though the Owen-Prinz method is applied to it. The switching is accordingly simplified, and the double balance of the original system is eliminated; there is also no question of a spurious square-wave output resulting from mismatched zero levels.

The correct sense relationships of the system require that the input signal as applied to the monitor stage shall be reversed in polarity with respect to that applied to the main amplifier. To achieve this without destroying the essential similarity of the input stages, a differential input is necessary in each stage; by simple transposition of the input connections, the necessary phase-reversal is effected. The entire amplifier is then differential by nature, though either input terminal may, of course, be earthed to suit single-sided input signals.

As shown in Fig. 2, each input stage has yet a third input terminal. In the case of the monitor stage, the storage capacitor for self-correction by the Owen-Prinz method is connected to this terminal; during the monitoring phase, a small fraction of the amplifier output is also applied here in such a sense and so adjusted that when the amplifier is operating correctly without introducing any drift the signal input to the monitor stage is exactly cancelled. The third input terminal of the main input stage is used for the injection of the correcting potential from the monitor.

## The Individual Stages

## Requirements

As in the case of the simple cascade-balance system, the design of the similar stages has to fulfil certain
conditions. The present requirements are as follows:
(1) the design must include three independent input terminals; two of these must provide equal and opposite sensitivities, forming a normal differential pair, while the third must provide similar (though not necessarily equal) sensitivity with a phase reversal to the output terminal of the stage;
(2) the stage gain should be high (preferably well over 100);
(3) the output-voltage swing must embrace earth potential; this requires potentiometer coupling from the anode circuit and the use of a negative supply;
(4) the current drawn by the third input terminal should be low (not greater than about $10^{-9} \mathrm{~A}$ ), as a correcting potential is applied at this point on a capacitor.
It will be noted that size of possible output-voltage swing is not a consideration in this case, as the design is not required to serve in the output-stage position. The remainder of the amplifier, in fact, will normally be of conventional single-sided direct-coupled form; it will most satisfactorily consist of a single stage.

## The Basic Five-Triode Stage

The basic circuit which has been developed to meet the requirements of the triple-input stages is shown in Fig. 3; input terminals 1 and 2 are used for the input signal, and terminal 3 for drift-correction and sample voltages.

The circuit is essentially that of a cascode amplifier with the lower triode triplicated. Its operation may be analysed by first considering the cathodes of $V_{1}$ and $V_{2}$ to be earthed. In this condition $V_{2}$ and $V_{3}$ are each shunted by the anode impedance of the other; since, however, the lower valve in a cascoded pair works into a low impedance (the cathode impedance of the upper valve) the mutual shunting effect of $V_{2}$ and $V_{3}$ is negligible, and the normal cascode gain is realized from the grid of each. The gain from the grid of $V_{1}$ is potentially much higher, but may be made to correspond to the cascode gain by making $R_{1}$ equal to the anode impedance of $\mathrm{V}_{3}$. If, now, the cathode coupling between $V_{1}$ and $V_{2}$ is restored, the signals on their respective grids are transmitted with very little distinction, partly through $V_{1}$ to the grid of $V_{4}$ and partly by cascode action through $\mathrm{V}_{2}$. At the same time the value of $R_{1}$

Fig. 3. Basic five-triode stage



Fig. 4. Five-triode stage in practical form. All resistors are high-stability, 5\% tolerance
becomes far less critical; in fact, a satisfactory match of the gains from the grids of $V_{1}$ and $V_{2}$ may be obtained even if $R_{1}$ is omitted, in which case the grid of $V_{4}$ is supplied from a steady potential and the action is cascode throughout. Omission of $R_{1}$ does, however, halve the stage gain and its presence provides a simple means of obtaining extremely high rejection factors against inphase components.

## The Five-Triode Stage in Practical Form

In practice, control of rejection factor by direct variation of $R_{1}$ is unsatisfactory as it disturbs the standing potentials in the circuit. Moreover, with the low value of $R_{1}$ that is normally required, the resulting potential drop would be inadequate for the proper operation of $\mathrm{V}_{4}$.

These disadvantages have been overcome in the final practical form of the circuit, shown in Fig. 4. $R_{1}$ itself is given a fixed value, equal to the average anode resistance encountered in $V_{3}$. An intermediate h.t. supply is provided for $V_{1}$, of such voltage that a satisfactory standing potential results at the grid of $\mathrm{V}_{4}$. Resistors $R_{6}$ and $R_{7}$ are introduced, $R_{6}$ being made equal to $R_{1}$ and the value of $R_{7}$ so chosen that the potential at the junction of $R_{6}$ and $R_{7}$ is approximately equal to the anode potentials of $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$; this point is connected to the slider of potentiometer $R V_{1}$, between the anodes of $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$. When the slider of $R V_{1}$ is at one extreme of its travel, $R_{6}$ shunts $R_{1}$ and thus reduces the gain of $\mathrm{V}_{1}$; at the other, $R_{6}$ shunts $\mathrm{V}_{3}$ and thus increases the gain of $V_{4}$ for signals applied to its grid. A wide range of control is thus obtained without seriously disturbing the standing potentials in the circuit.

A further addition to the basic circuit is resistor $R_{8}$, which has been inserted in the cathode return of $V_{3}$. This resistor is small enough in value not to interfere with the operation of the stage by itself, but provides a means of injecting zero-control and negative-feedback voltages into the stage.

## The Second Stage

The circuit which has been adopted for the remainder of the main amplifier is shown in Fig. 5 and comprises a
single pentode stage with a cathode-follower output. The design need not be rigidly followed; for instance, the pentode may be operated at a much lower anode current and a further cathode-follower interposed, in the manner of the cascade-balance amplifier described in Partl.

## Gain and Zero Controls and Associated Circuits

The method of overall drift-correction used involves a comparison between the input signal and a certain fraction, or 'sample', of the output signal. This sample must bear a constant relation to the input signal when the amplifier is operating correctly without introducing drift. It follows that any form of gain control used must not upset this relationship; in other words, if the gain is variable the sample cannot be a fixed fraction of the output signal but must vary with respect to it in an inverse manner to the gain. This condition is simply met by using a negative-feedback control of gain and deriving the sample voltage from the feedback circuit.

The method is shown in Fig. 6, where $R V_{2}$ is the gain control. The minimum gain is determined by the size of the feedback resistor, $R_{13}$, which is chosen to set this value at about 700 ; the maximum is the full gain of the amplifier, about 20,000 .

At low gain settings (i.e., for high degrees of feedback) the voltage at the slider of $R V_{2}$ is substantially independent of the setting of $R V_{2}$, for this is the point from which the feedback factor is invariable. The sample voltage may therefore be derived from this point, using a similar divider chain to that supplying the feedback voltage to the first stage. In Fig. 6, $R_{14}$ and $R_{15}$ form such a chain, corresponding to the feedback path formed by $R_{13}$ and $R_{8}$ (Fig. 4). Potentiometer $R V_{3}$ has been included to provide differential adjustment, allowing for slight variations in component values and possible mismatch between the monitor and main input stages.

If the full range of the gain control is to be used, this method of deriving the sample voltage must be amended, as a closer analysis shows a discrepancy which becomes more serious as the gain setting is increased. This discrepancy is a constant fraction of the output signal, equal to $1 / \mu$ where $\mu$ is the full gain of the amplifier referred to the correction grid. It may be exactly cancelled for all settings of the gain control by augmenting the sample voltage by the same constant fraction $I / \mu$ of the output voltage. An additional resistor for this purpose is shown in Fig. 6 as $R_{16}$; the value given is correct for the amplifier exactly as described, but may need revision if the design is varied in any way.

Reference back to Fig. 4 will show that a certain part of the main signal channel is inevitably excluded from the feedback loop, for the gain is stabilized with respect to the correction input, corresponding to the point in the monitor stage to which the sample voltage is applied. In practice, the overall gain of the signal channel will not vary by more than $1 \%$ provided that h.t. variations to the input stages are confined within about $4 \%$. Heater-voltage changes and changes in emission of the valves have negligible effect on gain, since the driftcorrection processes tend to stabilize the anode currents of the valves and thus effectively the slopes. (It should be understood that the drift correction, unlike the negative feedback, includes the entire amplifier within its scope.)


Fig. 5. Circuit of second stage. All resistors are $10 \%$ tolerance

## Zero Control

In the simple cascade-balance system the output zero-level is controlled in the second stage. In the present system the second stage is included in the correction loop; a control in that position would be insufficiently sensitive, and could not prevent overloading of the second stage due to unsuitable zero-levels in the first.

The zero control must therefore operate in either the signal input stage or the monitor stage, or else in both together by differential action. There is very little to choose between these possibilities; but the monitor stage offers a very convenient point for zero control, corresponding to the feedback point in the main amplifier. As shown in Fig. 6, therefore, the cathode resistor of $\mathrm{V}_{3}$ in the monitor stage has been shunted by a 10,000 -ohm potentiometer, $R V_{4}$, the slider of which passes a bleed current from the positive h.t. supply; a small d.c. is injected into the stage, depending on the setting of the control. To balance the stages at about the central position of this control, a bleed current of about half the magnitude is passed through the corresponding cathode resistor in the main amplifier.

## The Automatic Switching and Associated Circuits

The choice of frequency for the automatic switching operation is governed by the same considerations as given in Part l, and a frequency of $5 \mathrm{c} / \mathrm{s}$ is again adopted.

The total switching capacity required is the same as in the first system described, but all the contact actions are now associated with one stage, and the question of overlap does not arise. The contacts may therefore all be carried on a single relay. The contact sets total four in number and are all of the break-before-make changeover type; in Figs. 2 and 7 they have been identified by reference numbers corresponding to those of the associated terminals of the monitor stage.

Sequence of contact actions within the group is again important; the exact requirements in this respect are as follows:
(1) no contact must make in either condition (i.e., self-correct or monitor) while any contact remains closed in the other condition;
(2) contact $\mathrm{L}_{4}$ must be the last to make and the first to break in the self-correcting condition;
(3) contact $\mathrm{L}_{4}$ must also be the last to make and the first to break in the monitoring condition.
Contacts $L_{1} ; L_{2}$ and $L_{3}$ should be made to operate as near simultaneously as can be judged. In the detailed circuit diagram of the switching circuit, given in Fig. 7, the storage capacitor $C_{2}$ is shown permanently connected
to the sample circuit, which is consequently shortcircuited during the self-correcting phase; this avoids open-circuiting the correction grid in the change-over process.
The circuit of the multivibrator used for driving the relay is given in Fig. 8.

## Facilities for Static Tests and Adjustment

It is helpful during the preliminary checks of the amplifier, and also in any subsequent servicing which may be necessary, if the automatic switching operations may be suspended while particular parts and aspects of the system are examined. The arrangements made for this facility are included in Fig. 7.
Switch $S_{1}$, which is double-pole, prevents the relay from being energized, by short-circuiting its coil; in addition, it provides a leak path to $C_{1}$, causing that capacitor to charge and stay charged to the output potential of the monitor stage in the self-correcting condition. It thus passes on a correction voltage derived entirely from the monitor in its self-correcting condition, without reference to the signal and sample voltages. The cascade-balance action is not thereby affected; but the overall correction feature is suspended, with the result that the effects of any residual unbalance are magnified a hundred times or so. The final adjustments may be made with the amplifier in this condition, and a most accurate estimate of the overall stability may also be obtained.

The effect of manually closing the relay while $S_{1}$ is operated may now be noted: the monitor stage adopts the monitoring condition, but the 1-megohm leak $R_{19}$ is still in circuit; any a.c. component of the signal appearing at the output of the monitor stage, such as might result from an incorrect sample-voltage setting, would be observed on an oscilloscope applied to the test terminal. The relay should not be held closed for more than a second or so, since in this condition there is no means of maintaining the proper correcting potential on $C_{2}$. Switch $S_{2}$ removes this limitation by establishing a d.c. path through the 1-megohm resistors $R_{19}$ and $R_{20}$ to the output terminal of the monitor stage; when this switch is operated with $S_{1}$ the relay may be held closed indefinitely


Fig. 6. Inter-stage circuit showing gain control. Resistors $R_{13}, R_{14}$ and $R_{15}$ are high-stability, $5 \%$ tolerance, and all potentiometers are wire-wound


Fig. 7. Inter-stage circuit showing switching arrangements. $C_{1}$ and $C_{2}$ are $8-\mu F$ paper; the relay $L$ is type 3000, 4-pole change-over with platinum contacts and a 6500- $\Omega$ coil; $S_{1}$ and $S_{2}$ are respectively d.p.c.o. and s.p.c.o. toggle switches
while the behaviour of the monitor stage with a.c. signals is examined.

Figs. 6 and 7 are complementary and between them show in full the inter-stage connections.

## Power Supplies

The total power-supply requirements of the amplifier as described in this article are as follows:
(a) heater supplies
(b) +300 volts d.c. at 14 mA (stage 2 and multivibrator)
(c) -300 volts d.c. at 11 mA (stage 2 and multivibrator)
(d) +250 volts d.c. at 2 mA (input stages and zero control)
(e) -250 volts d.c. at $1 \frac{1}{2} \mathrm{~mA}$ (input stages)
(f) $\quad+85$ volts d.c. at $1 \frac{1}{2} \mathrm{~mA}$ (input stages and stage 2)

For the heater supplies, raw a.c. will normally be suitable and no stabilization is necessary. But, if wide supply-voltage changes are to be tolerated, the balancing technique described in a previous article* must be used. In Part 1 this principle was extended to a three-stage balance but, in the present system, the requirement reduces to a single net balance between the main-input and monitor stages. Control of each stage for supply-

## *See Part 1, reference 7.

Fig. 8. Multivibrator for driving relay

voltage sensitivity is effected through $\mathrm{V}_{3}$ and $\mathrm{V}_{4}$ in conjunction, these valves being paired in one envelope (if a double-triode with a tapped heater were used, $\mathrm{V}_{3}$ alone could serve as the control).

Fig. 9 shows the balancing circuit in the form used. As in the cascade-balance amplifier, certain valves are run with reduced heater-voltage to minimize grid current; the remaining heaters are supplied separately at their rated voltages.

The 300 -volt supplies are not subject to any critical requirements of stability or smoothing, but output capacitors of $100 \mu \mathrm{~F}$ are recommended to minimize common-impedance coupling between the multivibrator and signal circuits.

The 250 -volt and 85 -volt supplies must satisfy certain stringent requirements of filtering as a precaution against rapid mains-voltage fluctuations, which might otherwise defeat the relatively slow drift-correction processes. Steps must also be taken to avoid or counteract the small but significant changes in amplifier gain which can result from wide variations in these supply-voltages. Means have been developed for achieving these ends without resorting to stabilization, but these will not be discussed as it will probably be considered that stabilization is more straightforward, even if more costly. The 85 -volt supply is readily obtained using a single neon tube, such as an 85Al; it should be bypassed by a large capacitor. The stabilization of the 250 -volt supplies should be effective in reducing sudden small changes by a factor of at least 200, the criterion being that the voltage should not change at a faster rate than about $50 \mathrm{mV} / \mathrm{sec}$ and or instantaneously by more than 10 mV . Slow variations need only be reduced by a factor of about 5 .

## General

## Constructional Notes

Apart from the h.t. and $6 \cdot 3$-volt supplies, the circuit of a final design may be built up from Figs. 4 to 9 . In the practical layout of such an amplifier, care should be taken to position the input circuits as far as possible from the multivibrator valve, which may need to be screened. Usual precautions against hum pick-up in the input stages are necessary.

Adjustment of the relay contacts should be carried out before these are wired into the circuit; the contact
sequences may then be checked electrically. It should be noted that in Fig. 7 the contacts are shown in the energized condition of the relay.

## Tests and Adjustments

If resistors $R_{29}$ and $R_{30}$ have been made adjustable, they should be set with the heaters only switched on. The correct adjustments give voltage nulls between the ends of potentiometer $R V_{5}$ and its slider, which should be centrally set.

When the h.t. supplies are first applied to the complete amplifier switch $S_{1}$ should be in the test position, so that the relay remains unenergized and capacitor $C_{1}$ is allowed to adopt the same steady potential as $C_{2}$; switch $S_{2}$ should be in the normal position. In this condition the amplifier functions normally with d.c. and a.c. signals and the gain and zero controls are operative; as already explained, the cascade-balance principle is effective but the overall drift-correction process is suspended. Potentiometer $R V_{1}$ in the input stage should be adjusted for zero transmission of a common-mode a.c. signal applied to the input terminals. Switch $S_{2}$ should then be operated and the relay held closed while the signal at the test terminal is observed on an oscilloscope; with the common-mode a.c. signal still applied to the input terminals, potentiometer $R V_{1}$ in the monitor stage should likewise be adjusted for zero transmission. A differential signal should then be applied to the input terminals and potentiometer $R V_{3}$ adjusted for a null in the signal observed on the oscilloscope at the test terminal, with the relay still closed. This adjustment should hold for all settings of the gain control: any variation indicates that the value of $R_{16}$ requires modification to suit the particular amplifier. During these tests, care should be taken that the amplifier is not overloaded, or misleading results will be obtained.

It remains to balance the amplifier for the effects of mains-voltage changes: for this, the relay is released and $S_{2}$ returned to normal; potentiometer $R V_{5}$ is then adjusted so that changes of $\pm 10 \%$ in mains voltage, simulated by means of a variable transformer, have least effect on the d.c. output indication.

Switch $S_{1}$ should now be returned to normal, allowing the overall drift-correction process to function. The immediate result will be a reduction of any zero-offset by a factor of a hundred or so, while the transmission of the amplifier to a.c. and d.c. signals will not be affected. If the d.c. output level should wander in the presence of a large a.c. signal it may be taken that the sample-voltage adjustment (of potentiometer $R V_{3}$ ) is incorrect.

Various fault conditions can give rise to spurious output signals at switching frequency. A 'blunt' sawtooth waveform, or 'wobble', devoid of high-frequency components, may be caused by interference from the multivibrator through the h.t. supplies or by a microphonic valve responding to mechanical vibration from the relay. A 'sharp' sawtooth may be due to a leaky storage capacitor or excessive grid-current in $\mathrm{V}_{3}$ in either input stage, or abnormally large and rapid changes in mains voltage may be occurring. Sharp 'spikes' in the output indicate direct pick-up from the multivibrator if they persist with $S_{1}$ in the test position; otherwise, a momentary parasitic oscillation is probably occurring during the change-over operation of the monitor; such an effect may usually be cured by arranging

Fig. 9. Heater-supply arrangements for input valves. $R_{29}$ and $R_{30}$ are wire-wound $\frac{1}{2} A$ and can be of the adjustable type; $R V_{5}$ is wire-wound and a Gardners type L. 470 will serve for the mains transformer $T R$

one of contacts $L_{1}$ and $L_{2}$ to make in the monitoring condition slightly in advance of the other. Wider peaks signify that the inevitable transients in the monitor stage are reaching the signal channel through a commonimpedance coupling. A square-wave output at switching frequency may result from too high a source resistance or excessive grid current in the monitor stage.

## Performance

The following characteristics of the reflex-monitor amplifier described are maintained against slow variations in heater-supply voltage of $10 \%$, step changes of $0.5 \%$, and all normal temperature and long-term effects.

Gain: approximately 700 to 20,000 (continuously variable)
Zsco-slability: better than $100 \mu \mathrm{~V}$ referred to the input
Effective input resistance: greater than 1 megohm
Rejiclion factor against common-mode signals: not less than 10,000
*Maximum undistorted output-voltage swing: -30 to +70 volts (unloaded)
*Stability of gain: 1 \%
*Frequency response: level within $\pm 1 \%$ from $0 \mathrm{c} / \mathrm{s}$ to $25 \mathrm{kc} / \mathrm{s}$ (with low source-impedance)
*Oulput resistance: about 40 ohms

* at a gain selting of 1,000

For rated performance the following recommendations should be observed.
Maximum signal-source resistance: 100,000 ohms
Maximum source-to-earth resistance: 1 megohm
Maximum common-mode input voltage: 5 volts (d.c. or peak a.c.)
Warming-up time (with switch $S_{1}$ in test position): 10 minutes

## Possible Improvements in Performance

The quoted figure for zero-stability formed part of a preconceived specification upon which the typical design was based, and should not be regarded as the best obtainable from the system. Provided that a reduced source impedance is used, a direct improvement in stability may be obtained by raising the gain of the input stages; if necessary, these stages may be replaced by suitably designed two-stage sections, due consideration being given to the sensing requirements.
To give useful effect to an enhanced stability of mean zero-level, the residual variations at switching frequency would probably need comparable reduction. Short of actual fault conditions, the causes of these variations are twofold: first, the potential on the storage capacitors tends to alter between corresponding correcting opera-
tions; secondly, supply voltages may change too rapidly for the correction processes to give adequate reduction. Each of these conditions will introduce a spurious voltage of sawtooth waveform into the output of the amplifier. Their effects may together be reduced to any desired extent by suitably increasing the switching frequency. Otherwise they may be treated separately, as will be briefly suggested.

Change of potential on the storage capacitors is caused mainly by grid current and leakage in the valves; it may be lessened by using larger capacitances or electrometertype valves. With certain types of capacitor internal leakage may contribute to the effect; this could be minimized by introducing a series bias to relieve each capacitor of most of its standing potential.
The effects of rapid mains-voltage fluctuations felt through the l.t. supplies could be reduced by employing a simple voltage stabilizer; this need only be a simple constant-voltage transformer with a stabilization ratio of $10: 1$ or less, and frequency coefficient of voltage would be inconsequential. Otherwise the basic five-triode circuit of the input stages could be extended by the addition of yet a sixth triode. This would be cathodecoupled to $\mathrm{V}_{3}$ in the same way that $\mathrm{V}_{1}$ is coupled to $\mathrm{V}_{2}$ and its anode would be connected to the anode of $\mathrm{V}_{1}$. It would then be possible to balance each stage inherently for the effects of heater-voltage changes, and the time delay associated with the cascade-balance feature would be avoided.

## Radio-Frequency Interference

During the later stages of the tests on the amplifiers described in these articles a marked deterioration in the zero stability and noise level was noticed between certain hours of the day. This trouble was traced to interference from the B.B.C. and I.T.A. television transmitters situated a few miles away; the r.f. signals were being picked up in the amplifier circuits and signal sources and in some manner were being partially detected. The zero variations noticed were caused by the varying d.c. components which are present in the modulation envelopes of television signals and which set the mean brightness levels in the received pictures; the prominent frame-frequency components caused a $50-\mathrm{c} / \mathrm{s}$ hum of varying waveform and amplitude.

If such interference is suspected, the simplest check is to connect a pair of headphones across the output terminals of the amplifier: the vision signal would be heard as a rough hum, but the accompanying sound signal would probably give a surer indication.

Similar trouble has been experienced from the regional medium-wave transmitter. In this case the predominant symptom was an unusually high level of high-frequency noise in the amplifier output; this was resolved as a modulated carrier and again could be identified by listening.

The best precaution against such interference is the complete screening of the amplifier and the insertion of filters in all external leads. It has not been found possible to effect a cure with bypass capacitors.

## Conclusion

The reflex-monitor system is recommended for applications requiring high stability with a differential
input. Its main advantages over the conventional parallel-balance amplifier are:
(1) the avoidance of stabilized heater-supplies
(2) an improvement in long-term zero-stability of at least 100 times
(3) superior amplifier characteristics resulting from the application of negative feedback.
If a differential input-circuit is not required the simpler cascade-balance system described in Part 1 might be considered as an alternative; the performance capabilities are similar, but the reflex-monitor system avoids certain disadvantages.

## Acknowledgement

The author wishes to thank the Director and Council of the British Scientific Instrument Research Association for permission to publish these articles.

## CLEANING SEMICONDUCTOR COMPONENTS

A highly-effective continuous water washing system for removing surface contamination from semiconductor components has been adapted from valve-manufacturing techniques by Bell Telephone Laboratories. All water-soluble materials which remain after etching are removed and the effectiveness of the washing procedure is monitored.
When used on transistors, the new system has resulted in significant improvements in breakdown voltage, sharpness of voltage-current characteristics, saturation current, and cmitter reverse impedance.
Distilled water, replaced about once a week, is continuously re-circulated through the cleaning system at about two litres per minute. It first passes through a small de-ionising column which reduces its conductivity to about $0 \cdot 1$ micromho per cm as measured in a conductivity cell. The de-ionized water then rises through a vertical standpipe in which the parts being cleaned are suspended on a stainless steel frame. After flowing over the upper edge of the standpipe, the water passes through a second conductivity cell and thence to a sump for re-circulation.

Carbon dioxide from the air is used as a measuring tool. $\mathrm{CO}_{2}$ is picked up by the water in the washing chamber in sufficient quantity to increase its conductivity from 0.1 micromho per cm in the first cell to 0.15 micromho per cm in the second. Parts are washed until these two readings are obtained from the cells. The thoroughness of washing is readily specified by the conductivity of the effluent and this makes possible a one-hundred per cent inspection of the product.

Inserting transistors into the semiconductor washing system developed at Bell Telephone Laboratories


# Coaxial Transmission Lines 

## EFFEGT OF ELLIPTIGAL INNER CONDUGTOR ON HIGH-FREQUENCY CHARAGTERISTICS

## By S. Mahapatra*

SUMMARY. Approximate calculations are made for the distributed constants ( $R, L, G, C$ ) of a coaxial transmission line with the inner conductor of elliptical cross-section. The method of conformal transformation is used to find the capacitance on the assumption that the focal distance of the ellipse from the centre is small compared to the radius of the outer cylinder. The resistance of the inner conductor is computed from the electrostatic charge distribution. The minimum attenuation condition for a given eccentricity of the ellipse is specified.

Thhe problem of the performance of a coaxial line with an elliptical inner conductor arose out of the design of the dee-stem transmission line of the cyclotron at the Institute of Nuclear Physics, Calcutta. The peculiar geometry of the dee-chamber and the link connecting the manifold restricts the space in the vertical axis. Unless the dees are made demountable, which is not a convenient solution, assembly considerations lead to the construction of dee-stem transmission lines with very narrow inner conductors. A circular coaxial line with a ratio of the radii of the outer to the inner conductor exceeding five is not desirable because of the high attenuation involved. To satisfy the optimum condition in the circular case, the diameter of the outer conductors within the manifold may be decreased, but this considerably diminishes the Q-value of the line and is not a convenient solution. The alternative is to use an oval or elliptical inner conductor and the present article describes work on these lines. The theoretical calculations show that whenever space is restricted along one axis so that, for a circular coaxial, we cannot help making the outer-to-inner diameter ratio greater than five, it is always possible to, construct a transmission line with elliptical conductors of proper dimension so as to have less attenuation.

In this connection, we may refer to the case of the $225-\mathrm{cm}$ cyclotron at the Nobel Institute, Stockholm, where the dee-neck was made oval11. As the dissipation in the acceleration-chamber and the link-part was extremely high, the elliptical cross-section of the neck was found more suitable to keep the dissipation within reasonable limits ${ }^{12}$. This is quite in agreement with the conclusions derived in this paper. We have shown that the ratio of resistance of an elliptical conductor to that of a circular one with diameter equal to the minor axis of the ellipse sharply decreases with increase in major axis. Hence, where the dissipation is inordinately high, and the space is restricted along one axis, the dissipation in this part may be reduced by more than $50 \%$ by using an elliptical conductor.

In the case of coaxial lines with good conductors the

[^5]assumption of TEM wave is quite justified ${ }^{\mathbf{1}, 2}$ and this assumption has been employed to determine the distributed constants of a line with an elliptical inner conductor. In the propagation of a TEM wave in a transmission line, the transverse electric field configuration is identical with the static field distribution ${ }^{3}$. The conformal transformation ${ }^{4,5,6}$ is therefore employed to find the distributed capacitance $C$ per unit length of the line with the assumption that the radius of the outer shield is much greater than the focal distance of the cross-sectional ellipse of the inner conductor from the centre. The characteristic impedance $Z_{0}$, and the distributed inductance $L$ per unit length of the line are then readily obtained from the well-known relations for low-loss lines,
\[

$$
\begin{array}{llllll}
Z_{0}=\sqrt{L / C} \text { ohms } & . . & . & . . & . . & (1)  \tag{1}\\
v_{p}=1 / \sqrt{L C} \text { metres/sec. } & \ldots & \ldots & \ldots & (2)
\end{array}
$$
\]

where $v_{p}$ is the phase velocity and is equal to $3 \times 10^{8}$ metres per second in vacuum (or air).

Fig. 1. Cross-section of coaxial line with elliptical inner conductor. The dashed curve gives the confocal ellipse having a semi-major axis equal to the inner radius of the circular shield


To calculate the resistance and attenuation of the line, the distribution of current density must be known ${ }^{7}$. At high frequencies, skin effect predominates ; consequently current density becomes a surface phenomenon rather than a volume phenomenon. Calculations being restricted to the case where both the radius of curvature and the thickness of the conductors are very great with respect to the depth of penetration, we are led to the conclusions: (l) that the current distribution must tend to that which produces no internal magnetic field, (2) that the magnetic-field lines in the space between the conductors coincide with the electric equipotential lines and the magnetic equipotential lines with the electric field lines ${ }^{8,9}$. Consequently, the distribution of the current density on the surface of the conductors corresponds precisely to the distribution of electrostatic charge density. The latter is readily obtained from the knowledge of conformal transformation.

## Characteristic Impedance

The transformation

$$
\begin{equation*}
w=u+j v=A \log _{e}\left(\frac{z}{k}+\sqrt{\left(\frac{z}{k}\right)^{2}-1}\right) \ldots \tag{3}
\end{equation*}
$$

$$
z=x+j y
$$

gives a set of confocal ellipses for $u=$ constant as, on eliminating $v$, we get

$$
\begin{equation*}
\frac{x^{2}}{k^{2} \cosh ^{2} u / A}+\frac{y^{2}}{k^{2} \sinh ^{2} u / A}=1 \tag{4}
\end{equation*}
$$

If $u=$ constant gives equipotential lines, then corresponding to the ellipse in the $z$-plane of semi-major axis $a$ and semi-minor axis $b$ (Fig. 1) we get

$$
\begin{align*}
a & =k \cosh u / A \\
b & =k \sinh u / A  \tag{5}\\
\text { and } \quad k & =\sqrt{a^{2}-b^{2}}
\end{align*}
$$

It also follows from Equ. (3) that if $(z / k)^{2} \gg 1$, the transformation becomes very nearly equal to the form $w=A \log _{e} z$, which transforms $u=$ constant to circles in the $z$-plane. So for the cylindrical shield of inner radius $r$, if $(r / k)^{2} \gg 1$, the ellipse will almost completely coalesce into the circular cylinder.

For simplicity, and with no loss of generality, we may put $A=1$ and get the capacitance per unit length of the line as

$$
C=\frac{\oint \epsilon d v}{u_{\mathrm{ABC}}-u_{\mathrm{DEG}}}=\frac{2 \pi \epsilon}{\cosh ^{-1} r / k-\cosh ^{-1} a / k} \begin{align*}
& \text { farads } / \text { metre }
\end{align*}
$$



Fig. 2. The fractional percentage $\Delta r / r \times 100$ versus $r / k$
where the closed integral is performed over the $u=$ constant curve and $\epsilon$ designates the permittivity of the medium. It follows that if we assume $+Q$ charge per unit length of the inner conductor then the constant term $A$ will be $-Q / 2 \pi \epsilon$ so that the transformation of Equ. (3) may now be written as

$$
\begin{equation*}
w=-(Q / 2 \pi \epsilon) \log _{e}\left[z / k+\sqrt{(z / k)^{2}-1}\right] \tag{7}
\end{equation*}
$$

Equation (6), however, gives a slightly lower value as we have equalized the radius $r$ with the semi-major axis of the ellipse and a closer approximation will be obtained by subtracting a value $\Delta r$ from $r$. The fractional variation $\Delta r / r$ has been plotted in Fig. 2 for different values of $r / k$.

If the relative permittivity of the dielectric medium be $\epsilon_{r}$, the capacitance per unit length is then given by the formula

$$
\begin{gather*}
C=55 \cdot 6 \cdot \frac{\epsilon_{r}}{\log _{e} \frac{r+\sqrt{r^{2}-k^{2}}}{a+b}} \mathrm{pF} / \text { metre }  \tag{8}\\
k \text { being equal to } \sqrt{a^{2}-b^{2}}
\end{gather*}
$$

The inductance per unit length and the characteristic impedance from the previous discussion are then given by

$$
\begin{align*}
& L=0 \cdot 2 \log _{e} \frac{r+\sqrt{ } r^{2}-k^{2}}{a+b} \mu \mathrm{H} / \text { metre }  \tag{9}\\
& \mathrm{Z}_{0}=\frac{60}{\sqrt{ } \epsilon_{r}} \log _{e} \frac{r+\sqrt{r^{2}}-k^{2}}{a+b} \mathrm{ohms} \tag{10}
\end{align*}
$$

Equation (10), however, gives a slightly high value for the same reason that we get a slightly low value of capacitance by Equ. (8). It is seen that for $r / k$ greater than three, the error is very small, thus for $r / k=4$, the error is about $1 \%$, and for $r / k=5$, it is only about $0.5 \%$. A plot of characteristic impedance $Z_{0}$ versus $r / k$ is given in Fig. 3, with $b / a=0.5$ and air as the dielectric medium. The continuous line shows the value given by Equ. (10), while the dotted curve gives the value after correction for $r$.

## Calculation of Resistance

It is assumed that the radius of curvature and the thickness of the conductors are much greater (by at least eight times) than the depth of penetration ${ }^{9}$, so that the complex Bessel function calculation may be avoided and the simple knowledge of surface resistivity will enable us to calculate the effective resistance almost precisely.

The surface-charge density on the elliptical conductor is

$$
\begin{equation*}
q=-\epsilon\left|\frac{d w}{d z}\right| \tag{11}
\end{equation*}
$$

where $\quad\left|\frac{d w}{d z}\right|$ is taken on the surface of the conductor.
Hence from Equ. (7), putting $x$ and $y$ in the parametric form $a \cos \phi$ and $b \sin \phi$ respectively, we get

$$
\begin{equation*}
q=\frac{Q}{2 \pi} \cdot \frac{1}{\left(a^{2} \sin ^{2} \phi+b^{2} \cos ^{2} \phi\right)^{\frac{1}{2}}} \tag{12}
\end{equation*}
$$

If we represent the r.m.s. surface-current density by $i_{0}$ and the r.m.s. high-frequency current by $I$ we may


Fig. 3. Characteristic impedance $\left(\boldsymbol{Z}_{0}\right)$ versus $r / k$ as calculated from Equ. (10), for $b / a={ }_{2} 0 \cdot 5$. The dashed curve gives the value after correction for $r$
put, following the discussion at the beginning of the article,

$$
\begin{equation*}
i_{0}=\frac{I}{2 \pi} \cdot \frac{1}{\left(a^{2} \sin ^{2} \phi+b^{2} \cos ^{2} \phi\right)^{\frac{1}{2}}} \tag{13}
\end{equation*}
$$

So the power loss in an elementary strip of unit length and width equal to $\left(a^{2} \sin ^{2} \phi+b^{2} \cos ^{2} \phi\right)^{\frac{1}{2}} d \phi$ is given by,

$$
\begin{equation*}
d W=\frac{I^{2} R_{1}}{4 \pi^{2}} \cdot \frac{d \phi}{\left(a^{2} \sin ^{2} \phi+b^{2} \cos ^{2} \phi\right)^{\frac{1}{2}}} \tag{14}
\end{equation*}
$$

where $R_{1}$ is the surface resistivity and is given by

$$
\begin{equation*}
R_{1}=\sqrt{\frac{\pi f \mu}{\sigma}} \tag{15}
\end{equation*}
$$

$f=$ frequency (cycles/second)
$\mu=$ permeability of the conductor (henrys/metre).
$\sigma=$ conductivity of the conductor (mhos/metre).
Hence total loss per unit length of the inner conductor is,

$$
\begin{align*}
W & =\frac{I^{2} R_{1}}{4 \pi^{2}} \int_{0}^{2 \pi} \frac{d \phi}{\left(a^{2} \sin ^{2} \phi+b^{2} \cos ^{2} \phi\right)^{\frac{1}{2}}} \\
& =\left(I^{2} R_{1} / \pi^{2} a\right) F(e, \pi / 2) \tag{16}
\end{align*}
$$

where $F(e, \pi / 2)=\int_{0}^{\pi / 2} \frac{d \phi}{\sqrt{1-e^{2} \sin ^{2} \phi}}$
stands for the elliptic integral of the first kind, and $e$ is the eccentricity of the ellipse, being equal to $\sqrt{1-(b / a)^{2}}$.

So the effective resistance $R_{e l}$ of the elliptic conductor per unit length is given by

$$
\begin{equation*}
R_{e l}=\frac{W}{I^{2}}=\frac{R_{1}}{\pi^{2} a} \cdot F(e, \pi / 2) \mathrm{ohms} / \text { metre } \tag{17}
\end{equation*}
$$

$F(e, \pi / 2)$ has been plotted ${ }^{10}$ for different values of $b / a$ (Fig. 4).

It is of interest to compare the resistance $R_{c i r}$ of a circular cylinder with equal cross-sectional area. For equal area, the circle will have a radius equal to $a\left(1-e^{2}\right)^{\frac{1}{x}}$. So the ratio of the resistance per unit length of elliptic and circular cylinder is given by,

$$
\begin{equation*}
\frac{R_{e l}}{R_{e i r}}=\frac{2}{\pi} \cdot\left(1-e^{2}\right)^{\frac{1}{4}} \cdot F\left(e, \frac{\pi}{2}\right) \ldots \tag{18}
\end{equation*}
$$

This has been plotted against $b / a$ (Fig. 5). It is seen that the ratio decreases with lesser value of $b / a$ (i.e., greater
value of $e$ ) despite the increasing non-uniformity of current density. This is because, for the same crosssectional area, with greater values of $e$, the ellipse has got a larger perimeter which factor does more than balance the increase in resistance due to non-uniform current density. This is a good illustration showing the high frequency characteristics as a surface phenomenon rather than a volume phenomenon. However, for equal perimeter the ratio

$$
\begin{equation*}
\frac{R_{e l}}{R_{c i r}}=\frac{4}{\pi^{2}} \cdot F(e, \pi / 2) \cdot E(e, \pi / 2) \tag{19}
\end{equation*}
$$

[where $E(e, \pi / 2)=\int_{0}^{\pi / 2} \sqrt{1-\epsilon^{2} \sin ^{2} \phi} \cdot d \phi$ stands for the elliptic integral of the second kind] increases with increase in $e$; i.e., decrease in $b / a$ (Fig. 6).
For all practical purposes, the following simpler formula will give very nearly correct value of resistance up to the value of $e=0.866$ (i.e., $b / a=0.5$ ),

$$
\begin{equation*}
R_{e l}=\frac{R_{1}}{2 \pi a}\left[\left(1-\frac{e^{2}}{2}\right)^{-\frac{1}{2}}+\frac{3}{64} \cdot \frac{e^{4}}{1-e^{2}}\right] \tag{20}
\end{equation*}
$$

Thus, for $b / a 0 \cdot 5$, the value given by Equ. (20) is only about $0.2 \%$ less than the actual value. This formula may be extended to $e=0.94$ (i.e., $b / a \approx 0.34$ ) where the value given by equation (20) is approximately $3 \%$ higher than the actual one.

The resistance per unit length of the transmission line is, therefore,

$$
\begin{equation*}
R=\left(R_{1} / \pi^{2} a\right) F(e, \pi / 2)+R_{2} / 2 \pi r \text { ohms } / \text { metre } \tag{21}
\end{equation*}
$$

where $R_{1}$ and $R_{2}$ are the surface resistivities of the materials of the inner and outer conductors respectively. If the permeability of conductors be taken equal to that of the space we get, $\sigma_{1}$ and $\sigma_{2}$ being the respective conductivity of the centre and outer conductor,

$$
\begin{equation*}
R=\sqrt{\frac{f}{10^{7}}}\left[\frac{2 \times F(e, \pi / 2)}{\pi a \sqrt{\sigma_{1}}}+\frac{1}{r \sqrt{\sigma_{2}}}\right] \text { ohms/metre } \tag{22}
\end{equation*}
$$

For values of $e \leqslant 0.94$, we can utilize Equ. (20) and write,

$$
\begin{align*}
R= & \sqrt{\frac{f}{10^{7}}}\left[\frac { 1 } { a \sqrt { \sigma _ { 1 } } } \left\{\sqrt{\frac{2}{1+(b / a)^{2}}}\right.\right. \\
& \left.\left.+\frac{3}{64}\left(\frac{a}{b}-\frac{b}{a}\right)^{2}\right\}+\frac{1}{r \sqrt{\sigma_{2}}}\right] \text { ohms/metre } \tag{23}
\end{align*}
$$

Fig. 4. $F(e, \pi / 2)$ versus b/a. This also gives the relative value of resistance of elliptical conductor for different values of b/a, when the semi-major axis $a$ is kept constant. The broken line gives the relative resistance (right-hand scale) when the minor axis is kept constant



Fig. 5. The ratio of resistance per unit length of the elliptical conductor to that of the circular one, of equal cross-sectional area, against b/a

## Attenuation Constant $\alpha$

At high frequency, the attenuation constant $\alpha$ is given by,

$$
\begin{equation*}
\alpha=R / 2 Z_{0}+G Z_{0} / 2 \text { nepers } / \text { metre } \tag{24}
\end{equation*}
$$

where $G$ is the shunt conductance per unit length and is, $G=2 \pi f C \tan \delta=3.49 \times 10^{-10}$

$$
\begin{equation*}
\frac{f \epsilon_{r} \tan \delta}{\log _{e}\left(r+\sqrt{r^{2}-k^{2}}\right) /(a+b)} \text { mhos/metre } \tag{25}
\end{equation*}
$$

$\delta$ being the loss angle of the dielectric medium.
So, from Equations (22) and (10) we get,

$$
\begin{align*}
& \alpha= \frac{\sqrt{\frac{f \epsilon_{r}}{10^{7}}}}{}\left[\frac{2 \times F(e, \pi / 2)}{\pi a \sqrt{\sigma_{1}}}+\frac{1}{r \sqrt{\sigma_{2}}}\right] \\
& 120 \log _{e} \frac{r+\sqrt{r^{2}-k^{2}}}{a+b}  \tag{26}\\
&+1 \cdot 05 \times 10^{-8} \sqrt{\epsilon_{r}} f \tan \delta \text { nepers/metre }
\end{align*}
$$

With negligible dielectric loss and $1 \geqslant b / a \geqslant 0.34$, substituting $m, n$ and $\rho$ for $b / a, \sigma_{1} / \sigma_{2}$ and $r / a$ respectively we have, using Equ. (23),

$$
x=\frac{\sqrt{\frac{f \epsilon_{r}}{10^{7} \sigma_{1}}} \cdot \frac{1}{r}\left[\rho \left\{\sqrt{\left.\left.\frac{2}{1+\mathrm{m}^{2}}+\frac{3}{64}\left(\frac{1-m^{2}}{m}\right)^{2}\right\}+\sqrt{n}\right]}\right.\right.}{\left(120 \log _{e} \frac{\rho+\sqrt{\rho^{2}-\left(1-m^{2}\right)}}{1+m}\right)}
$$

nepers/metre

To get the condition for minimum attenuation for a given value of $r$ and $m$, we differentiate Equ. (27) with respect to $\rho$ and the minimum condition is satisfied by the equality

$$
\begin{aligned}
& \log _{e} \frac{\rho+\sqrt{\rho^{2}-\left(1-m^{2}\right)}}{1+m} \\
& =\frac{1}{\sqrt{\rho^{2}-\left(1-m^{2}\right)}}\left[\rho+\frac{\sqrt{n}}{\sqrt{2 /\left(1+m^{2}\right)+3 / 64\left[\left(1-m^{2}\right) / m\right]^{2}}}\right]
\end{aligned}
$$

For the conductors with same material, Table 1 gives the optimum value of $\rho=r / a$ and the corresponding attenuation normalized with respect to the circular coaxial.

The attenuation constant $\alpha$ is plotted in Fig. 7 against $\rho$ for three values of $b / a$, viz., $0.9,0.7$ and 0.5 . The dashed curve corresponding to the circular case ( $b / a=1$ ), is given for reference.

TABLE 1

| $m=b / a$ | $\rho=r / a$ | Normalized $\alpha$ |
| :---: | :---: | :---: |
| 1.0 | 3.59 | 1.000 |
| 0.9 | 3.45 | 1.004 |
| 0.8 | 3.31 | 1.009 |
| 0.7 | 3.16 | 1.015 |
| 0.6 | 3.02 | 1.025 |
| 0.5 | 2.86 | 1.042 |

It follows from a study of the Fig. 7 that the ratio $r / a$ becomes more critical with greater eccentricity of the ellipse, which is not unexpected. Since an elliptical cylinder has a smaller h.f. resistance than a circular cylinder of equal cross-sectional area, it follows that making both the conductors elliptical or oval, where the cross-sectional area is restricted, specially from one axis, may lead to better performance so far as the attenuation is concerned.

## Q of an Elliptical Line

A cyclotron engineer is usually interested in obtaining a high $Q$-value for the line. The $Q$-value of a circular coaxial line having radii of the outer and inner conductors $r_{1}$ and $r_{2}$ respectively, is given by ${ }^{7}$,

$$
Q=\left(2 r_{1} / d\right)\left[\left(\log _{e} r_{2} / r_{1}\right) /\left(1+r_{1} / r_{2}\right)\right]
$$

where $d$ is the depth of penetration, and, in the case of an elliptical inner conductor of semi-major axis $a$ and semi-minor axis $b$, with outer conductor of radius $r_{2}$

$$
Q=\frac{2 a}{d}\left(\log _{e} \frac{r_{2}+\sqrt{r_{2}^{2}-\left(a^{2}-b^{2}\right)}}{a+b}\right) /\left((2 / \pi) F(e, \pi / 2)+a / r_{2}\right)
$$

It follows that with restriction in one axis, the elliptical inner conductor transmission line will provide higher $Q$-values. This occurs specially where the circular coaxial would have to be made with a diameter ratio greater than five, when the $Q$-value obtainable by such lines may be more than $20 \%$ greater than that achieved with circular lines. In such cases, it seems worth while to construct an elliptical conductor. Other cases are conceivable involving similar restrictions where such solutions may be of benefit.

Fig. 6. The ratio of resistance per unit length of the elliptical conductor to that of the circular one, having equal perimeter, versus b/a


## Acknowledgement

The author has pleasure in expressing his deep gratitude to Dr. B. D. Nag Chaudhuri, Director, Institute of Nuclear Physics, Calcutta, for his encouragement in the work.

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Fig. 7. The increase in attenuation in per cent over the minimum of the circular case versus $\rho(=r / a)$ for three values of b/a: 0.9 (curve $I$ ), 0.7 (curve II), 0.5 (curve III). The dashed curve corresponds to the circular case ( $b / a=1$ )

# MATHEMATICAL TOOLS 

By Computer

## Matrices. 1-General Principles

In circuit work we are familiar with the idea that a two-terminal network has an 'impedance' which is usually a complex number. The concept of 'impedance' enables us to determine immediately, under steady-state conditions, the current resulting from the application of a given sine-wave voltage to the network. By means of operational calculus, we can obtain the current when an arbitrary voltage is applied, and we can take full account of transient terms. Without the impedance concept, we should be obliged to solve many twoterminal network problems by means of differential equations in the classical manner, and the physical significance of the results obtained would be much more difficult to appreciate. If, however, we consider a network having more than two terminals, it is no longer possible to sum up the properties of this network by means of a single number, even if this number may be complex. We require several such numbers. We can describe such a network by means of a number of its attributes; for example, input and output admittances, open-circuit and short-circuit impedances, transfer constants, etc. There is a wide choice of possible descriptive parameters of this kind available, and those well skilled in the art are able to use these with some facility and perhaps even to have some mental picture
of the whole whose parts are represented by these parameters. What is really needed, however, is a specification of the network performance by means of the smallest possible number of parameters, each of which has a value determined by the essential behaviour of the network, which remains unchanged if a particular form of this network is replaced by an equivalent circuit. The important facts about a network or any other physical entity are those associated with what it does; the question 'What is this network ?' is usually irrelevant. If we can not only specify network performance by a group of parameters associated with what the network does, but also can apply to these groups of parameters, regarded as single entities, algebraic manipulations analogous to those associated with impedances in two-terminal network theory, an enormous simplification of network theory becomes possible, much as two-terminal network theory is simplified by the impedance concept. Matrices are groups of essential parameters of the type under discussion, and there is a machinery for their algebraic manipulation. Although this machinery is unfamiliar and apparently difficult to the uninitiated, the matrices associated with four-terminal networks are of a particularly simple kind, and the technique for handling
these matrices can be learnt by an engineer in a few hours.

The mathematical machinery of the complex number enabled electricians to think of an a.c. voltage, current or impedance as a single quantity, even though this quantity had real and imaginary parts and the algebra required had the special law that $j^{2}$ must be replaced by -1 in addition to the normal laws of 'real' algebra. At first this machinery, being unfamiliar, appeared to complicate the subject, but in the end it was recognized that the difficulty lay in the subject and not in the machinery. Once the machinery of complex-number theory was understood, the subject of two-terminal network theory became easier to understand; essentially the subject was reduced to the repeated application of a generalized form of Ohm's Law.

The situation is similar with regard to four-terminal network theory and matrices. The essential behaviour of such a network containing linear elements can be expressed by means of four quantities arranged in two rows. Suppose that $V_{1}$ and $I_{1}$ are the input voltage and current (or rather the $p$-world counterparts of these quantities wiht which we have become familiar in recent articles on operational calculus), and that $V_{2}$ and $I_{2}$ are the corresponding output current and voltage, with the sign convention of Fig. 1. In these articles we shall always use that sign convention. It is the most suitable convention for passive networks where no external voltage is applied at the output. $V_{2}$ is then the voltage developed at the output terminals as a result of the application of $V_{1}$, and $V_{2} / I_{2}$ is the impedance of the external circuit connected to the output terminals. With active networks it is more usual to choose $I_{2}$ flowing in the opposite direction, and $V_{2}$ is an externally applied voltage, so that $V_{2} / I_{2}$ is then the output impedance. It will therefore be necessary to consider carefully


Fig. 1. The two-terminal-pair network has a matrix which is defined in terms of the input and output voltages and currents
the sign appropriate to the output current of active networks with the sign convention of Fig. 1. This at first seems confusing, but the confusion decreases rapidly with practice. Failure to have a consistent sign convention leads to far worse confusion, because the signs of half the elements of the matrices to be described will then be in doubt. With the sign convention of Fig. 1, there are two linear relations between the four quantities $V_{1}, I_{1}, V_{2}$ and $I_{2}$. These relations can be written in the form

$$
\begin{align*}
& V_{1}=a_{11} V_{2}+a_{12} I_{2}  \tag{1}\\
& I_{1}=a_{21} V_{2}+a_{22} I_{2} \tag{2}
\end{align*}
$$

where
$\left.a_{11}=V_{1} / V_{2}\right]_{I_{2}=0}=$ reciprocal of open-circuit voltage attenuation factor
$\left.a_{12}=V_{1} / I_{2}\right]_{V_{2}=0}=$ forward short-circuit transfer impedance
$\left.a_{21}=I_{1} / V_{2}\right]_{I_{2}}=0=$ backward open-circuit transfer admittance $\left.a_{22}=I_{1} / I_{2}\right]_{V_{2}}=0$ reciprocal of short-circuit current attenuation factor.
Alternative ways of writing the linear relations (1) and (2) will be considered in a later article. For the present, we are only concerned with the fact that the expression

$$
A=\left(\begin{array}{ll}
a_{11} & a_{12}  \tag{3}\\
a_{21} & a_{22}
\end{array}\right)
$$

obtained by orderly arrangement of the coefficients of (1) and (2), can be regarded as a single entity representing the essential properties of the network, in spite of the fact that four complex numbers are required to define $A$. Matrix algebra enables us to handle the "A-matrix" $A$ as a single entity. Any information thus obtained could, in fact, be obtained by means of equations (1) and (2). The process, however, is not only greatly simplified by means of matrix algebra, but also its physical meaning and significance become clearer. Matrices enable us to express the behaviour of a complicated network in terms of that of its component parts.

The quantities $a_{11}, a_{12}, a_{21}$ and $a_{22}$ are called the elements of the $A$-matrix (3). They are unique, that is to say, they are determined entirely by the performance of the network, and remain unchanged if the network is replaced by any of the many possible equivalentcircuit representations of it.

By considering a few special cases, we shall be able to see the significance of these elements. Consider, for example, the equations (1) and (2) for an ideal transformer of ratio $\lambda: 1$. They are

$$
\left.\begin{array}{lllll}
V_{1}=\lambda V_{2} & \cdots & \ldots & \cdots & .  \tag{4}\\
I_{1}=(1 / \lambda) & I_{2} & \cdots & \cdots & \cdots \\
.
\end{array}\right\}
$$

Hence the $A$-matrix (3) becomes

$$
A_{T}=\left(\begin{array}{cc}
\lambda & 0  \tag{5}\\
0 & 1 / \lambda
\end{array}\right)
$$

so that $a_{12}$ and $a_{21}$ are both zero. We shall see later that if the network happens to have a single series element, the impedance of that element is $a_{12}$, while if the network happens to have a single shunt element, the admittance of the shunt element is $a_{21}$. The physical significance of the network is best understood in terms of $a_{12}, a_{21}$, and two other numbers $\left(a_{11} / a_{22}\right)^{1 / 2}$ and ( $a_{11} a_{22}-a_{12} a_{21}$ ) which we now consider.

If a network is symmetrical, that is to say, it remains the same if it is reversed so that input and output are exchanged, then it will be found that $a_{11}$ and $a_{22}$ are equal, whether $a_{12}$ and $a_{21}$ are zero or not. When $a_{12}$ and $a_{21}$ are zero, the ratio $\left(a_{11} / a_{22}\right)^{1 / 2}$ is seen, by comparing (3) and (5), to be the transformer ratio, which is unity in the symmetrical case. In the general case, the quantity $\left(a_{11} / a_{22}\right)^{1 / 2}$ indicates a certain resemblance between the behaviour of the actual network and the behaviour of the analogous ideal transformer having ratio $\left(a_{11} / a_{22}\right)^{1 / 2}$.

The remaining physically significant quantity associated with (3) is its 'determinant' $|A|$ defined by
$|A|=a_{11} a_{22}-a_{12} a_{21}$

This quantity, as will be shown in a later article, is always unity if the network is passive and obeys the law of reciprocity. As many practical passive networks obey this law, (3) for these networks contains only three effective independent parameters.

For purposes of thought and general understanding (though not necessarily for numerical calculation) we can therefore advantageously regard the behaviour of the four-terminal network as essentially determined by the following four quantities :
(i) the series impedance quantity $a_{12}$
(ii) the shunt admittance quantity $a_{21}$
(iii) the ratio $\left(a_{11} / a_{22}\right)^{1 / 2}$ of the analogous ideal transformer
(iv) the determinant $|A|$ given by (6), which is unity for a passive reciprocal network.
Now consider the matrix

$$
\left(\begin{array}{cc}
0 & j Z_{0}  \tag{7}\\
j / Z_{0} & 0
\end{array}\right)
$$

which is associated with an impedance inverter. The equations analogous to (1) and (2) are

$$
\begin{equation*}
V_{1}=j \lambda I_{2} ; I_{1}=j V_{2} / \lambda \tag{8a}
\end{equation*}
$$

so that, if either of $V_{1}$ or $I_{2}$ is zero, the other is also zero, and if either of $I_{1}$ or $V_{2}$ is zero, the other is also zero. (8a) can be combined in the form

$$
\begin{equation*}
\frac{V_{1}}{I_{1}} \cdot \frac{V_{2}}{I_{2}}=\lambda^{2} \tag{8b}
\end{equation*}
$$

which shows that $\lambda$ is the geometric mean of the input impedance $V_{1} / I_{1}$ and the output impedance $V_{2} / I_{2}$.

In practice, the matrix (7) is somewhat idealized but, if a network has an $A$-matrix whose elements differ by small quantities from those of (7) at a particular frequency, we can expect it to behave somewhat similarly to an impedance inverter at or near that frequency.

Thus we have seen that a network having two terminal pairs should be considered as a single entity; although it cannot be represented by a single number, it can be represented by a single $A$-matrix, whose four elements are, or are closely related to, quantities having a clear physical significance in relation to the behaviour of the network. With practice, the essential significance of many such $A$-matrices can be recognized immediately. In later articles we shall first give the rules of matrix algebra and then apply them. Initially, these rules may appear somewhat arbitrary, but they make it possible to analyse the behaviour of a complicated structure in terms of the behaviour of its component parts, and lead to a confident understanding of difficult circuits (such as coupled circuits) which is almost impossible without matrices.

# Transistor Cut-Off Frequency 

## VARIATION WITH GOLLEGTOR VOLTAGE

By W. L. Stephenson, B.Sc.*

SUMMARY. The variation of cut-off frequency with collector voltage is calculated from known physical relationships for the transistor. This leads to an expression for the Early feedback factor $\mu$ in terms of cut-off frequency and collector voltage, thereby providing a method of measurement of this factor. Other factors which can in theory be determined from these cut-off frequency measurements are the base resistivity and the effect of the field in the base at high current densities.

I$t$ is well known that the cut-off frequency of a transistor varies with the applied collector voltage. This is primarily due to the varying width of the depletion layer at the collector causing changes in the effective base width, which is also related to the Early feedback factor $\mu$.

Starting from well-known physical formulae, expressions for the relationships between cut-off frequency, collector voltage and $\mu$ can de derived, thus giving an indirect method of measuring $\mu$. Since the expressions are also affected by the base resistivity it should be possible to determine this by the same method.

[^6]For convenience of measurement the cut-off frequency used in this article is not the true $\alpha$ cut-off frequency $f_{c \alpha}$ but the frequency $f_{1}$ at which the earthed-emitter current amplification factor $\left|\alpha^{\prime}\right|=1$. The arguments, however, are equally valid for $f_{c \alpha}$.

## Assumptions

Certain fundamental, physical relationships are assumed and these will be described in detail.

The variation of $\alpha$ with frequency at low current densities is given by ${ }^{1}$
$\alpha=\operatorname{sech} \sqrt{j \omega \frac{W^{2}}{D}}$
where $W$ is the effective base width
$D$ is the diffusion constant for minority carriers in the base.
Putting $\sqrt{\frac{\omega \overline{W^{2}}}{2 D}}=A$ this can be written as

$$
\begin{align*}
& \qquad \begin{aligned}
& \alpha=\frac{1}{\cosh A \cos A+j \sinh A \sin A} \\
& \text { Since } \quad \alpha^{\prime}=\frac{\alpha}{1-\Omega} \\
& \text { we have } \quad\left|\alpha^{\prime}\right|=\frac{1}{\cosh A-\cos A} \\
&=1 \text { when } A=0 \cdot 9986 \approx 1 \\
& \therefore|\alpha|=1 \text { at a frequency given by } \\
& \omega_{1}=\frac{2 D}{W^{2}} \quad . \quad . \quad . \quad . \quad .
\end{aligned} .
\end{align*}
$$

This compares with the well-known formula

$$
\omega_{c \alpha}=\frac{2 \cdot 43 D}{W^{2}}, \text { giving } f_{c \alpha}=1 \cdot 22 f_{1}
$$

At normal currents, the diffusion constant is increased


Fig. 1. Variation of $f_{1}$ with $V_{c}$ for four transistors. The curves are drawn to different scales and the letters indicate which one is applicable. The curves show calculated results; measured points are indicated by $\times$
by a factor $n$ on its low current value. This factor lies between the values 1 and 2 and depends on the current density at the emitter.

Equation (2) may therefore be rewritten:

$$
\begin{equation*}
f_{1}=\frac{n D_{0}}{\pi W^{2}} \cdot 10^{-6} \tag{3}
\end{equation*}
$$

where $f_{1}$ is measured in $\mathrm{Mc} / \mathrm{s}$.
The relationship between the width of the collector depletion layer and the voltage across the collector junction is given by ${ }^{2}$

$$
\begin{equation*}
W_{d}=N \sqrt{\rho V_{c}} \tag{4}
\end{equation*}
$$

where $\rho$ is the resistivity of the base material in $\Omega-\mathrm{cm}$ and $N$ depends on the type of base material used.

If the resistivity on the base side of the collector junction is considerably higher than that on the collector side (which is normally the case), the depletion layer is almost entirely contained in the base so that

$$
\begin{equation*}
W=W_{0}-W_{d} \tag{5}
\end{equation*}
$$

where $W_{0}$ is the distance between the junctions.

## Variation of $\boldsymbol{f}_{\mathbf{1}}$ with $\boldsymbol{V}_{\boldsymbol{c}}$

On the basis of these two assumptions a relationship between $f_{1}$ and $V_{c}$ can be derived.
From (3)

$$
\begin{align*}
\frac{d f_{1}}{d V_{c}} & =-\frac{2 n D_{0} \times 10^{-6}}{\pi W^{3}} \cdot \frac{d W}{d V_{c}}  \tag{6}\\
& =-2 \cdot 10^{3} \sqrt{\frac{\pi}{n D_{0}}} f_{1}^{3^{\prime} \cdot 2} \frac{d W^{\gamma}}{d V_{c}} \tag{7}
\end{align*}
$$

From (4) and (5)

$$
\begin{equation*}
\frac{d W}{d V_{c}}=-\frac{d W_{a}}{d V_{c}}=-\frac{N}{2} \sqrt{\frac{\rho}{V_{c}}} \tag{8}
\end{equation*}
$$

and from (7) and (8)

$$
\begin{align*}
& \frac{d f_{1}}{d V_{c}}=N \times 10^{3} \sqrt{\frac{\pi \rho}{n D_{0}}} \cdot f_{1}^{3 / z_{b}^{-}} V_{c^{-3}}  \tag{9}\\
& \therefore \quad \int f_{1}^{3 / 2} d f_{1}=\lambda \int V_{c}^{-\frac{1}{2}} d V_{c} \\
& \text { where } \lambda=N \times 10^{3} \sqrt{\frac{\pi \rho}{n D_{0}}}  \tag{10}\\
& \therefore \quad 2 f_{1}^{-\frac{1}{2}}=-2 \lambda V_{c^{\frac{1}{2}}}+\text { a constant } \\
& \text { so that } \\
& f_{1^{-\frac{1}{2}}}-f_{0^{-\frac{1}{2}}}=\lambda\left(V_{0^{\frac{1}{2}}}-V_{c^{\frac{1}{2}}}\right) \tag{11}
\end{align*}
$$

where $f_{0}$ and $V_{0}$ are any corresponding values of frequency and voltage.

A similar formula with $V_{0}=0$ was derived by Ebers and Miller ${ }^{3}$.

The value of $\lambda$ may conveniently be determined in practice by measuring at two voltages, the difference of whose square roots is an integer. Such voltages are l, 4 and 9 volts, so that

$$
\lambda=\left(f_{1}^{-\frac{1}{2}}\right)_{1}-\left(f_{1^{-\frac{1}{2}}}\right)_{4}=\left(f_{1^{-\frac{1}{2}}}\right)_{4}-\left(f_{1^{-\frac{1}{2}}}\right)_{9}
$$

where the suffix indicates the value of collector voltage.
Once $\lambda$ is known the value of $f_{1}$ at all intermediate points may be calculated using equation (11). Measured and calculated results agreed within $\pm 1 \%$, and the form of the curve can be seen in Fig. 1.

## Variation of $\mu$ with $V_{c}$

By definition ${ }^{4}$ the Early feedback factor $\mu$ is given by

$$
\begin{equation*}
\mu=-\frac{k T}{q} \cdot \frac{1}{W} \cdot \frac{d W}{d V_{c}} \cdots \tag{12}
\end{equation*}
$$

where the negative sign is that of the collector voltage and from equation (6)

$$
\begin{align*}
\frac{d f_{1}}{d V_{c}} & =-\frac{2 n D_{0}}{\pi W^{2}} 10^{-6} \cdot \frac{1}{W} \cdot \frac{d W}{d V_{c}} \\
& =-2 f_{1} \cdot \frac{1}{W} \cdot \frac{d W}{d V_{c}} \tag{13}
\end{align*}
$$

$\therefore$ From equations (12) and (13)

$$
\begin{equation*}
\mu=\frac{k T}{q} \cdot \frac{1}{2 f_{1}} \cdot \frac{d f_{1}}{d V_{c}} \tag{14}
\end{equation*}
$$

Since this equation has been derived without any assumptions about the base resistivity or the collector depletion layer, but only that $f_{1} \propto 1 / W^{2}$ it does not necessarily apply only to alloy transistors. Also, since $f_{1}$
is directly proportional to $f_{c \alpha}$, equation (14) is equally true with $f_{1}$ replaced by $f_{c \alpha}$.

In the case of alloy transistors, equation (9) applies, and equation (14) may be rewritten as

$$
\begin{equation*}
\mu=\frac{k T}{q} \cdot \frac{\lambda}{2} \cdot \sqrt{\frac{f_{1}}{V_{c}}} \tag{15}
\end{equation*}
$$

$\mu$ may therefore be measured in two ways: (a) by measuring $f_{1}$ and $d f_{1} / d V_{c}$ at some particular voltage and applying equation (14); (b) by measuring $\lambda$ as outlined in section (3) and applying equation (15). This is only true for alloy transistors.

The measurements of $\mu$ by this method agree to about $20 \%$ with the voltage feedback ratio in earthed-base circuits ( $h_{12}$ ) measured at low currents.

The variation of $\lambda$ with voltage and current is given in Fig. 2.

## The Coefficient $\lambda$

In equation (10) this was defined by

$$
\lambda=N \times 10^{3} \sqrt{\frac{\pi \rho}{n D_{0}}}
$$

$\rho$ and $D_{0}$ are independent of current, so that any


Fig. 2. Variation of feedback factor $\mu$ with $V_{c}$ at $I_{e}=1 m A(a)$, and with $I_{e}$ at $V_{c}=6 \mathrm{~V}(b)$
variation of $\lambda$ with current is due to changes in $n$, which is a measure of the field present in the base region due to a high concentration of minority carriers.

In theory $n=1$ at low current levels and $n=2$ at high current levels so that $\rho$ may be determined from the value of $\lambda$ measured at different current levels.

In practice, however, the low-current values of $f_{1}$ are affected by the emitter depletion-layer capacitance and, at high current, the value of $f_{1}$ falls as the hole flow lines
move away from the centre of the emitter and the effective base-width increases.

This makes the determination of $\rho$ by this method


Fig. 3. Change of $\rho / n$ with $I_{e}$ for four transistors
somewhat inaccurate. The variation of $\rho / n$ calculated from the formula

$$
\begin{aligned}
\frac{\rho}{n} & =\frac{D_{0} \lambda^{2}}{\pi N^{2}} \times 10^{-6} \\
& =1 \cdot 14 \times 10^{3} \lambda^{2} \text { for germanium p-n-p transistors }
\end{aligned}
$$ is given in Fig. 3.

## Conclusions

The form of the variation of cut-off frequency with collector voltage for alloy transistors has been determined theoretically and has shown good agreement with practical measurements.

The theory also shows that the Early feedback factor may be determined from the change of cut-off frequency with collector voltage, and this is not necessarily limited to alloy transistors.

In theory, the measurement of the cut-off frequency variation can also be used to determine the resistivity of the base materials but, due to other effects, this does not give very accurate results in practice.

## Acknowledgements

The author wishes to thank the Director of Mullard Research Laboratories and the Directors of Mullard Limited for permission to publish this paper.

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## CORRECTIONS

In the article "Input Resistance of L.F. Aerials" in the May 1955 issue of Wireless Engineer (pp. 131-138) an error occurred in equation (9). In the right-hand expression, the first term in square brackets should be

$$
\frac{h}{\rho^{2}\left(\rho^{2}+h^{2}\right)^{\frac{1}{2}}}
$$

The Cossor transmitter/receiver illustrated on p. 408 of our November 1957 issue was incorrectly described as a motor-cycle radio telephone. It is, in fact, a 6 -Ib f.m. walkie-talkie.

# Push-Pull Amplifier Design 

By R. G. Christian, Graduate I.E.E., Grad. Brit. I.R.E.*

SUMMARy. A method of designing class AB push-pull amplifiers which eliminates the need to plot composite characteristics is discussed, and some examples are given which compare favourably with practical results.

Thhe design of push-pull amplifiers by means of composite characteristics suffers from the severe disadvantage that in plotting these characteristics the supply voltage and grid bias must be chosen first for each set of curves. In the design of an amplifier, several sets of curves may have to be plotted in order to obtain the best operating conditions. This is a tedious and timeconsuming procedure which is only necessary if it is


Fig. 1. (a) Ideal $I_{a}-V_{a}$ curves; (b) anode-current variation over one cycle
desired to compute the harmonic distortion present. Langford-Smith ${ }^{1}$ describes an approximate method for triodes and pentodes using only one set of anode-current-anode-voltage curves which would appear to suffer from the disadvantage that it gives optimistic results. The method to be described here is suitable for triodes and pentodes and the results obtained err on the pessimistic side. The author considers this to be an advantage since, if the design is within the specification by calculation, it will certainly be so in practice.

## Design Method

Ideal triode characteristics are shown in Fig. 1 (a) in which the operating point is P and the no-signal anode current per valve is $I_{0}$. The anode load is $R_{L}$ which is a quarter of the anode-to-anode load and is assumed to be a straight line passing through the point $P$. This point corresponds to an anode supply voltage $V_{b}$ and a fixed grid bias $-V_{g}$ as for a single-ended stage. The graph of anode current against time for a sinusoidal grid input voltage is shown in Fig. 1 (b) and is drawn as a negative cosine wave for ease of calculation. The shaded area represents current flow in the valve, which

[^7]is non-conducting over the remaining portion of the cycle. The average value of anode current for two valves is shown in the appendix to be
\[

$$
\begin{align*}
& I_{\text {ave }}=2 / \pi\left[I_{0}(\pi-a)+I_{m} \sin a\right]  \tag{1}\\
& \text { where } a=\cos ^{-1}\left(I_{0} / I_{m}\right)
\end{align*}
$$
\]

The peak current $I_{m}$ is readily obtainable from the loadline graph and is used to compute the output power in the load which is

$$
\begin{equation*}
P_{0}=I_{m}^{2} R_{L} / 2 \ldots \tag{3}
\end{equation*}
$$

The d.c. power input to the stage at maximum power output is

$$
\begin{equation*}
P_{i}=\mathrm{V}_{b} \cdot I_{a v e} \tag{4}
\end{equation*}
$$

giving an anode efficiency of

$$
\begin{equation*}
\eta=P_{0} / P_{i} \tag{5}
\end{equation*}
$$

and an anode dissipation per valve of

$$
\begin{equation*}
P_{a}=\frac{1}{2}\left(P_{i}-P_{0}\right) \tag{6}
\end{equation*}
$$

The analysis assumes fixed bias operation but it could be applied to circuits using cathode bias in which case the result would be even more pessimistic. This is due to the increase in bias which occurs as the mean anode current rises from $I_{0}$ to $I_{\text {ave }}$ resulting in greater power output and smaller average current.

## Examples

Two examples are given, one for a pair of pentodes, the second for a pair of triodes, each pair operating in class AB push-pull with fixed bias.
(1) Pentode. Fig. 2 shows anode characteristics for an EL37 pentode and a load line is drawn to represent


Fig. 2. $I_{a}-V_{a}$ curves for EL37 pentode


Fig. 3. $I_{a}-V_{a}$ curves for $2 A 3$ triode
operation with an h.t. supply of 400 V , a grid bias of -35 V and an anode-to-anode load of $3250 \Omega$. The load per valve is $812 \Omega$ and the no-signal anode current per valve $I_{0}$ is 50 mA . From the graph $I_{m}=410 \mathrm{~mA}$ giving $\cos a=50 / 410=0 \cdot 121$, whence $a=1 \cdot 24$ radians and $\sin a=0.94$. The average anode current with maximum signal is

$$
I_{a v e}=2 / \pi[50(\pi-1 \cdot 24)+(410 \times 0.94)]=306 \mathrm{~mA}
$$ and the power output is $P_{0}=410^{2} \times 812 / 2 \times 10^{6}=68 \mathrm{~W}$.

(2) Triode. Anode characteristics for a 2A3 triode are plotted in Fig. 3 on which a load line is drawn for an anode-to-anode load of $3000 \Omega$, an h.t. supply of 300 V and a grid bias of -62 V . The load per anode is $750 \Omega$ and the no-signal current per valve is 40 mA . From the graph, $I_{m}=225-40=185 \mathrm{~mA}$ giving $a=$ 1.35 radians, $\sin a=0.977, \pi-a=1.79$ radians.

TABLE 1

|  | EL37 Pentode |  | 2A3 Triode |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Design value | Makers' figure | Design value | Makers' figure |
| Supply voltage (V) | 400 | 400 | 300 | 300 |
| Grid bias (V) | -35 | -35 | -62 | -62 |
| Anode-to-anode load( $\Omega$ ) | 3250 | 3250 | 3000 | 3000 |
| Anode current, no-signal (mA) | 100 | 100 | 80 | 80 |
| Anode current, max. signal (mA) | 306 | 276 | 151 | 147 |
| Power output (W) | 68 | 69 | 13 | 15 |
| Peak-to-peak grid input | 70 | 70 | 124 | 124 |

The average anode current with maximum signal for two valves is therefore
$I_{\text {ave }}=2 / \pi[(40 \times 1 \cdot 79)+(185 \times 0 \cdot 977)]=151 \mathrm{~mA}$ and the power output is $P_{0}=\left(185^{2} \times 750\right) / 2 \times 10^{6}=13 \mathrm{~W}$. The results obtained above are compared with those obtained from the data sheets issued by the valve manufacturers in Table 1.

## Conclusions

The results using this method are in fairly good agreement with the makers' figures although they tend
to be somewhat pessimistic in that lower values of power output and higher values of average anode current are obtained. This is probably due to the fact that the method assumes linear characteristics and a linear load line for each valve, which is not so in practice. The errors are not large and, moreover, they are on the right side. If the harmonic distortion is required, it will be necessary to plot the composite characteristics, in which case this method should suffice as a starting point to determine suitable values of anode and grid voltages. If the distortion is to be measured in an actual circuit rather than estimated beforehand, then the design should be possible without further curve-plotting. Furthermore, in this era of heavy negative feedback, harmonic distortion is of less importance.

## REFERENCE

${ }^{1}$ F. Langford Smith, "Radio Designer's Handbook", 1953, pp. 577-580, pp. 583-584. (Iliffe \& Sons).

## APPENDIX

The anode-current curve is chosen to be a negative cosine curve added to a direct current $I_{0}$, giving the equation for anode current as $I_{a}=I_{0}-I_{m} \cos \theta$
The shaded area under the curve is

$$
\begin{aligned}
& \int_{a}^{b} J_{a} \cdot d \theta=\int_{a}^{b}\left(I_{0}-I_{m} \cos \theta\right) d \theta \\
= & {\left[I_{0} \theta-I_{m} \sin \theta\right]_{a}^{b}=I_{0}(b-a)-I_{m}(\sin b-\sin a) }
\end{aligned}
$$

Now $a+b=2 \pi$ or $a=2 \pi-b$
$\sin a=\sin (2 \pi-b)=-\sin b$
$b-a=2 \pi-a-a=2(\pi-a)$
$\cos a=I_{0} / I_{m}$
$\therefore$ area $=2 I_{0}(\pi-a)+2 I_{m} \sin a$
and the average current for two valves is
$I_{a v e}=2 / \pi\left[I_{0}(\pi-a)+I_{m} \sin a\right] \quad . . \quad . \quad . . \quad$.. (1)
where $a=\cos ^{-1}\left(I_{0} / I_{m}\right) \quad . \quad$.. .. .. .. .. (2)

## TALKING BOOKS FOR THE BLIND

The organizers of the Nuffield Talking Books Library for the Blind, the function of which is to distribute gramophone equipment and gramophone records of readings of books, have asked for assistance from radio engineers. Blind persons frequently have difficulty in operating the equipment, although this is very simple. The organization would like voluntary helpers to give assistance to users and also to carry out simple maintenance. There are Talking Books centres throughout the country, but those offering help are asked in the first instance to write to D. Finlay Maxwell, Esq., J. Gladstone \& Co., Ltd., Galashiels, Scotland.

## I. E. E. CONVENTION ON RADIO AIDS TO AERONAUTICAL AND MARINE NAVIGATION

The Committee of the Radio and Telecommunication Section of the Institution are arranging a Convention on Radio Aids to Aeronautical and Marine Navigation to be held at the Institution on the 27th and 28th March 1958. The following subjects will be covered: Ground, Air and Shipborne Radar; Harbour and Airfield Approach Aids; Hyperbolic and Distance-Bearing Navigational Aids; Doppler and Inertia Navigation.

The Convention is open to members and non-members and the registration fee and other fees payable will be announced in due course.

# Correspondence 

Letters to the Editor on technical subjects are always welcome. In publishing such communications the Editors do not necessarily endorse any technical or general statements which they may contain.

## The Use of Power Series in Network Responses

Sir,-The article by "Computer" in the December 1957 issue on the subject of Power Series Solutions to transient problems will have aroused interest in this method, and I am therefore prompted to draw attention to some extensions to it which have the virtue of neatness-almost elegance-from the mathematical point of view. Unfortunately they are not quite so attractive when applied to numerical and empirical problems.
If the input waveform to a network is zero until time $t=0$, and if the input and output waveforms are expressed in power-series form, then the unit-step response of the network can be calculated in the same form from the coefficients of the input and output series. The transfer function is readily obtained from the new coefficients by the use of Heaviside's Series Expansion Theorem.

Let the input waveform be $E(t)=\sum_{n=1}^{n} a_{n} t^{n}$
Let the output waveform be $F(t)=\sum_{n=2}^{n=\infty} b_{n} t^{n}$
Let the unit-step response of

$$
\begin{equation*}
\text { the network be } \phi(t)=\sum_{m=1}^{m=} c_{m} t^{m} \quad \ldots \tag{3}
\end{equation*}
$$

Now in reference 1 the following relationship is derived:

$$
\begin{align*}
& F(t)=\sum_{n=1}^{n=\infty} \sum_{m=1}^{m=\infty} a_{n} c_{m} \frac{n!m!}{(n+m)!} t^{m+n} \tag{4}
\end{align*}
$$

$$
\begin{align*}
& +\left(\frac{1}{5} a_{1} c_{4}+\frac{1}{10} a_{2} c_{3}+\frac{1}{10} a_{3} c_{2}+\frac{1}{5} a_{4} c_{1}\right) t^{5} \\
& +\left(\frac{1}{6} a_{1} c_{5}+\frac{1}{15} a_{2} c_{4}+\frac{1}{20} a_{3} c_{3}+\frac{1}{15} a_{4} c_{2}+\frac{1}{6} a_{5} c_{1}\right) t^{6} \\
& +\left(\frac{1}{7} a_{1} c_{6}+\frac{1}{21} a_{2} c_{5}+\frac{1}{35} a_{3} c_{4}+\frac{1}{35} a_{4} c_{3}+\frac{1}{21} a_{5} c_{2}+\frac{1}{7} a_{6} c_{1}\right) t^{7} \\
& + \text { etc. } \tag{5}
\end{align*}
$$

(Remaining terms are derived thus: for any power $n$ the first and last terms have denominator $n$, and the denominator of any other term is the sum of the corresponding denominator and the one before it in the previous row)

Thus we have, from Equ. (2),

$$
b_{2}=\frac{1}{2} a_{1} c_{1}, \quad b_{3}=\frac{1}{3} a_{1} c_{2}+\frac{1}{3} a_{2} c_{1} \text { and so on. }
$$

It is therefore easy to determine the coefficients of the unit-step response of the network, thus:

$$
\begin{align*}
& c_{1}=2 b_{2} / a_{1} \\
& \begin{aligned}
c_{2}= & \frac{b_{3}-\frac{2}{3} \frac{a_{2} b_{2}}{a_{1}}}{\frac{1}{3} a_{1}}=\frac{3 a_{1} b_{3}-2 a_{2} b_{2}}{a_{1}{ }^{2}} \\
c_{3}= & \frac{4}{a_{1}}\left(b_{4}-\frac{1}{6} a_{2} c_{2}-\frac{1}{4} a_{3} c_{1}\right) \\
& =\frac{4}{a_{1}{ }^{3}}\left[a_{1}{ }^{2} b_{4}-\frac{a_{1} a_{2}}{2} b_{3}+\left(\frac{1}{3} a_{2}{ }^{2}-\frac{1}{2} a_{1} a_{3}\right) b_{2}\right] .
\end{aligned}
\end{align*}
$$

and so on, by a simple and not-too-laborious process. Thus $\phi(t)$ is readily calculated.
The transfer function, $T(p)$, of the network can now be obtained in series form by the use of Heaviside's Series Expansion ${ }^{2,4,5}$; thus:

$$
\begin{equation*}
\text { If } T(p)=\sum_{n=1}^{n=\infty} \frac{d_{n}}{p^{n-1}} \tag{7}
\end{equation*}
$$

and if this series is convergent (e.g., if $\left|p^{n-1}\right|>d_{n}$ ), then

$$
\begin{equation*}
\phi(t)=\sum_{n=1}^{n=\infty} \frac{d_{n} t^{n-1}}{(n-1)!} \tag{8}
\end{equation*}
$$

Now since $\phi(t)$ has been determined above, Equ. (3), then clearly $d_{n}=(n-1)!c_{n-1}$, and the corresponding transfer function is

$$
\begin{equation*}
T(p)=\sum_{n=1}^{n=\infty} \frac{(n-1)!c_{n-1}}{p^{n-1}} \tag{9}
\end{equation*}
$$

which may be more simply written as

$$
\begin{equation*}
T(p)=\sum_{n=1}^{n=\infty} \frac{n!c_{n}}{p^{n}} \tag{10}
\end{equation*}
$$

since it is assumed that $c_{0}=0$.

## Observations on the Use of this Method

In practice, where power series are fitted empirically to observed functions, the series (1) and (2) cannot be infinite, and will have to be restricted to a relatively small number of terms which adequately describe the function over a limited range of $t$. If $r$ terms are taken, then the waveform can be exactly fitted at $r$ points (apart from $t=0$ ). But it should be observed that, in the process of reference 1, if $E(t)$ and $\phi(t)$ are represented by $r$ terms each, then according to Equ. (5), $F(t)$ will contain non-zero terms up to $t^{2 r}$. Therefore, in operating the reverse process [i.e., in determining $\phi(t)$, given $E(t)$ and $F(t)$ ] it is necessary to take terms up to $t^{4}$ in $E(t)$ but up to $t^{2 r}$ in $F(t)$ if a correct series of $r$ terms for $\phi(t)$ is to be obtained. Good results have been obtained when this has been done, but errors become large if only $r$ terms are taken in $F(t)$.

When we come to consider the use of Equ. (10) to represent the transfer function, we encounter further practical difficulty. Since the waveforms are fitted to the power series over only a limited range of time, and the steady-state response is not represented, then it is clear that the power series in $1 / p$ cannot be expected to be correct for low values of $p$. If we restrict consideration to the transfer function $T(\omega)$ (obtained on putting $p=j \omega$ ), clearly we would not expect this to apply at frequencies below the reciprocal of the highest time fitted in the power-series in $t$. This would probably mean that $T(\omega)$ would apply only above the cut-off frequency in the case of a low-pass filter.

The relationship between $\phi(t)$ and $T(\omega)$, if carefully fitted by empirical power series, is reliable in respect of the ultimate slope of the network loss response. For instance, an $m$-derived resistanceterminated single-section Zobel filter has an ultimate cut-off slope of 6 dB per octave, and this is indicated by its transient response having a linear term in $t$, corresponding to a dominant term in $1 / \omega$ in the transfer function at high frequencies; but a similar constant- $k$ filter has a transient response without linear or square term ${ }^{3}$, so that the dominant term in $T(\omega)$ is $1 / \omega^{3}$, correctly indicating an ultimate slope of 18 dB /octave.

Electrical Engineering Department, D. G. Tucker
University of Birmingham.
6th December 1957.

## REFERENCES

${ }^{1}$ D. G. Tucker, "A Note on Duhamel's Integral . . .", Phill. Mag., 1948, Vol. ${ }^{39}$, p. 203 . Carslaw and J. C. Jaeger, "Operational Methods in Applied Mathematics', Oxford, 1949 , p. ix and p. 271
${ }_{3}^{3}$ D. G. Tucker, "Transient Response of Filters", Wireless Engineer, 1946,
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'E. J. Berg, "Heaviside's Operational Calculus", New York, 1936.
${ }^{8}$ H. J. Josephs, "Heaviside's Electric Circuit Theory", Methuen, London, 1946.

## Son et Lumière

Sir,-In your October issue " "Quantum" has shown the difference between the Doppler effect in acoustics and optics, using the Galilean and Lorentz transformations respectively. This is quite a natural procedure since, in the optical case, the Lorentz transformation must be used while, in the acoustic case, the Galilean transformation may be used without introducing practically measurable errors. Thus, quite unintentionally, an impression could have been created that the difference is in some way connected with the fact that two different transformations have been used. This is obviously not the case, since there is nothing that forbids the use of the Lorentz transformation in the acoustic case. Hence it may seem advisable to state explicitly that the difference between the two cases is due to the sole fact that in the optical case we deal with two frames of reference, while in the acoustic case we have three such frames.

This is a trivial statement, saying simply that an ether does not exist while air (or any other sound-propagating medium) does. Its importance lies in its form which emphasizes the fact that both cases, while being identical from the point of view of mathematical treatment (both being represented by the wave equation and yielding an exact solution with the aid of the Lorentz transformation) differ in the physical models which represent them-namely the existence of an additional frame of reference in the acoustic case. "Quantum's" paper is a well-timed contribution to the clarification of an almost controversial subject, in view of some recent reports on the application of the Doppler effect ${ }^{2,3,4}$.
Ministry of Defence,
Efraim Weissberg
Tel Aviv, Israel.
10th December 1957.

## REFERENCES

${ }^{1}$ Quantum "Fringe of the Field; Son et Lumière", Electronic and Radio Engineer, Octóber 1957, Vol. 34, No. 10 .
Standard Station, et al., "Doppler Shift of the Received Frequency from the Standard Station Refle
"Brown et al., "Radio Observations of the Russian Earth Satellite", Proc Inst. Radio Engrs, Nov. 1957, Vol. 45, P. 1552.
4. M. Peterson, "Radio and Radar Pracking of the Russian Earth Satellite",
Proc. Inst Radio Engrs, Nov, 1957, Vol. 45, p. 1553 .

Sir,-Although I did not put it in quite the same way as Mr. Weissberg, the purpose of the article was to emphasize the error of using the Galilean transformation with its single frame of reference in dealing with the optical case where there are two frames. The point would have been obscured for many readers if I had harped on unmeasurably small inexactness when the Galilean transformation is used for the acoustic case. For, accepting Newtonian mechanics for acoustics, the argument is exact; but if we try this on with optics, the argument is wrong whether or not the error in the result is detectable.
To the mathematician, a procedure must be general or it is valueless. The physicist as a rule works in Newtonian terms as long as he has (or thinks he has) a Galilean reference frame, and generalizes only when it is forced on him. I agree with what your correspondent has said so clearly, of course. But I would take the line that the existence of the third frame of reference renders the other two redunant for all practical purposes.
Taking the formal analogy between the two cases as being complete, if we use the Lorentz transformation in acoustics, then the $c$ is the velocity of sound. We should have to do this if clocks could only be synchronized by sound-signals. In fact, in doing this we discard any information that light-signals may afford us, and are effectively choosing to work blindfolded. There is nothing that forbids us to do this at any time if we want to. It would be worth while to inconvenience ourselves in this way only if acoustic measurements could be made more precisely than their optical counterparts.

6th January 1958.
Quantum

## Uncorrelated Grid Noise

Sir,-Although I am rather late in reading your November issue, I cannot pass by Mr. Harris's further contribution on grid noise, since we are now getting down to fundamentals.
Mr . Harris rejects my treatment in terms of individual electron pulses. But, in the middle of the second column of his letter, he states "the combination of $\delta i_{1}$ and $\delta i_{2}$ occurs in the conductor and not in the valve spaces", $\delta i_{1}$ and $\delta i_{2}$ being the contributions to the grid current from the cathode-grid and grid-anode spaces. I would go further, and say that provided the external circuit is linear the
two are not combined in any irrevocable sense: one finds their difference in the circuit but, if in a hypothetical case they differed in frequency, one could still separate them again. In the same way, either of these currents consists simply of the sum of its component parts (i.e., of electron transits) and one can find the response of a linear system to the whole by summing its responses to the individual parts. This is the basis of Moullin's treatment of shot noise by Fourier analysis of the individual pulses ${ }^{1}$, and is also the basis of the treatment by Campbell's theorem ${ }^{2}$. One must not assume a Fourierseries or integral representation of a random process extending over time, because (as Mr. Harris says) the phases of the components are randomly distributed; and therefore the phases cannot be known until the phenomenon under analysis is completed; i.e., one cannot predict the Fourier series from general knowledge of the characteristics of the process. What one can predict is the power spectrum (or mean-square values of frequency components) because this excludes phase and refers only to long-term averages, not to particular instances.

No one ignores the effect of pulse spacing: both the treatments cited above ${ }^{1,2}$, and also the derivation of the power spectrum via the autocorrelation function and the Wiener-Khintchine transformation, postulate that successive electron transits are uncorrelated; i.e., they state specifically that the effect of pulse spacing on the power spectrum is nil. Even the Schottky-North theory of space-charge smoothing does not postulate correlation between electron transits which do not overlap in time. It is a matter of mathematical convenience only whether one treats the phenomenon in terms of individual pulses or (in a narrow-band circuit) in terms of a nominal centre frequency which is phase-modulated by the noise. But it must be remembered that the signal applied to the narrow-barid circuit is much wider, and will therefore include phase-modulation at such a rate that the narrow circuit cannot follow it. It is not sufficient to consider the response of the circuit to the unmodulated sinusoid.
I believe that the failure to distinguish between the nature of the response of the grid circuit to random noise and to a continuous sinusoid is due in practice to the use of a detecting system of much narrower bandwidth than that of the grid circuit.

No one questions the correlation between currents in the first and second spaces so long as one means correlation between the currents due to the same group of electrons as they pass successively through the two spaces. What one must avoid suggesting is that there is some collective Fourier series (known in phase as well as amplitude) which is associated with large numbers of electrons and which extends in time with coherence over a number of successive electron transits. This obviously affects the treatment of reflected electrons as well. (Surely the distinction between reflected electrons and secondaries is that only the reflected electrons have sufficient energy to return against the field through the grid to the cathode region?)

My reason for questioning the introduction of $(\omega T)^{3}$ is that I think one should see how the second-order model fits the physical facts before bringing in a third-order term. A current $\delta i$ induces gridcurrent $\delta i_{g}$ which causes a grid voltage $\delta v_{g}$ and this in turn causes a new component of cathode current $\delta i^{\prime}=g_{m} \delta v_{g}$. But, in the absence of phasing effects between $\delta i$ and $\delta v_{g}$, the peak of $\delta i^{\prime}$ would leave the cathode as the group of electrons causing $\delta i$ passes through the grid, so that $\delta i^{\prime}$ would lag behind $\delta i$ by a time of approximately $T_{1}$. This means that $\delta v_{\mathrm{g}}$ must be further advanced relative to $\delta i$ if $\delta i^{\prime}$ is to compensate $\delta i$; and since the requisite amount is a fixed time, it will appear as an increasing phase advance with increasing frequency. This will explain the results of Houlding and Glennie, and I do not see that it requires the introduction of the term in $(\omega T)^{3}$.
Electrical Engineering Dept., D. A. Bell University of Birmingham. 24th December 1957.

REFERENCES
${ }^{2}$ E. B. Moullin, "Spontaneous Fluctuations of Voltage" (Oxford University Press, 1938), pp. 52-56
${ }^{2}$ N. R. Campbell and V. J. Francis, J. Instn elect. Engrs, 1946, Vol. 93, Part III p. 45.

## Comparison of Four Television Standards

Srr,-Dr. N. W. Lewis has informed me that there is an error in my article entitled: "A Comparison of Four Television Standards", which appeared in your November 1957 issue (Vol. 34).
The error in question relates to Fig. 4 (p. 419) for which the responses of vestigal-sideband systems were calculated by means of subtraction from unit-step responses of the same responses delayed


Fig. 4. Normalized rectangular pulse responses (demodulated outputs). The demodulated normalized display tube video voltage is given by

$$
\begin{gathered}
E^{\prime}(t)=\frac{2}{r}\left\{-\frac{1}{2} a+\sqrt{2}\left[\left[\frac{1}{2} a+\frac{r}{2 \pi}\left\{\operatorname{Si} \omega_{c} t-\operatorname{Si} \omega_{c}\left(t-10 \pi / \omega_{c}\right)\right\}\right]^{2}\right.\right. \\
\left.\left.+\frac{r^{2}}{4 \pi^{2}}\left[\frac{\sin t \Delta \omega}{t \Delta \omega}-\frac{\sin \Delta \omega\left(t-10 \pi / \omega_{c}\right)}{\Delta \omega\left(t-10 \pi / \omega_{c}\right)}+\operatorname{Ci} \omega_{c} t-\operatorname{Ci} \omega_{c}\left(t-10 \pi / \omega_{c}\right)-\operatorname{Ci} t \Delta \omega+\operatorname{Ci} \Delta \omega\left(t-10 \pi / \omega_{c}\right)\right]^{2}\right]\right\}
\end{gathered}
$$

by a time equivalent to ten picture elements for each system. Such a method may only be used for linear transmission networks and is not applicable to vestigial-sideband systems.
I am grateful to Dr. Lewis for pointing out this error and must add that the fault is mine and not Mr. J. W. Head's to whom the calculations required for Fig. 4 were ascribed.

I give herewith a correct Fig. 4 and would add that the conclusions which I came to are not altered by the above error because they were not based upon this particular figure.
Research Department,
R. D. A. Maurice

British Broadcasting Corporation,
Tadworth, Surrey.
8th January 1958.

## New Books

## Lewis's Medical, Scientific and Technical Lending Library Catalogue

Pp. 1178 + xii. Revised to December 1956. H. K. Lewis \& Co. Ltd., P.O.Box 66, 136 Gower Street, London, W.C.1. Price 42s. (to library subscribers, 25s.). Author and subject indexes.

## Electronic Designers' Handbook

By R. W. Landee, D. C. Davis and A. P. Albrecht. Pp. 1029. McGraw-Hill Publishing Co. Ltd., 95 Farringdon Street, London, E.C.4. Price $£^{688}$.

In addition to the type of general information to be expected in
reference books of this kind, there are nine chapters on particular devices, such as multivibrators, variable delay circuits, trigger circuits, clippers, limiters, and clamps. There are also chapters on waveform and network analysis.

## Basic Physics

By Alexander Efron, E.E., Ph.D. Pp. 692. John F. Rider Publisher Inc., 116 West 14th Street, New York 11, N.Y., U.S.A. Price $\$ 7.60$.

Elementary physics textbook, comprising two 'volumes' bound together. The first of these gives an introduction to the subject, and the second goes into more detail.

## F.B.I. Register of British Manufacturers 1958

Published for the Federation of British Industries by Kelly's Directories Ltd, and Iliffe \& Sons Ltd. Pp. 1138. Iliffe \& Sons Ltd., Dorset House, Stamford Street, London, S.E.1. Price 42s. post free.

Foreword by the President of the F.B.I., Sir Hugh Beaver, K.B.E.; Details of the Organization, Aims and Activities of the F.B.I. at home and overseas; French, German and Spanish sections; Products and Services: Classified Buyers' Guide; Language Glossaries; Addresses : Alphabetical Directory; Trade Associations; Brands and Trade Names; Trade Marks.

## Closed Circuit TV System Planning

By Morris A. Mayers and Rodney D. Chipp, P.E. Pp. 250. John F. Rider Publisher Inc., 116 West 14th Street, New York 11, N.Y., U.S.A. Price $\$ 10.00$. A user handbook.

## EXHIBITIONS

March 4-6. Television Society, Royal Hotel, Woburn Place, London, W.C.1.
March 24-27. Physical Society, Royal Horticultural Society's Halls, London, S.W.l.
March 24-29. International Instrument Show, Caxton Hall, Westminster, London, S.W.I.
March 25-29. Electrical Engineers' Exhibition (A.S.E.E.), Earls Court, London, S.W.5.
April 14-17. Radio \& Electronic Component Manufacturers' Federation, Grosvenor House and Park Lane House, Park Lane, London, W.1.
April 16-25. Instruments, Electronics and Automation Show, Olympia, London, W.14.
April 18-21. London Audio Fair, Waldorf Hotel, London,
(including W.C.2.

Sunday 20th)
Aug. 27-Sept. 6. National Radio Show, Earls Court, London, S.W.5.

Sept. 1-7. Farnborough Air Show, S.B.A.G., Farnborough, Hants.
Nov. 28-Dec. 4. Electronic Computer Exhibition, Olympia, London, W. 14.

## MEETINGS

I.E.E.

6th February. "High Polymers", 49th Kelvin Lecture by H. W. Melville, K.C.B., D.Sc., F.R.S.

18th February. "Magnetic Tape for Data Recording", by C. D. Mee, Ph.D. (To be read by J. F. Doust.)

19th February. ''The Relation between Picture Size, Viewing Distance and Picture Quality, with Special Reference to Colour Television and Spot-Wobble Techniques’, by L. C. Jesty, B.Sc.

24th February. "Stereophonic Recording on Gramophone Discs", by H. A. M. Clark, B.Sc.(Eng.)

4th March. "Some Impressions of Technical and Industrial Training in the United States', discussion to be opened by K. R. Sturley, Ph.D., B.Sc., at 6 o'clock.

These meetings will be held at the Institution of Electrical Engineers, Savoy Place, Victoria Embankment, London, W.C.2, commencing at 5.30 except where otherwise stated.

Brit. I.R.E.
5th February. 'rRadio Investigations during the I.G.Y.", by W. J. G. Beynon, Ph.D., D.Sc. 26th February. "DECTRA: A Long Range Navigational Aid", by C. Powell.

These meetings will be held at 6.30 at the London School of Hygiene and Tropical Medicine, Keppel Street, Gower Street, London, W.C.1.
The Television Society
7th February. "The Effects of Noise in Television Transmission", by T. Kilvington, B.Sc.

20th February. "Test Equipment for Colour Television Receivers", by F. H. Cohen and D. C. Kidd.

These meetings will be held at 7 o'clock at the Cinematograph Exhibitors' Association, 164 Shaftesbury Avenue, London, W.C.2.

## The Radar Association

12th February. "The Early Days of Radar", by Sir Robert Watson-Watt, at 7.30 at the Anatomy Theatre, University College, Gower Street, London, W.G.1.

## R.S.G.B.

14th February. "The Television Interference Problem", by G. A. Bird, to be held at 6.30 at the Institution of Electrical Engineers, Savoy Place, Victoria Embankment, London, W.C.2.

## B.S.R.A.

21 st February. "Reducing Distortion in F.M. Reception", by Dr. G. J. Phillips, to be held at 7.15 at the Royal Society of Arts, John Adam Street, Adelphi, London, W.C.2.

## Women's Engineering Society

26th February. "Three Case Studies in Automation", by G. Denton, to be held at 6.45 at Central Electricity Headquarters, Winsley Street, London, W.1.

## NEW YEAR HONOURS

Among the recipients of awards in the Queen's New Year Honours List are:
William R. J. Cook, G.B., deputy director, Atomic Weapons Research Establishment, Aldermaston, who receives a knighthood.
Dr. Harry W. Melville, secretary, Department of Scientific and Industrial Research, who is appointed a Knight Commander of the Order of the Bath.
J. E. S. Cooper, C.M.G., assistant director, Government Communications Headquarters, who becomes a C.B.
Major-General W. R. C. Penney, G.B., G.B.E., D.S.O., M.G., lately director, London Communications Security Agency, who is promoted Knight Commander of the British Empire.
E. H. Ball, managing director, British Thomson-Houston; V. A. M. Hunt, director, Civil Aviation Control and Navigation Directorate, Ministry of Transport and Civil Aviation; J. A. Mason, M.M., manager and director, Automatic Telephone and Electric and a director of British Telecommunications Research; C. Metcalfe, managing director, E.M.I. Electronics; M. J. L. Pulling, O.B.E., controller, Television Service Engineering, B.B.C., who are appointed C.B.E.s.
W. J. Challens, senior superintendent, Atomic Weapons Research Establishment, Aldermaston; Lt..Col. E. N. Elford, T.D., manager radar division, Marconi's Wireless Telegraph Co.; R. G. Fall, senior signals officer, Civil Aviation Telecommunications Directorate, Ministry of Transport and Civil Aviation; R. A. McMahon, secretary, British Electrical and Allied Industries Research Association ; H. K. Robin, chief engineer, Communications Department, Foreign Office; E. G. Rowe, chief valve engineer, Standard Telephones \& Cables, and WingCdr. E. M. Smith, M.B.E., chief executive officer, Foreign Office, Government Communications Headquarters, who become O.B.E.s.

STANDARD-FREQUENCY TRANSMISSIONS
(Communication from the National Physical Laboratory) Deviations from nominal frequency* for December 1957

| Date <br> 1957 <br> December | MSF $60 \mathrm{kc} / \mathrm{s}$ 2030 G.M.T. <br> parts in $10^{9}$ | Droitwich $200 \mathrm{kc} / \mathrm{s}$ parts in $10^{8}$ |
| :---: | :---: | :---: |
| $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \\ & 4 \\ & 5 \\ & 6 \\ & 7 \\ & 8 \\ & 9 \\ & 10 \\ & 11 \\ & 12 \\ & 13 \\ & 14 \\ & 15 \\ & 16 \\ & 17 \\ & 18 \\ & 19 \\ & 20 \\ & 21 \\ & 22 \\ & 23 \\ & 24 \\ & 24 \\ & 25 \end{aligned}$ | $\begin{aligned} & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -3 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \\ & -2 \end{aligned}$ |  |

* Nominal frequency is defined to be that frequency corresponding to a value of $9192631830 \mathrm{c} / \mathrm{s}$ for the N.P.L. caesium resonator. N.M. $=$ Not Measured.


## New Products

## Miniature Connector

A 15 -way miniature high-voltage connector has been developed which is claimed to be safe and inexpensive.

The method of connecting a cable is said to permit closer pin spacing and to require less skilled operation than orthodox methods.

Plug-pins and socket-inserts are fully shrouded in resilient polythene mouldings, which eliminate the need for gaskets and

provide the necessary insert anchorage and a considerable degree of protection against vibration.
Plugs and sockets may be used either as fixed or free units. Mating of the units is achieved without the use of coupling nuts or jacking mechanisms.

Multi-stranded cable up to a maximum o.d. of 0.075 in . and maximum conductor o.d. of 0.034 in . may be used.

The connectors have a working voltage of 1 kV and a current rating of $2 \frac{1}{2} \mathrm{amps}$ per contact and are suitable for operation in temperatures up to $80^{\circ} \mathrm{C}$. The unit occupies a total space of 0.75 sq . in.
The Plessey Co. Ltd.,
Ilford, Essex.

## Thermal Relays

Thermal relays of unusual design are available in this country from Mercia Enterprises. These are known as G-V relays, and the principle is illustrated in the drawing. A and B are identical metal members. Differential cxpansion of these causes the contact $C$ t to make. The $\operatorname{arm} \mathrm{A}$ is heated when current flows through the coil wrapped round it, causing the contact to operate after a certain time which, in different designs, ranges from about 2 sec . to 3 min . Changes in ambient temperature affect $A$ and $C$ equally, and the delay time remains substantially constant. E is a diaphragm through which protrudes the adjusting arm D, moved by the adjusting screw G. This construction cnables the device to be hermetically sealed.


In addition to effecting thermal delays, the same type of mechanism can be used for sensing the magnitude of a current passed through the coil and, can therefore, be

utilized for overload protection and voltage stablization. The makers' specification states that the operating point will not change by more than $\pm 5 \%$ over an ambient temperature range of $-70^{\circ}$ to $+100^{\circ} \mathrm{C}$, and that the differential between contact operation and contact return currents is less than $1 \%$.

A folder containing detalled information is available from the suppliers.
Mercia Enterprises Ltd.,
Godiva House, Allesley Old Road, Coventry.

## 20-Mc/s Sweep Generator

Marconi Instruments Ltcl. have introduced a new $20-\mathrm{Mc} / \mathrm{s}$ sweep generator, Type TFl099. This is a video-frequency sweep generator which, in conjunction with a

suitable oscilloscope, is said to enable response measurements to be made to better than 0.01 dB .

The sweep starts at a frequency of less than $100 \mathrm{kc} / \mathrm{s}$ and extends to an upper frequency that is continuously variable up to $20 \mathrm{Mc} / \mathrm{s}$; the lower frequency limit is locked to the start of the sweep in order to ensure a steady display on the c.r.o. The level of the frequency-swept signal is variable from 0.3 to 3 volts peak-to-peak, and the selected output level is held constant to within $\pm 0.1 \mathrm{~dB}$. A $250-\mathrm{V}$ time-base waveform, synchronized to the sweep frequency, is provided for connection to the X-plates of a cathode-ray oscilloscope, and a series of
marker pips at $1-\mathrm{Mc} /$ s intervals is available for superimposing on the display to facilitate accurate frequency identification.

The TF 1099 includes special circuits for precision differential measurement. For the differential method, the overall gain of the apparatus under test is reduced to unity by means of an external attenuator, and the outputs of the sweep generator and of the apparatus are both sampled; the two signals are then combined and the amplified difference voltage is displayed on the c.r.o. Marconi Instruments Ltd.,
St. Albans, Herts.

## Switches

Measuring less than $1 \frac{7}{8} \mathrm{in}$. by $1 \frac{1}{2} \mathrm{in}$. by $1 \frac{3}{8}$ in., these new 3 - and 4-pole lever switches are rated at 10 A ; both types are one-hole mounting.

The 3-pole types are said to be of special interest to electrical engineers on account of the sliding-action contact mechanism, which

ensures simultaneous breaking of all three contacts, an essential feature when switching 3-phase motors.
N.S.F. Ltd.,

31-32 Alfred Place, London, W.C.1.

## Electronic Recorder

The recorder illustrated was developed for the atomic-energy industries but is now generally available. Three types of input amplifier are produced. Of these, one is intended for operation from low-impedance sources, such as thermocouples, and gives a minimum instrument range of 1 mV ; the second is for a.c. signals from low or mediumimpedance sources; the third is for d.c. inputs from high-impedance sources (up to $10 \mathrm{M} \Omega$ ) and gives a minimum range of 30 mV . Other points from the makers' specification are given below.
Mains supply : $210-250 \mathrm{~V}, 40-60 \mathrm{c} / \mathrm{s}$.
Pen speed: 2 or 20 sec . full scale.
Chart speed: 1,2 or 3 in . per minute or
1, 2 or 3 in. per hour.
Accuracy : $\pm 0 \cdot 3 \%$ f.s.d.
George Kent Lid.,
Luton, Beds.


## Abstracts and References

COMPILED BY THE RADIO RESEARCH ORGANIZATION OF THE DEPARTMENT OF SCIENTIFIC AND INDUSTRIAL RESEARCH AND PUBLISHED BY ARRANGEMENT WITH THAT DEPARTMENT

The abstracts are classifed in accordance with the Universal Decimal Classification. They are arranged within broad subject sections in the order of the U.D.C. numbers, except that notices of book reviews are placed at the ends of the sections. U.D.C. numbers marked with a dagger ( $\dagger$ ) must be regarded as provisional. The abbreviations of journal titles conform generally with the syle of the World List of Scientific Periodicals. An Author and Subject Index to the abstracts is published annually; it includes a selected list of journals abstracted, the abbreviations of their titles and their publishers' addresses. Cobies of articles or journals referred to are not available from Electronic \& Radio Engineer. Application must be made to the individual publisher concerned.


ACOUSTICS
AND AUDIO FREQUENCIES
534.1.087: 621.395.616

332
The Condenser Microphone as a Displacement Detector Calibrator.-W. Koidan. (J. acoust. Soc. Amer., July 1957, Vol. 29, No. 7, pp. 813-816.) The absolute calibration of a variable-capacitance-type displacement detector was performed by using the diaphragm of a condenser microphone as a reference moving surface. Measured values of the detector response are plotted from $10 \mathrm{c} / \mathrm{s}$ to $40 \mathrm{kc} / \mathrm{s}$. See also 30 II of 1954.

## 534.2-8-16

333
Ultrasonic Attenuation in Metals at Low Temperatures in the Normal and in the Superconducting State.-G. Kurtze. (Naturwissenschaften, July 1957, Vol. 44, No. 13, pp. 368-370.) Report of measurements on $\mathrm{Cu}, \mathrm{Pb}$ and Sn single crystals for longitudinal and transverse waves.
534.2-8-16: 538.221

Change of Ultrasonic Absorption in Ferrites by an External Magnetic Field.-G. Uhlig. ( Nachr Tech., May 1957, Vol. 7, No. 5, p. 221.) Preliminary note on experiments with a ferrite rod. A strong axial magnetic field produces up to $100 \%$ reduction in the ultrasonic absorption of the $\operatorname{rod}$ at $3 \mathrm{Mc} / \mathrm{s}$.

### 534.213-8

335
Dispersion Effects in Ultrasonic Waveguides and their Importance in
the Measurement of Attenuation.-M. Redwood. (Proc. phys. Soc., 1st Aug. 1957, Vol. 70, No. 452B, pp. 721-737.) The possible sources of error are investigated which arise from the use of the pulse technique in determining absorption at $10-100 \mathrm{Mc} / \mathrm{s}$ in low-loss solid materials. Estimated errors of attenuation measurements are tabulated and compared with the intrinsic absorption in fused silica and singlecrystal Ge. See also 366 of 1957 (Redwood \& Lamb).
534.23: 621.396.677.3

336
Theory of Time-Averaged-Product Arrays.-A. Berman \& C. S. Clay. ( $J$. acoust. Soc. Amer., July 1957, Vol. 29, No. 7, pp. 805-812.) Mathematical analysis in polynomial form of the directional characteristics of linear additive arrays. It is shown that the same directional characteristics may be obtained from multiplicative arrays having a small number of detectors as with an additive array with many elements. See also 983 of 1956 (Fernandez Huerta).

### 534.232 : 534.64

337
Self-Reciprocity Transducer Calibration in a Solid Medium.-R. M. White. (J. acoust. Soc. Amer., July 1957, Vol. 29, No. 7, pp. 834-836.) The application of the self-reciprocity technique to the calibration of a reversible compressional-wave transducer is described.

### 534.25/.26-14 : 534.213.4

338
Acoustic Refraction and Scattering with Compliant Elements.-W.J. Toulis (J. acoust. Soc. Amer., Sept. 1957, Vol. 29, No. 9, pp. 1021-1033.) Various techniques of using mechanical structures, such as
compliant tubes, for effectively increasing the compressibility of water are described; the results of measurements are analysed.

### 534.75

339
Localization of High-Frequency Tones.-W. D. Fedderson, T. T. Sandel, D. C. Teas \& L. A. Jeffress. (J. acoust. Soc. Amer., Sept. 1957, Vol. 29, No. 9, pp. 988991.) Continuation of earlier work ( 649 of 1956).
534.76: 534.78

## 340

Mechanism of Binaural Fusion in the Hearing of Speech.-B. M. Sayers \& E. C. Cherry. (J. acoust. Soc. Amer., Sept. 1957, Vol. 29, No. 9, pp. 973-987.) The mechanism is discussed as a form of statistical operation based upon the brain's execution of running cross-correlation of the two ear signals.

### 534.846

341
Acoustics of Large Orchestral Studios and Concert Halls.-K. L. Rao: T. Somerville \& C. L. S. Gilford. (Proc. Instn elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, p. 597.) Comment on 2017 of 1957 and authors' reply.

### 621.395.625.6: 534.862.3

342
Improved Light Valve for the Photograpbic Recording of Vibrations.-G. Menon Sreekantath. (J. acoust. Soc. Amer., Sept. 1957, Vol. 29, No. 9, pp. 1034-1035.) A beam of light is modulated by passing through two similar coarse gratings one of which vibrates, and the modulations are recorded on a moving photographic film. The process may be applied to sound recording.

## AERIALS

AND TRANSMISSION LINES
621.315 .212

343
Multiple Screening of Flexible Coaxial Cables.-L. Krügel. (Telefunken Ztg, Sept. 1957, Vol. 30, No. 117, pp. 207-214. English summary, pp. 218-219.) The screening effect of double layers of braiding with and without intermediate magnetic shields is investigated; results are given in graphical form. See also 2334 of 1957.

### 621.315.212.095.3: 621.372.2

344
An Iteration Method for Computing Electromagnetic Fields.-A. Redhardt. (Arch. elekt. Ubertragung, June 1957, Vol. 11, No. 6, pp. 227-230.) The conditions at a discontinuity inside a coaxial line are analysed and the resulting field is computed.
621.372 .2 345
Initial Value Problems and Time Periodic Solutions for a Nonlinear Wave Equation.-F. A. Ficken \& B. A Fleishman. (Commun. pure appl. Math., Aug. 1957, Vol. 10, No. 3, pp. 331-356.) A discussion of an equation governing the displacement of a taut string, with restraining forces, and applicable to the voltage on a uniform transmission line with certain nonlinear characteristics.
621.372 .2

346
Return Loss: Part 2.-T. Roddam. (Wireless World, Dec. 1957, Vol. 63, No. 12, pp. 583-588.) The relation between loss and circuit response characteristics is discussed with particular reference to distortion in a television picture. Methods of measuring return loss are described. Part 1: 16 of January.
621.372.22.09

Theory of Nonuniform Lines.-R. Codelupi. (Alta Frequenza, Aug. 1957, Vol. 26, No. 4, pp. 226-282.) Mathematical functions are derived for use in determining the input impedances and voltages along the line and at its terminals. Examples of analyses for multiple reflections are given.

### 621.372.51: 621.396.674

348
A 200-Watt Balun Coupler for CentreFed Antennas.-J. M. Shulman. (QST, June 1957, Vol. 41, No. 6, pp. 26-28.) Commercial-type wide-band balun coils are used to provide either $75 \Omega / 75 \Omega$ or $75 \Omega / 300 \Omega$ unbalance/balance transformation.

### 621.372.51.029.6: 621. 317.335.3 <br> 349

The Dielectric Disk used as Transformation Quadripole for the Magnification of the Node Displacement on Measuring Lines.-L. Breitenhuber. (Arch. elekt. UUbertragung, June 1957, Vol. 11, No. 6, pp. 223-226.) The maximum attainable node displacement is derived as a function of the thickness and the dielectric constant of the disk. The maximum is obtained when the disk shifts the phase by $45^{\circ}$; in this case and for very high dielectric constants the magnification of the node displacement is directly proportional to the dielectric constant.

Characteristics of some Ferrous and Nonferrous Waveguides at 27 Gc/s.J. Allison, F. A. Benson \& M. S. Seaman (Proc. Insin elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, pp. 599-602.)
621.372.8.001.2 351
An Application of Sturm-Liouville Theory to a Class of Two-Part BoundaryValue Problems.-S. N. Karp. (Proc. Camb. phil. Soc., April 1957, Vol. 53, Part 2, pp. 368-381.) " A simple solution of a general problem involving a bifurcated waveguide is presented. The purpose of the work is to explain a new and simple method of solving such problems and to exhibit an organic connexion between Sturm-Liouville theory and the theory of two-part boundaryvalue problems."
621.372.8.002.1

352
Waveguide Design for Die-Casting.P. Humphreys. (Electronic Radio Engr, Dec. 1957, Vol. 34, No. 12, pp. 441-447.) " This article explains how components which have been designed in normal rectangular waveguide may be easily modified on a theoretical basis to make them suitable for die-casting manufacturing methods. The theory is applicable to cases where the waveguide can be manufactured by splitting it along the length of the central E-plane and the unit is therefore cast in two halves."

### 621.372.822

353
Theory of the Helical Waveguide of Rectangular Cross-Section.-R. A. Waldron. (J. Brit. Instn Radio Engrs, Oct. 1957, Vol. 17, No. 10, pp. 577-592.) A mathematical treatment of the properties of a helical waveguide, regarded as an equivalent circular waveguide in which points differing in azimuth by $2 \pi$ radians are not equivalent.

### 621.372.832.6

354
A New Form of Hybrid Junction for Microwave Frequencies.-L. Young: P. D. Lomer \& J. W. Crompton. (Proc. Instn elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, p. 586.) Comment on 2339 of 1957 and authors' reply.

### 621.372.832.8

355
A Broad-Band Microwave Circulator. -E. A. Ohm. (Bell. Lab. Rec., Aug. 1957, Vol. 35, No. 8, pp. 293-297.) A device for routing microwave energy over a variety of waveguide transmission paths is described. By surrounding the ferrite insert with material of high dielectric constant the rotation/frequency characteristic is flattened and a wide-band device is obtained.
621.372.852.22 356

Wide-Band Isolator at $4 \mathbf{k M c} / \mathrm{s}$. -S. Kawazu, K. Matsumaru \& H. Ishii. (Rep. elect. Commun. Lab., Japan, March 1957, Vol. 5, No. 3, pp. 15-17.) The isolator which incorporates a magnetized ferrite insert covered by dielectric material has forward and reverse losses of 1.5 and 20 dB respectively over a $530-\mathrm{Mc} / \mathrm{s}$ band.
621.396.677: 621.372.092:621.318.134 357

A New Technique in Ferrite Phase Shifting for Beam Scanning of Microwave Antennas.-Reggia \& Spencer. (See 387.)
621.396.677: 621.396.11

Aerial/Propagation Mismatch.-R. J. Hitchcock. (Wireless World, Dec. 1957, Vol. 63, No. 12, pp. 599-602.) Many point-to-point h.f. circuits in operation are inefficient because aerial systems are not matched to the predominant modes of propagation. Recent investigations show that on medium- and long-distance circuits low angles of arrival predominate both by day and night. Appropriate improvements to aerials and sites are discussed.

### 621.396.677.3

359
The Effect of the Mutual Impedance due to the Neighbouring Elements on the Driving-Point Impedances of a Linear Array.-R. Parthasarathy. ( $J$ Instn Telecommun. Engrs, India, June 1957, Vol. 3, No. 3, pp. 242-247.) The driving point impedance of a four-element array is independent of the beam direction, provided the element spacing is not closer than $\lambda / 4$.
621.396.677.3

The New Aerial Installation of the Vatican Short-Wave Broadcasting Service at Santa Maria di Galeria.-W Berndt. (Telefunken Ztg, Sept. 1957, Vol. 30, No. 117, pp. 174-184. English summary, p. 217.) Facilities are provided for changing the angles of main radiation in both the horizontal and vertical planes.
621.396.677.3: 534.23

361
Theory of Time-Averaged-Product Arrays.-Berman \& Clay. (See 336.)
621.396.677.5

The 'Quad' Aerial.-F. B. Singleton (Wireless World, Dec. 1957, Vol. 63, No. 12, pp. 607-608.) The advantages of these aerials for indoor use on bands I and II are outlined.
621.396.677.833.1

363
An Experimental Wide-Band Parabolic Aerial for the $2000-\mathrm{Mc} / \mathrm{s}$ Band. N. Ganapathy \& P. E. G. T. Hopkins. (Marconi Rev., 4th Quarter 1957, Vol. 20, No. 127, pp. 134-152.) A 10-ft-diameter horn-fed paraboloid, for multichannel links, combining high gain with good impedance match over a wide band is described; performance data are quoted.

## AUTOMATIC COMPUTERS

681.142

Odd Binary Asynchronous Counters. -J. F. Robertson. (Trans. Inst. Radio Engrs, March 1956, Vol. EC-5, No. 1, pp. 12-15. Abstract, Proc. Inst. Radio Engrs, June 1956, Vol. 44, No. 6, Part 1, p. 832.)
681.142

365
A One-Microsecond Adder using OneMegacycle Circuitry.-A. Weinberger \& J. L. Smith. (Trans. Inst. Radio Engrs, June 1956, Vol. EC-5, No.2, pp. 65-73. Abstract, Proc. Inst. Radio Engrs, Aug. 1956, Vol. 44, No. 8, p. 1083.)
681.142

High-Speed Computer stores 2-5 Megabits.-W. N. Papian. (Electronics, 1st Oct. 1957, Vol. 30, No. 10, pp. 162-167.) Design and performance details of the Lincoln TX-2 computer are given.
681.142

367
An Iterative Analogue Computer for Use with Resistance Network Analogues.-I. C. Hutcheon. (Brit. J. appl. Phys., Sept. 1957, Vol. 8, No. 9, pp. 370-373.)

### 681.142

368
Circuitry and Characteristics of a Repeating Electronic Analogue Com-puter.-W. Dhen. (Elektrotech. Z., Edn A, 11 th July 1957, Vol. 78, No. 14, pp. 490494.) Description of a computer for solving engineering problems. A hyperbolic-field tube [2924 of 1956 (Schmidt)] is used as multiplier.

### 681.142

369
The Error Effect of the Operation Amplifier in Analogue Computers.-A. Kley. (Telefunken Ztg, June 1957, Vol. 30, No. 116, pp. 136-141. English summary, p. 153.) The various errors and their sources are discussed and some methods of automatic correction are described.
681.142 370
A Multiplier based on the TwoParabola Method.-W. Schneider. (Telefunken Ztg, June 1957, Vol. 30, No. 116, pp. 141-145. English summary, p. 153.) The method of operation is described and the accuracy obtainable is shown by some examples of calculations.

### 681.142 : 538.244

371
The Utilization of Domain Wall Viscosity in Data-Handling Devices.V. L. Newhouse. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp. 1484-1492.)
681.142: 621.314.7: 621.375.4

372
Transistors in Current - Analogue Computing.-B. P. Kerfoot. (Trans. Inst. Radio Engrs, June 1956, Vol. EC-5, No. 2, pp. 86-93.) A comparison of variablecurrent and variable-voltage analogue computing techniques shows that transistors are particularly suitable for the former. Lowpower low-frequency transistors in directcoupled amplifiers which may be used in computers are described.
681.142 : 621.318 .57

373
Electric Correlators.-K. Steinbuch \& H. Endres. (Nachrichtentech. Z., June 1957, Vol. .10, No. 6, pp. 277-287.) Typical applications of electric correlating devices are discussed, and the operation of various types of these is described. Details are given of a static-type translator using transistors and crystal diodes as nonlinear switching elements.
681.142 : 621.374 .33

374
A Time-Division Multiplier.-M. L. Lilamand. (Trans. Inst. Radio Engrs, March 1956, Vol. EC-5, No. 1, pp. 26-34. Abstract, Proc. Inst. Radio Engrs, June 1956, Vol. 44, No. 6, Part 1, p. 832.)
681.142: 621.385.5

375
Analogue Multipliers and Squarers using a Multigrid Modulator.-R. L. Sydnor, T. R. O'Meara \& J. Strathman. ( Trans. Inst. Radio Engrs, June 1956, Vol. EC-5, No. 2, pp. 82-85. Abstract, Proc. Inst. Radio Engrs, Aug. 1956, Vol. 44, No. 8, p. 1084.)
681.142: 621.395.625.3

376
A Small Coincident-Current Magnetic Memory.-W. J. Bartik \& T. H. Bonn. (Trans. Inst. Radio Engrs, June 1956, Vol. EC-5, No. 2, pp. 73-78. Abstract, Proc. Inst. Radio Engrs, Aug. 1956, Vol. 44, No. 8, p. 1083.)
621.3 .049 .75
The Role of Printed Wiring in High Fidelity.-N. H. Crowhurst. (Audio, May 1957, Vol. 41, No. 5, pp. 17-20 . . 78.) Thie advantages of printed-wiring techniques are summarized.
621.314 .22

378
A Design Method for Wide-Band Balanced and Screened Transformers in the Range $0 \cdot 1-200 \mathrm{Mc} / \mathrm{s}$.-M. M. Maddox \& J. D. Storer. (Electronic Engng, Nov. 1957, Vol. 29, No. 357, pp. 524-531.) Leakages and winding capacitances are accurately and independently controlled, and a high degree of winding balance is attained with an insertion loss of about 0.5 dB .

### 621.314 .22

379
Simplified Pulse Transformer Design.-J. H. Smith. (Electronic Engng, Nov. 1957, Vol. 29, No. 357, pp. 551-555.) An outline of design techniques for low- and high-power pulse transformers.

### 621.316.726: 621.396.62

380
The Frequency-Lock A.F.C. Circuit. -R. Leek. (Proc. Instn elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, pp. 587-597.) Noise-free operation of the system is analysed and its performance at low signal/noise ratios is considered. A theory of the system operation under the latter conditions is developed from an examination of the tracking errors resulting from noise and changes in signal frequency. Practical results obtained are in agreement with this theory.

### 621.318 .57

381
A Novel Electronic TransmitReceive Switch.-A. Sabaroff. (QST, June 1957, Vol. 41, No. 6, pp. 24-25 . . 162.) A Type 6AH6 valve, capable of withstanding 250 V between grid and cathode, isolates the receiver from the transmitter tank circuit.

### 621.318 .57 : 621.314 .7

382
Stabilization of Current-Operated Transistor Switching Circuits.-N. W. Morgalla. (A.T.E. J., July 1957, Vol. 13,

No. 3, pp. 192-200.) A method is given for calculating the parameters of simple compensating circuits.
621.318.57: 621.314.7: 621.395.3 383

The Transistor as a Speech-Path Switch.-R. C. N. Mundy. (A.T.E. J., July 1957, Vol. 13, No. 3, pp. 227-235.) The suitability of transistors is discussed and some methods of using them for this purpose in telephone systems are described.
621.318.57.01: 681.142

384
Complexity in Electronic Switching Circuits.-D. E. Muller. (Trans. Inst. Radio Engrs, March 1956, Vol. EC-5, No. 1, pp. 15-17. Abstract, Proc. Inst. Radio Engrs, June 1956, Vol. 44, No. 6, Part 1, p. 832.)

### 621.37 .049 : $[537.3+538.6$

385
Future Circuit Aspects of Solid-State Phenomena.-E. W. Herold. (Proc. Inst. Radio Engrs, Nov. 19957, Vol. 45, No. 11, pp. 1463-1474.) Several phenomena such as superconductivity, molecular amplification, magnetic effects in semiconductors, and the nonlinear capacitance of $p-n$ junctions, are discussed from the point of view of the circuit designer. New devices will, to an increasing extent, be based on controlled inhomogeneity.

### 621.372 : 538.565.5

386
The Influence of Electromagnetically Coupled Systems.-W. Dahlke. (Arch. elekt. Ubertragung, June 1957, Vol. 11, No. 6, pp. 231-238.) Compound systems consisting of a primary electromagnetically coupled to a secondary system are considered. The equations obtained are applied to examples of magnetic coupling and a conducting diode.
621.372.092: 621.318.134: 621.396.677 387

A New Technique in Ferrite Phase Shifting for Beam Scanuing of Microwave Antennas.-F. Reggia \& E. G. Spencer. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp. 1510-1517.) In the device described a longitudinal magnetic field is applied to a ferrite rod in a rectangular waveguide excited in the $\mathrm{TE}_{10}$ mode. Phase shifts of over $250^{\circ} / \mathrm{in}$. and variations in transmitted power of less than $\pm 0.2 \mathrm{~dB}$ have been obtained with a field of 60 oersteds. See also 44 of 1957 (Scharfman).

### 621.372.412.011.2

388
Computation of Crystal Admittance. -W. J. Lucas \& P. B. Barber. (Electronic Radio Engr, Dec. 1957, Vol. 34, No. 12, pp. 454-458.) The results of a digital-computer program designed to calculate the admittance of a coaxial crystal for various values of video resistance, spreading resistance and barrier capacitance over the range $2-18$ $\mathrm{kMc} / \mathrm{s}$ are given. Comparisons with available measurements are made.
621.372.413

389
Method of Obtaining Pressure- and Temperature-Insensitive Microwave Cavity Resonators.-C. M. Crain \& C. E. Williams. (Rev. sci. Instrum., Aug. 1957, Vol. 28, No. 8, pp. 620-623.) Methods using invar walls with steel or brass end plates for $\mathrm{TE}_{011}$ cavities are unsatisfactory due to hysteresis effects. Improved techniques
are described for fixed-frequency resonators which have temperature coefficients less than $\pm 0.2$ in $10^{6}$ per ${ }^{\circ} \mathrm{C}$. The pressure coefficient is less than 0.003 in $10^{8}$ per millibar.
621.372.413: 621.318.134

Retardation Effects Caused by Ferrite Sample Size on the Frequency Shift of a Resonant Cavity.-J. E. Tompkins \& E. G. Spencer. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9, pp. 969-974.) Expressions are derived, using perturbation theory, for the frequency shift of a circularly polarized resonant microwave cavity due to insertion of a small ferrite sample.

### 621.372 .51

391
Simplified Design of ImpedanceMatching Networks. - G. Grammer. (QST, March-May 1957, Vol. 41, Nos. 3-5, pp. 38-42, 32-35 \& 29-34.) A step-by-step method of impedance transformation is described. The formation of $\Pi$ and $T$ networks from the basic $L$ section and some complex matching networks for particular applications are discussed.
621.372 .543 .2

Super Selectivity with Crystals.R. F. Burns. (Radio TV News, July 1957, Vol. 58, No. 1, pp. 52-53 . . 132.) Constructional details of a lattice-type i.f. filter with two crystals; the response curve is symmetrical.
621.372.56.029.6: 621.372.8 393
A Frequency-Independent Microwave Attenuator with Largely Constant Phase Shift.-R. Steinhart. (Nachrichtentech. Z., June 1957, Vol. 10, No. 6, pp. 294-297.) A waveguide attenuator of the rotary-vane type is described and calibration and error curves are given. Close agreement of measured attenuation with theoretical values was obtained in attenuators for the range $3300-4200 \mathrm{Mc} / \mathrm{s}$.

### 621.372 .57

394
The Transactor.-A. W. Keen. (Electronic Radio Engr, Dec. 1957, Vol. 34, No. 12, pp. 459-461.) The two-terminal constantcurrent and constant-voltage generators used in equivalent circuits of active networks are replaced by transmission-type active elcments called transactors. The relations between variants of this element are established.
621.372.6: 621.3.018.1

395
Theory of Two-Phase Networks.-G. Wunsch. (Nachr Tech., May 1957, Vol. 7, No. 5, pp. 200 205.) Phase-splitting networks as used in s.s.b. modulation systems are discussed and calculations by approximation methods are described.
621.373.4.029.4: 621.396.963.5

396
Phase-Shift Oscillator Indicates Radar Range.-R. C. Barritt. (Electronics, lst Oct. 1957, Vol. 30, No. 10, pp. 160-161.) Firing range information is conveyed by a variable a.f. note.

### 621.373.4.029.64

397
High-Order Harmonics for $X$ Band Oscillator Stabilization.-M. C. Thompson \& J. V. Catcora. (Rev. sci. Instrum., Aug. 1957, Vol. 28, No. 8, p. 656.) A simplified
phase-locking stabilization technique for microwave oscillators. Harmonic orders up to about 300 are used.

### 621.373 .421

398
The Simultaneous Generation of Two Oscillations in One Oscillator and the Stability of the Difference Frequency.W. Feist. (Nachrichtentech. Z., May 1957, Vol. 10, No. 5, pp. 215-222.) The operating conditions are determined which are required for the simultancous generation of two different frequencies in a valve feedback oscillator [see also 80 of 1952 (Herzog)]. Experimental resuilts are discussed.

### 621.373 .43

399
'Grid-Diode' Sawtooth Generator.T. A. Mendes. (Wireless World, Dec. 1957, Vol. 63, No. 12, pp. 603-606.) Description of a simple timebase circuit with wide frequency range
621.373 .5 : 537.311 .33 : 538.632

400
Experimental and Theoretical Investtigation of Semiconductor Hall-Effect Generators.-Strutt \& Sun. (See 4.92.)

### 621.373 .52

Silicon Transistor Crystal Oscillators have High Temperature Stability.E. G. Homer. (Electronics, 1st Oct. 1957, Vol. 30, No. 10, pp. 218-222.) Outline of circuit design considerations and discussion of experimental results.

### 621.374 .32

402
Difference Counters.-A. F. Fisclımann. (Electronic Engng, Nov. 1957, Vol. 29, No.357, pp. 546-550.) Two examples are given with maximum counting rates (a) $2 \times 10^{5}$ pulses $/ \mathrm{s}$ and (b) $10^{7}$ pulses/s. The design of a decimal difference counter is outlined.

### 621.375.2.024

403
Direct-Coupled Amplifiers.-D. J. R. Martin. (Electronic Radio Engr, Dec. 1957, Vol. 34, No. 12, pp. 438-441.) "A method is described of artificially matching valves to obtain improved mutual compensation for the effects of normal heater-supply voltage changes. Adjustment is easier than selecting naturally matched pairs of valves, and considerably better balance is oblained."

### 621.375.221.029.62

404
A 70-Mc/s I.F. Amplifier for WideBand Microwave Links.-L. J. Herbst \& G. R. Shoubridge. (A.T.E. J., July 1957, Vol. 13, No. 3, pp. 184-191.)

### 621.375 .4 <br> 405

Direct-Coupled Amplifiers with Junction Transistors.-S. Giustini. Alta Frequenza, Aug. 1957, Vol. 26, No. 4, pp. 196-225.) A balanced d.c. amplifier circuit is analysed and the theory of its operation is developed on the basis of the work by Ebers \& Moll (884 of 1955). The problem of balancing the circuit with ideal and with commercial-type transistors is considered and practical design formulae are derived.
621.375.9: 538.569.4

406
Masers and Reactance AmplifiersBasic Power Relations.-B. Salzberg. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp. 1544 1545.) Au alternative
derivation, based on circuit theory, o the expressions of Manley \& Rowe (2988 of 1956). The power relations involve only the source and load frequencies and are independent of the specific characteristics of the nonlinear device.
621.375.9: 538.569.4

### 621.317.3.029.64

Maser Noise Measurement.-Helmer (See 547.)

### 621.375.9.029.63/.64:538.221 <br> 408

New Ferrite Microwave Amplifier. -(Bell Lab. Rec., Aug. 1957, Vol. 35, No. 8, pp. 316 317.) An experimental solid-state amplifier using a ferrite material as the active element is described. The device is suitable as an amplifier of very weak microwave signals. See also 3076 of 1957 (Suhl).
621.375.9.029.64:538.569.4

## 409

The Reaction Field and its Use in Some Solid-State Amplifiers.-P. W. Anderson. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9, pp. 1049-1053.) The theory of the maser is presented in terms of the radiation 'reaction' field produced in a cavity or waveguide by the presence of the electromagnetic moment of the sample being investigated. Two amplifiers are discussed which use the reaction field in different ways from the usual solid-state maser.

### 621.376.32: 621.314 .63

The PN Junction on a Variable Reactance Device for F.M. Production.
D. C. Brown \& F. Henderson. (Electronic Engng, Nov. 1957, Vol. 29, No. 357, pp. 556-557.) A transistor modulator for a $10-\mathrm{Mc} / \mathrm{s}$ carrier frequency is described which gives good f.m. with negligible a.m. $0 \cdot 15-\mathrm{V}$ change in modulating signal produces a deviation of $100 \mathrm{kc} / \mathrm{s}$.

## GENERAL PHYSICS

### 537.226 .2

411
The Influence of a Strong Magnetic Field on the Dielectric Constant of a Diamagnetic Fluid.-A. D. Buckingham, (Proc. phys. Soc., 1st Aug. 1957, Vol. 70, No. 452B, pp. 753-760.)

### 537.226 .2

412
Formulae for Dielectric Constant of Mixtures.-J. A. Reynolds \& J. M. Hough. (Proc. phys. Soc., 1st Aug. 1957, Vol. 70, No. 452B, pp. 769-775.) 15 formulae are tabulated with references and shown to be special cases of a general fundamental formula. An exception is the Lichtenecker type of formula, possibly owing to incorrect assumptions.

### 537.311

413
The Second-Order Effect of Free Electrons on Lattice Conduction.-I. C. Pyle. (Proc. Camb. phil. Soc., April 1957, Vol. 53, Part 2, pp. 508-513.) " Secondorder perturbation theory, in conjunction with the usual treatment of electron-phonon
interaction, allows us to calculate the correction to the first-order result for the scattering of phonons by electrons. It is shown that the second-order term is much smaller, and therefore negligible. This justifies the use of the first-order theory in the treatment of the interaction in metals and semiconductors." See also 2017 of 1956 (Ziman).
537.311 .1 414
A Method of Calculation of Electrical Conductivity.-H. Nakano. (Progr. theor. Phys., Feb. 1957, Vol. 17, No. 2, pp. $145-$ 161.) Using relaxation theory a general solution is obtained for the electric current density ; irreversibility is then introduced so that practical cases may be considered. A perturbation approximation gives the same result as that based on the Bloch theory.

### 537.312.62

415
A Note on the Energy-Gap Model of Superconductivity.-M. J. Buckingham. (Nuovo Cim., 1st June 1957, Vol. 5, No. 6, pp. 1763-1765. In English.)

### 537.312.62

416
Gauge Invariance and the Energy-Gap Model of Superconductivity.-J. Bardeen. (Nuovo Cim., 1st June 1957, Vol. 5, No. 6, pp. 1766-1768. In English.) See also 415 above.

### 537.321

417
On the Elementary Theory of Thermoelectric Phenomena.-R. Stratton. (Brit. J. appl. Phys., Aug. 1957, Vol. 8, No. 8, pp. 315-321.) All the relations between the thermoelectric parameters are deduced from physical properties rather than by means of mathematical transformations. The sources of the heat and e.m.f. developed are indicated.
537.525: 538.56

418
The Plasma Resonator.-A. Dattner. (Ericsson Tech., 1957, Vol. 13, No. 2, pp. 309-350.) The interaction between an ionized gas column and an electromagnetic wave in a waveguide is studied at $\lambda=6 \mathrm{~cm}$. Effects examined include the influence of the discharge current, gas collisions, decay times of electron density, and modulation of the r.f. power.

### 537.525: 621.387.032.435.4

419
New Effects of an Auxiliary Electrode on a Discharge at Low Pressure. Thong Saw Pak. (J. Electronics Control, Nov. 1957, Vol. 3, No. 5, pp. 471 480.) An auxiliary electrode close to the cathode provides a means of sensitive control of the discharge. Optimum operational conditions were found for a range of discharge parameters. Low-frequency noise may be suppressed by an electrode of wire gauze.

### 537.533.8

 420Theory of Secondary Emission.R. G. Lye \& A. J. Dekker. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, pp. 977-981.) The elementary theory of secondary electron emission has been generalized and modified to incorporate results of recent measurements of the range/energy relation and the dissipation of energy by slow electrons in solids. These modifications give consider-
ably improved agreement between the theoretical and experimental 'universal' reduced yield curves.

## 538.1

 421'Satellite-Electron' Theory of Ferromagnetism, Antiferromagnetism and Related Phenomena.-L. Singh. (Naturwissenschaften, Aug. 1957, Vol. 44, No. 15, pp. 417-418. In English.) A theory based on classical concepts is developed to show the electronic nature of ferromagnetism. Magnetic properties of transition-metal oxides are briefly discussed.

### 538.11: 538.124

422
A Note on the Ground State of Anti-ferromagnetism.-H. Taketa \& T. Nakamura. (J. phys. Soc. Japan, Sept. 1956, Vol. 11, No. 9, pp. 919-923.) Kasteleijn's method (2199 of 1952) of obtaining the lowest energy state is generalized for the cases of two- and three-dimensional lattices.

## 538.3: 52

423
On the Reflection and Refraction of Magnetohydrodynamic Waves.-S. Prakash \& J. N. Tandon. (Proc. nat. Inst. Sci. India, Part A, 26 th July 1957, Vol. 23, No. 4, pp. 264-273.)
538.566: 535.42

424
Asympiotic Formulas for Diffraction by Parabolic Surfaces.-H. Hochstadt. (Commun. pure appl. Math., Aug. 1957, Vol.10, No. 3, pp. 311-329.) Asymptotic solutions to the wave equation are found at a boundary consisting of a paraboloid of revolution or a parabolic cylinder. The results are applied to the reflection, at such surfaces, of incoming plane waves or divergent waves from a point or line on the axis of the surface.
538.569 .4

425
Double Modulation System for Narrowing Electron Resonance Absorption Lines.-R. R. Unterberger, J. L. Garcia de Quevedo \& A. E. Stoddard. (Rev. sci. Instrum., Aug. 1957, Vol. 28, No. 8, pp. 616-619.) A method for observing electron-resonance absorption on an oscilloscope screen by modulating both the magnetic field and the klystron frequency. The apparent line width can be reduced by a factor of 17 relative to the true line width.
538.569.4

426
Microwave Studies of the Internal Motion and the Structure of Methyl Amine.-T. Nishikawa. (J. phys. Soc. Japan, June 1957, Vol. 12, No. 6, pp. 668680.)
538.569.4

427
Potential Barrier and Molecular Structure of Methyl Mercaptan from its Microwave Spectra.-T. Kojima \& T. Nishikawa. (J. phys. Soc. Japan, June 1957, Vol. 12, No. 6, pp. 680-686.)

### 538.569.4

428
Microwave Spectrum of BrCN and Dependence of Quadrupole Coupling Constant on the Vibrational State.-T. Oka \& H. Hirakawa. (J. phys. Soc. Japan, July 1957, Vol. 12, No. 7, pp. 820-823.)
538.569.4: 621.375.9

429
Proposal for a Nuclear Quadrupole Maser.-R. Braunstein. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, pp. 1195-1196.) It is suggested that certain substances exhibiting pure quadrupole transitions have the requisite properties for maser operation. The differences between masers based on these substances and on paramagnetic solids are discussed.
538.569.4 : 621.375.9.029.6

430
Fluctuations in Amplification of Quanta with Application to Maser Amplifiers.-K. Shimoda, H. Takahasi \& C. H. Townes. (J. phys. Soc. Japan, June 1957, Vol. 12, No. 6, pp. 686-700.) Expressions for the probability distribution of quanta, for the average values and for the fractional fluctuation are developed and applied to maser-type amplifiers.
538.569.4: 621.375.9.029.64

The Reaction Field and its Use in Some Solid-State Amplifiers.-Anderson. (See 409.)
538.615

432
Radio-Frequency Zeeman Effect in $\mathbf{O}_{2}$ - J. M. Hendrie \& P. Kusch. (Phys. Rev., Ist Aug. 1957, Vol. 107, No. 3, pp. 716-723.) By the molecular-beam magneticresonance method the ratio of the $g$-value of the rotational magnetic moment to that of the electron-spin moment is found to be $(6.08 \pm 0.74) \times 10^{-5}$; the ratio of the $g$ value of the unpaired-electron spin moments in $\mathrm{O}_{2}$ to that of the free-electron spin moment is $1-(190 \pm 13) \times 10^{-6}$.
539.16.08: 621.372.413

433
The Cloud Chamber.-(Electronic Radio Engr, Dec. 1957, Vol. 34, No. 12, pp. 447450.) The theory and application of the Wilson cloud chamber are outlined, and its modification by Gabor \& Hampton (Nature, Lond., 12th Oct. 1957, Vol. 180, No. 4589, pp. 746-749) is briefly described.

GEOPHYSICAL AND
EXTRATERRESTRIAL PHENOMENA

### 523.16: 523.4

434
Sources of Radio Noise on the Planet Jupiter.-C. H. Barrow, T. D. Carr \& A. G. Smith. (Nature, Lond., 24th Aug. 1957, Vol. 180, No. 4582, p. 381.) Daily record's made from 31st December 1956 to 8th March 1957 at Gainesville, Florida, at $18 \mathrm{Mc} / \mathrm{s}$ suggest that there are two localized sources on Jupiter and that Jupiter is surrounded by an ionosphere of electron density $10^{8} / \mathrm{cm}^{3}$, i.e. comparable with that of the earth's ionosphere. See 2710 of 1956 (Shain).
523.16: 523.64

435
Radio Emission from the Comet 1956 h.-H. G. Müller, W. Priester \& G. Fischer. (Naturwissenschaften, July 1957, Vol. 44, No. 14, pp. 392-393.) Report of observations carried out at the radio observatory Stockert. illations as Caused by Interstellar Particles Entering the Ionosphere: Part 3-The Kind, Number and Apparent Radiant of the Incoming Particles. -G. A. Harrower. (Canad. J. Phys., July 1957, Vol: 35, No. 7, pp. 792-798.) Discussion of results given earlier ( 106 of January) indicates that the interstellar particles must be hydrogen atoms.

## $523: 7$

437
The Proportion of Umbra in Large Sunspots, 1878-1954.-A. W. F. Edwards. (Observatory, April 1957, Vol. 77, No. 897, pp. 69-70.) The ratio of umbral area to whole-spot area is evaluated and shown to vary significantly with the position of the sunspot in the solar cycle.

## 523.7: 621.396.822.029.66 <br> 438 <br> Detection of Submillimetre Solar

 Radiation.-H. A. Gebbie. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, pp. 1194 1195.) Preliminary results are presented which indicate regions of transmission in the wavelength range $1 \mathrm{~mm}-300 \mu$.
### 523.72 : 621.396 .822

439
Short Time Transients in Solar Noise. -T. de Groot. (Nature, Lond., 24th Aug. 1957, Vol. 180, No. 4582, p. 382.) Histograms have been made from observations at Dwingeloo, Holland, at $400 \mathrm{Mc} / \mathrm{s}$. Reber's theory (see 1637 of 1955) that there is a linear relation between wavelength and duration of 'pips' is not confirmed at this frequency.

### 523.746

440
A Review of Recent Investigations into Sunspot Cycles.-N. A. Huttly. (Marconi Rev., 4th Quarter 1957, Vol. 20, No. 127, pp. 117-129.) Summaries of, and comments on, selected published papers and C.C.I.R. documents relating to predictions of solar activity for use in ionospheric work.

### 523.75

441
Occultation of a Radio Source by the Solar Corona.-O. B. Slee. (Observatory, Dec. 1956, Vol. 76, No. 895, pp. 228-231.) Measurements of radio-noise flux from Taurus-A, when its angular separation from the sun is very small, suggest.that partial wide-angle scattering has occurred due to electron density irregularities in the solar corona.

### 523.75

442
A Solar Flare on 1956 November 7.P. A. Wayman. (Observatory, Feb. 1957, Vol. 77, No. 896, pp. 24-26.) Visual and radio observations during the flare are presented. Anomalies in the radio observations are accounted for by small regions of the flare remaining enhanced for several hours after the main effect had subsided.
523.78

Centimetre-Wave Observations of the Solar Eclipse of 1954 June 30.-J. S. Hey \& V. A. Hughes. (Observatory, Dec. 1956, Vol. 76, No. 895, pp. 226-228.) Radiation measurements at $10.5 \mathrm{~cm} \lambda$ disclose an ellipticity in the brightness distribution of the sun's disk with the greatest extent in the equatorial plane.

Proper and Improper Use of Statistics in Geophysics.-B. Kinsman. (Tellus, Aug. 1957, Vol. 9, No. 3, pp. 408-418.) A discussion of some of the peculiarities of the geophysical sciences together with their implications for statistical methods, particularly for the correlation coefficient, is given. The discussion is illustrated by an analysis of a recently published paper. In conclusion some advice on the use of correlations is offered.

### 550.384

 445Hydromagnetics and the Earth's Inner Core.-G. H. A. Cole. (Observatory, Feb. 1957, Vol. 77, No. 896, pp. 17-19.) It is suggested that the terrestrial magnetic field is produced in an inner liquid core permeated by a magnetic field of $\approx 10^{5} \mathrm{G}$. Secondary motions, partly hydromagnetic, occur in an outer surrounding liquid region and the field emerging from the complete core is the small field measured at the earth's surface.

### 550.385.1: 523.7

446
Method of Magnetic-Storm Forecasting from the Activities of Flares Accompanied by the Solar Radio Noise Outbursts.-K. Sinno. (J. Radio Res. Labs, Japan, July 1957, Vol. 4, No. 17, pp. 267276.) A statistical examination has been made of the occurrence of magnetic storms, solar flares and radio noise outbursts on $200 \mathrm{Mc} / \mathrm{s}$. The correlations discovered are applied to the problem of forecasting magnetic storms during the I.G.Y.

### 550.389.2: 551.510.535 (54)

447
Ionospheric Studies in India during the International Geophysical Year.K. R. Ramanathan. ( $J$. Instn Telecommun. Engrs, India, June 1957, Vol. 3, No. 3, pp. 193-197.)
550.389.2: 621.396.11

448
Propagation and the International Geophysical Year.-G. W. Slack. (R.S.G.B. Bull., July 1957, Vol. 33, No. 1, pp. 8-11.) Summary of phenomena which affect h.f. and v.h.f. propagation. Some methods of observation are suggested to the radio amateur.

### 550.389.2: 629.19

449
Artificial Satellites of the Earth.(Wireless World, Dec. 1957, Vol. 63, No. 12, pp. 574-578.) Extracts are given from Radio, Mosk. published before the launching of the U.S.S.R. satellites [see e.g. 3860 of 1957 (Vakhnin)] and results of observations made at various stations in the U.K. are summarized.
550.389.2 : 629.19: 681.142

450
Tracking the Man-Made Satellite.-M. Gunther. (Radio TV News, July 1957, Vol. 58, No. 1, pp. 31-33.) An outline of the preparations for launching and observing the U.S. satellite, including the use of an electronic computer for calculating the orbit from observational data.
551.501.8: 621.396.11

451
The Use of Surface Weather Observations to Predict the Total

Atmospheric Bending of Radio Rays at Small Elevation Angles.-Bean \& Cahoon. (See 578.)

### 551.508 .7

452
The Detection and Measurement of Water Droplets.-H. F. Liddell \& N. W. Wootten. (Quart. J. R. met. Soc., April 1957, Vol. 83, No. 356, pp. 263-266.) A method of obtaining a permanent record of drop size is described; it can be used for droplets of less than $1 \mu$ diameter.

### 551.510 .5

453
The Threefold Structure of the Atmosphere and the Characteristics of the Tropopause.-F. Defant \& H. Taba. (Tellus, Aug. 1957, Vol. 9, No. 3, pp. 259 274.) The atmosphere in the northern hemisphere is divisible into three regions, north of the polar-front jet, south of the subtropical jet and the region between the jets. Each region has a typical vertical temperature structure in the stratosphere and troposphere and a characteristic tropopause height.

### 551.510 .535

454
The Effect of the Equatorial Electrojet on the Ionospheric $E_{s}$ and $F_{2}$ Layers. -N. J. Skinner \& R. W. Wright. (Proc. phys. Soc., Ist Sept. 1957, Vol. 70, No. 453B, pp. 833-839.) The occurrence of low values of $f \mathrm{E}_{s}$ at Ibadan is correlated with variations in the horizontal and vertical components of the earth's field, and with $\mathrm{F}_{2}$-layer parameters. An immediate relation is indicated between the electrojet, the production of equatorial $\mathrm{E}_{s}$, and vertical drifts in the $\mathrm{F}_{2}$ layer.
551.510.535

455
Dynamical Structure of the Ionospheric $\mathbf{F}_{2}$ Layer.-T. Shimazaki. ( $J$. Radio Res. Labs, Japan, July 1957, Vol. 4, No. 17, pp. 309-332.) Formulae giving diffusion velocity and its divergence are derived for the electron-ion gas in the ionosphere, on the assumption of a linear temperature gradient. The change in electron density distribution is then calculated, using these formulae, for different models of the ionosphere. Comparisons of the calculated and observed changes in the $\mathrm{F}_{2}$ layer show that Bradbury's rather than Chapman's theory is more appropriate.

### 551.510 .535 (52)

456
On the Occurrence of the $F_{1.5}$ Layer in Japan: Part 1.-I. Kasuya. (J. Radio Res. Labs, Japan, July 1957, Vol. 4, No. 17, pp. 291-300.) A statistical analysis based on vertical incidence soundings over a sunspot cycle shows annual seasonal and diurnal variations. Good correlation is demonstrated between frequency of occurrence and sunspot number.

## $551.524 .7+551.571 .7$

457
Some Further Observations from Aircraft of Frost Point and Temperature up to 50000 ft . - N. C. Helliwell, J. K. Mackenzie \& M. J. Kerley. (Quart. J. R. met. Soc., April 1957, Vol. 83, No. 356, pp. 257-262.) Measurements at various altitudes taken in 46 flights over Southern England in 1955 are tabulated. Good general agreement is obtained with 1954 measurements.

Variation with Height of Rainfall below the Melting Level.-W. G. Harper. (Quart. J. R. met. Soc., July 1957, Vol. 83, No. 357, pp. 368-371.) 3-cm radar measurements in warm-front conditions suggest that there is uniformity of drop size distribution and rate of rainfall with height once meeting is complete and terminal velocity has been attained.
551.59 459
On a Special Aspect of the Condensation Process and its Importance in the Treatment of Cloud Particle Growth.C. Rooth. (Tellus, Aug. 1957, Vol. 9, No. 3, pp. 372-377.) The distribution of water vapour around a droplet depends upon the ratio of droplet size to a factor determined by the equilibrium rate of exchange of molecules between the water surface and the water vapour.
551.59

460
Electric Charge Separation in Subfreezing Cumuli.-S. Twomey. (Tellus, Aug. 1957, Vol. 9, No. 3, pp. 384-393.) A theory of the electrification of thunderclouds on charge separation occurring when supercooled droplets impinge on ice particles The theory can explain observed charge separations without assuming the presence of large hailstones.
551.594.21

461
The Measurement of World-Wide Thunderstorm Activity at a Single Locality.-G. A. Isted. (Marconi Rev., 4th Quarter 1957, Vol. 20, No. 127, pp. 130132.) Counts of atmospheric impulses received in England in the $0 \cdot 3-12 \mathrm{kc} / \mathrm{s}$ band are found to be similar to records of integrated noise in California in the band $25-130 \mathrm{c} / \mathrm{s}$ [see 2070 of 1956 (Holzer \& Deal)]. It is inferred that world-wide thunderstorm activity was recorded in both experiments.

### 551.594.221

462
Preliminary Discharge Processes in Lightning Flashes to Ground.-N. D. Clarence \& D. J. Malan. (Quart. J. R. met. Soc., April 1957, Vol. 83, No. 356, pp. 161172.) The first return stroke is usually preceded by three successive and distinct discharge processes lasting several hundred milliseconds. The characteristics of the field changes in these preliminary stages are analysed in terms of the distance of the source. Probable mechanisms are discussed.
551.594 .6

463
The Accuracy of the Determination of Reflection Heights and Distances of Atmospherics on the basis of their Waveform.-G. Skeib. (Z. Met., May/ June 1957, Vol. 11, Nos. 5/6, pp. 129-135.) The errors in calculating reflection height $H$ and distance $D$ of atmospherics are investigated as a function of the ratio $H / D$ and of the reflection modes. A recorded waveform is analysed and results are tabulated. See also 1762 of 1957 and 122 of 1956 (Horner \& Clarke).
551.594.6: 621.396.029.4 464
Diurnal Variation in the Occurrence of 'Dawn Chorus'.-J. H. Pope. (Nature, Lond.; 31st Aug. 1957, Vol. 180, No. 4583 ,
p. 433.) A histogram of observations made at frequencies between 1 and $10 \mathrm{kc} / \mathrm{s}$ on 116 days between January and July 1956 at College, Alaska, shows a maximum at 1400 local time which appears to be related to geomagnetic latitude.

## LOCATION

AND AIDS TO NAVIGATION
621.396.9: 621.396.11.029.55

465
Direct-Vision-Type Direction Finder for High Frequency.-K. Miya, T. Sasaki, M. Ishikawa \& S. Matsushita. (Rep. Ionosphere Res. Japan, March 1957, Vol. 11, No. 1, pp. 1-10.) The bearing of an h.f. signal is indicated directly on a c.r. tube by a bright radial line at the corresponding angle. A sensitivity 40 dB higher than that of conventional equipment is achieved by deriving the c.r.-tube deflection voltages from the changes in the rectified output of a receiver when different aerial combinations are connected to its input in sequence. The high sensitivity permits directional observations on weak scattered signals. Circuit diagrams are given and sources of error are discussed.
621.396.962.33

466
Two Doppler Navigators.-(Brit. Commun. Electronics, Sept. 1957, Vol. 4, No. 9, pp. 551-553.) Brief details of airborne equipments for use by military and commercial aircraft.

### 621.396.962.33

467
Radar Drift Measurement using Doppler Techniques.-P. L. Stride. (Brit. Commun. Electronics, Sept. 1957, Vol. 4, No. 9, pp. 554-557.) A drift indicator is described which includes all the control and display circuits necessary to adapt a conventional search radar to measure drifts. Some results of recent trials are discussed.
621.396.963.5: 621.373.4.029.4 468
Phase-Shift Oscillator Indicates Radar Range.-Barritt. (See 397.)
621.396.969.33

469
Errors in Radar Navigation.-T. Stuland. (J. Inst. Nav., Oct 1957, Vol. I0, No. 4, pp. 390-396.) The possible maximum errors are considered which may be contributory factors to collisions between ships. Alteration in course may not, by itself, be sufficient and should be combined with speed reduction so that there is more time in which information is obtained.

## MATERIALS

AND SUBSIDIARY TECHNIQUES

### 533.583 : 621.385 .032 .14 470

The Oxidation of Evaporated Baxium Films (Getters).-R. N. Bloomer. (Brit. J. appl. Phys., Aug. 1957, Vol. 8, No. 8,
pp. 321-329.) Mott's theory of oxidation (see e.g. 439 of 1948 ) is applied to measurements of the main quantities important to the gettering process. The formation of the first monolayer of oxide film is explained. Below a critical temperature of $40^{\circ} \mathrm{C}$ a protective oxide film grows to a thickness of about $50 \AA$ only, while above $40^{\circ} \mathrm{C}$ Ba films are oxidized right through. See also 2140 of 1957.
533.583: 621.385 .032 .14
Baxium Getters and Carbon Mon-oxide.-R. N. Bloomer. (Brit. J. appl. Phys., Sept. 1957, Vol. 8, No. 9, pp. 352-355.) An experimental study of the absorption of CO by evaporated Ba films indicates that the CO is dissociated at the surface of the Ba film, forming an oxide layer containing free carbon. The critical temperature above which the oxide layer ceases to be protective is $80^{\circ} \mathrm{C}$.

### 535.215: 537.533

472
Photoelectric Emission from Barium Oxide.-H. R. Philipp. (Phys. Rev., 1st Aug. 1957, Vol. 107, No. 3, pp. 687-693.) Photoelectric emission measurements were made on sprayed coatings of BaO in several states of thermionic activity and at different temperatures. The spectral distribution of the photoelectric yield shows a rise at a quantum energy of 3.8 eV ascribed to exciton-induced emission, and another rise at 5 eV attributed to electrons ejected from the filled band. Analysis of the energy distribution of emitted electrons shows that different emission mechanisms are operative at low and high incident quantum energies.
535.37: 546.472.21 473
The Measurement of the Optical Properties of Zinc Sulphide.-C. K. Coogan. (Proc. phys. Soc., 1st Sept. 1957, Vol. 70, No. 453B, pp. 845-861.) A comprehensive description of apparatus and technique, and a discussion of results. A comparison is made with other work on the optical properties of ZnS . A band at about $330 \mathrm{~m} \mu$ is found in the absorption spectrum, particularly at liquid air temperatures, together with a corresponding region of anomalous dispersion.

### 535.37: 546.472 .21 <br> 474

Models of Different. Types of Traps in Zinc Sulphide Phosphors. Thermal and Optical Liberation of Trapped Electrons.-D. Curie. (J. Phys. Radium, April 1957, Vol. 18, No. 4, pp. 214-222.) Models for shallow and deep traps are considered and activation energies are calculated. 40 references.
535.376: 546.472.21

475
Mechanism of Electroluminescence of Zinc Sulphide.-R. Goffaux. (J. Phys. Radium, Jan. 1957, Vol. 18, No. 1, pp. 1-4.)
537.226/.227: [546.431.824-31

Solid-State Reaction between Barium Titanate and Strontium Titanate,-S. Nomura. (J. phys. Soc. Japan, Sept. 1956, Vol. 1I, No. 9, pp. 924-929.) The reaction is induced by sintering. Measurements were made of the variations, with sintering con-
ditions, of the permittivity/temperature characteristics and of the crystal structure of $1: 1$ mixtures.
$537.226 / .227: 546.431 .824-31 \quad 477$
Some Aspects of Wedge - Shaped Domains in $\mathrm{BaTiO}_{8}$ Crystal.-T. Nakamura, W. Kinase \& Y. Kato. (J. phys. Soc. Japan, July 1957, Vol. 12, No. 7, pp. 836837.) At $20^{\circ} \mathrm{C}$ wedge-shaped domains were observed which were presumed to have formed during the transition from cubic to tetragonal structure in cooling through the $120^{\circ} \mathrm{C}$ Curie point. On cooling below $5^{\circ} \mathrm{C}$ a marked nonreversible change in the pattern occurred.
537.226: 537.52

478
Dipoles and Electric Breakdown.J. A. Kok \& M. M. G. Corbey. (Appl. sci. Res., 1957, Vol. B6, No. 6, pp. 449-455.) The breakdown of dielectric material may be caused by induced as well as permanent dipoles gathering at a place of maximum stress to form a bridge.

### 537.227

479
Laboratories Announce New Ferro-electric.-(Bell Lab. Rec., July 1957, Vol. 35, No. 7, p. 271.) Some of the properties of triglycine sulphate are described. These properties make it a promising material for switching circuits and storage devices.

### 537.228.1

 480Coupling Coefficient and the Electromechanical Efficiency of Piezoelectric Materials.-Y. Le Corre. (J. Phys. Radium, Jan. 1957, Vol.' 18, No. 1, pp. 5158.) A mathematical analysis is given defining the electromechanical coupling coefficients and efficiencies of unidimensional and orthorhombic crystals. A hollow cylindrical piezoelectric detector is also considered.

### 537.311 .33

481
Vasileff's Calculation of Electronic Self-Energy in Semiconductors.-E. N. Adams. (Phys. Rev., 1st Aug. 1957, Vol. 107, No. 3, p. 671:) Vasileff's theory (2178 of 1957) fails for semiconductors of the usual type because of the predominance of processes involving virtual phonons of large wave number.

### 537.311 .33

482
The Mass Action Laws for the Reactions between Free Carriers and Impurities in Semiconductors considering the Electron Spin.-F. W. G. Rose. (Proc. phys. Soc., 1st Aug. 1957, Vol. 70, No. 452B, pp. 801-803.) A general rule is quoted which does not require a knowledge of the partition function. The reaction between free electrons and group-V donors in Si or Ge is treated to illustrate the use of the general rule.
537.311 .33 483
Low-High Conductivity Junctions in Semiconductors.-L. W. Davies. (Proc. phys. Soc., 1st Sept. 1957, Vol. 70, No. 453B, pp: 885-889.) A theoretical study including the effect of diffusion of charge carriers near the junction. A quantitative description of the 'accumulation' of minority charge carriers at low-high junctions in filaments is given.
537.311 .33 484
Semiconductor Lifetime as a Function of Recombination State Density.D. H. Clarke. (J. Electronics Control, Oct. 1957, Vol. 3, No. 4, pp. 375-386.) "The analysis of the Shockley-Read model is extended to describe the transient behaviour. The results are compared with those already given by Fan [1797 of 1954] and by Rittner, and it is concluded that the latter cease to be valid at high recombination state densities. The relation between steady-state and transient measurements of photoconductivity is examined, and some numerical examples are presented."

### 537.311.33

485
Cooling of Hot Electrons by Acoustic Scattering in Degenerate Semicon-ductors.-R. F. Greene. (J. Electronics Control, Oct. 1957, Vol. 3, No. 4, pp. $387-$ 390.) " Shockley's calculation of the energy loss rate of hot electrons by acoustic scattering in semiconductors is extended to include the case of degenerate electron statistics. A simple formula is given for the loss rate in terms of the acoustic mean free time, valid for any degree of degeneracy. A relaxation time for the electron energy is expressed in terms of the acoustic mean free time showing the effect of degeneracy."

### 537.311 .33

486
Quasi-electric and Quasi-magnetic Fields in Nonuniform Semiconductors. -H. Kroemer. (RCA Rev., Sept. 1957, Vol. 18, No. 3, pp. 332-342.) In a nonuniform semiconductor, e.g. one with nonuniform elastic strains, or a semiconductor alloy of varying composition, the width of the energy gap varies throughout the material. This produces gradients of the band edges which differ for the conduction and valence bands, and act as 'quasi-electric' fields which are not the same for holes and electrons. Examples are given to show how transistor performance can be improved by the incorporation of such fields. A description is also given of how 'quasi-magnetic' fields arise when an inhomogencity causes a shift of the location within the Brillouin zone of the energy minimum of the band.

### 537.311 .33 : $[537.32+536.21$

487
Thermoelectric and Thermal Properties of Semiconductors.-A. Joffe. ( $J$. Phys. Radium, April 1957, Vol. 18, No. 4, pp. 209-213.) Discussion with reference to the application of semiconductor thermocouples for power supply.

### 537.311 .33 : 537.32

488
A Simple Derivation of the Thermoelectric Voltage in a Nondegenerate Semiconductor.-F.- W. G. Rose, E. Billig \& J. E. Parrott. (J. Electronics Control, Nov. 1957, Vol. 3, No. 5, pp. 481-486.) Only concepts such as Fermi levels, field current, diffusion current, etc., are used in the derivation.

### 537.311.33: 537.533

489
Thermionic and Semiconducting Properties of [Ag]-Cs $\mathbf{2}_{2} \mathbf{O}, \mathbf{A g}, \mathbf{C s}$.-J. E. Davey. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9, pp. 1031-1034.) A description of measurements on $[\mathrm{Ag}]-\mathrm{Cs}_{2} \mathrm{O}$ as a
thermionic emitter. Results are given for work function, conductivity, and activation energy over a wide range of temperatures.
537.311.33: 538.632

Determination of the Impurity Concentrations in a Semiconductor from Hall Coefficient Measurements.-P. A. Lee. (Brit. J. appl. Phys., Aug. 1957, Vol. 8, No. 8, pp. 340-343.) Impurity concentrations are found from an equation relating carrier concentration to temperature and acceptor and donor concentrations. The experimental method is applied to $p$-type Si.
537.311.33: 538.632

491
The Relationship between the Hall Coefficient and the Resistivity of Semiconductors, taking Various Scattering Mechanisms of the Charge Carriers into Account.-T. Fukuroi \& C. Yamanouchi. (Sci. Rep. Res. Inst. Tohoku Univ., Ser. A, Aug. 1957, Vol. 9, No. 4, pp. 267272.) In addition to lattice and ionizedimpurity scattering, neutral-impurity and dislocation scattering become appreciable at low temperatures. The relation between Hall coefficient and resistivity is calculated for five cases in which two of these four mechanisms are combined. The method is similar to that used by Jones (1357 of 1951) for combined lattice and ionized-impurity scattering.
537.311 .33 : 538.632 : 621.373 .5 492
Experimental and Theoretical Investigation of Semiconductor Hall-Effect Generators.-M. J. O. Strutt \& S. F. Sun. (Arch. elekt. Ubertragung, June 1957, Vol. 11, No. 6, pp. 261-265.) D.c. amplification was obtained using an experimental feedback circuit incorporating a Hall element of $\operatorname{InSb}$ at room temperature. An oscillator circuit covering the range $13-330 \mathrm{c} / \mathrm{s}$ with an output of about 12 mW is described. Results of measurements agree with theory; the effect of temperature on oscillator performance is discussed.
537.311 .33 : 539.23

493
Frequency Dependence of the A.C. Resistance of Thin Semiconducting Films.-M. Lax \& R. Sachs. (Phys. Rev., 1st Aug. 1957, Vol. 107, No. 3, pp. 650655.) A modification of Howe's theory (see Wireless Engr, Nov. 1940, Vol. 17, No. 206, pp. 471-477) is put forward in which the assumption of constant capacitance per unit length is dropped. The theoretical results agree with the experiments of Broudy \& Levinstein (2696 of 1954) ; the agreement of the Howe theory with earlier experiments is shown to be partially fortuitous.
537.311 .33 : $[546.28+546.289$ 494
Anisotropic Diffusion Lengths in Germanium and Silicon Crystals containing Parallel Arrays of Edge Dis-locations.-R. L. Bell \& C. A. Hogarth. (J. Electronics Control, Nov. 1957, Vol. 3, No. 5, pp. 455-470.) Techniques are described for introducing parallel arrays of edge dislocations into Ge and Si by plastic bending. Ge crystals with similar dislocations but with a higher mean minoritycarrier lifetime than those subjected to plastic bending, may be grown by pulling from the melt, using a suitably orientated dislocated
seed crystal. The diffusion length is greater when measured along the dislocations than across them. A model suggests that the anisotropies observed will be more marked for crystals in which the dislocations are highly polygonized.
537.311.33: 546.28

495
The Effect of Heat Treatment on the Bulk Lifetime of Excess Charge Carriers in Silicon.-LL. M. Nijland \& L. J. van der Pauw. (J. Electronics Control, Oct. 1957, Vol. 3, No. 4, pp. 391-395.) Bulk lifetime in both $p$ - and $n$-type crystals made by the floating zone technique, and in $n$-type crystals made by the Czochralski technique, are increased by annealing at $300^{\circ} \mathrm{C}$ to $700^{\circ} \mathrm{C}$. Annealing at $>700^{\circ} \mathrm{C}$ decreased lifetimes for $p$ - and $n$-type crystals made by either method.
537.311 .33 : 546.28 496
Radiochemical Analysis of Silicon.J. A. James \& D. M. Richards. (J. Elec-. tronics Control, Nov. 1957, Vol. 3, No. 5, pp. 500-506.) ' $R$ Results of radioactivation analyses for some 12 elemenis are given for silicon from two sources. The results of segregation coefficient measurements using radiochemical methods are quoted for P, Fe, Co, W, and Au."

### 537.311 .33 : 546.28 : 535.343

497
Infrared Absorption of Oxygen in Silicon.-H. J. Hrostowski \& R. H. Kaiser. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, pp. 966-972.) Three infrared absorption bands have been correlated with the oxygen concentration of Si . Results obtained are explained by a model in which interstitial oxygen is bonded to two adjacent Si atoms in a nonlinear $\mathrm{Si}-\mathrm{O}-\mathrm{Si}$ unit.

### 537.311.33: 546.28: 538.63

498
Galvanomagnetic Effects in p-Type Silicon.-D. Long. (Phys. Rev., Ist Aug. 1957, Vol. 107, No. 3, pp. 672-677.) Measurements are reported of the dependence, on temperature and field strength, of the resistance and Hall effect, for several samples of $p$-type Si . The results are discussed with reference to the usual valence-band model to show that there is some inconsistency.

### 537.311.33: 546.289

 499Recombination in Plastically Deformed Germanium.-G. K. Wertheim \& G. L. Pearson. (Phys. Rev., 1st Aug. 1957, Vol. 107, No. 3, pp. 694-698.) "Lifetimes in plastically deformed $n$ - and $p$-type Ge have been measured as a function of the amount of deformation and as a function of temperature. The results indicate that the dislocations have an electron capture radius of $3.4 \times 10^{-8} \mathrm{~cm}$. The lifetime in high-purity crystals containing $10^{3}$ to $10^{4}$ dislocations per $\mathrm{cm}^{2}$ may consequently be limited by recombination at dislocations."

### 537.311.33: 546.289

500
Recombination Centres and Fast States on Unstable Germanium Sur-faces.-S. Wang \& G. Wallis. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, pp. 947953.) The results of measurements of surface conductance, photoconductance,
dark field effect and field effect under illumination are presented for freshly etched samples of $n$ - and $p$-type Ge exposed to the Brattain-Bardeen ambient cycle. Analysis shows that the recombination centres and 'fast' centres are identical.

### 537.311.33: 546.289

501
Modulation of Light Reflected from Germanium by Injected Current Car-riers.-I. Filiński. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, p. 1193.) Preliminary experimental results are reported of the modulation of reflected light from the surfaces of single-crystal diodes, which arises when alternating voltages are applied to them.

### 537.311.33: 546.289

502
Contribution of Current Carriers in the Reflection of Light from Semi-conductors.-L. Sosnowski. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, pp. 11931194.) An interpretation is given of the electro-optical phenomena reported by Filiński (501 above).
537.311.33: 546.289

503
On the Absorption by Free Carriers in Semiconductors.-B. Donovan \& N. H. March. (Proc. phys. Soc., 1st Sept. 1957, Vol. 70, No. 453B, pp. 883-885.) The range of validity is assessed of some theoretical treatments of the properties of free carriers in alternating fields [see e.g. 2110 of 1956 (Fan et al.)], by examining infrared absorption in $n$-type Ge.

### 537.311.33: 546.289

504
Field Dependence of Mobility in p-Type Germanium.-K. S. Mendelson \& R. Bray. (Proc. phys. Soc., 1st Sept. 1957, Vol. 70, No. 453B, pp. 899-900.) A short description of results obtained on $p$-type Ge at $78^{\circ} \mathrm{K}$ and $195^{\circ} \mathrm{K}$, using samples with carrier content between $3 \times 10^{12}$. and $4 \times 10^{15} \mathrm{~cm}^{-3}$. A graph of conductivity as a function of electric field is shown.

### 537.311.33: 546.289

505
Effect of Edge Dislocations on the Alloying of Indium to Germanium.J. I. Pankove. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9, pp. 1054-1057.) Observations of the effects of crystal imperfections on the alloying process show that. edge dislocations and other crystal disturbances enhance the dissolution of Ge in In. An interpretation of this and other effects is given.

### 537.311.33: 546.289

506
Spiral Etch-Pits in Germanium.R. G. Rhodes, K. O. Batsford \& D. J. DaneThomas. (J. Electronics Control, Oct. 1957, Vol. 3, No. 4, pp. 403-408.) Discussion illustrated with photographs of spiral 'terraced' pits produced by etching the $\{111\}$ or $\{100\}$ crystal surfaces with iodine solution. The density is $10^{6}-10^{6} \mathrm{~cm}^{-2}$; association with impurities is suggested.
537.311.33: 546.289

507
On the Carrier Recombination through Nickel Impurities in Germanium.-J. Okada. (J. phys. Soc. Japan, June 1957, Vol. 12, No. 6, p. 741.)

The increase of the photo-conductivity to a saturation value as the temperature decreases may be explained by assuming that Ni introduces two acceptor levels and recombination takes place through multiple levels of constant capture cross-section.

### 537.311.33: 546.289

508
Some Experiments on the Surface Field Effects in Germanium Single Crystals.-M. Kikuchi. (J. phys. Soc. Japan, July 1957, Vol. 12, No. 7, pp. 756-762.) Measurements of the field effect on surface conductance and on surface recombination velocity show that the difference between the Fermi level and the middle of the energy gap at the surface drifts to a negative value when the surface is kept in room air after CP4 etching. The drift is accompanied by a gradual growth of an oxide layer on the surface.

### 537.311.33: 546.289

509
A Simpler Method for Removing Copper from Germanium.-M. Kikuchi \& S. Izima. (J. phys. Soc. Japan, July 1957, Vol. 12, No. 7, p. 824.) A simple treatment involving immersion in concentrated nitric acid followed by heating in A is described, which removes about $45 \%$ of the Cu atoms originally present with a density of about $4-7 \times 10^{-14} \mathrm{~cm}^{-8}$.

### 537.311.33: 546.289: 538.63

510
Galvanomagnetic Effects in Ger-manium.-G. C. Della Pergola \& D. Sette. (Nuovo Cim., lst June 1957, Vol. 5, No. 6, pp. 1670-1678.) Results of measurements on $n$ - and $p$-type single-crystal Ge of magnetoresistance and Hall effect (see also 3444 of 1956) as a function of magnetic induction are compared with results derived theoretically from a knowledge of the valence band structure. This comparison is wholly satisfactory only for $n$-type material.
537.311.33: 546.289: 548.73

511
Fine Structures of X-Ray Absorption Spectra of Crystalline and Amorphous Germanium.--T. Shiraiwa, T. Ishimura \& M. Sawada. (J. phys. Soc. Japan, July 1957, Vol. 12, No. 7, pp. 788-792.) A comparison of the spectra suggests that amorphous Ge has a structure similar to the diamond lattice of the crystalline Ge but with a larger spacing.

### 537.311.33: 546.48.86

512
Electrical Properties of Cd-Sb.-T. Miyauchi \& H. Kimura. (J. phys. Soc. Japan, Sept. 1956, Vol. 11, No. 9, pp. 1013-1014.) From conductivity and Hall coefficient measurements it is found that hole mobility at room temperature is $1100 \pm 200 \mathrm{~cm}^{2} /$ V. sec and the width of the forbidden energy gap is $0.3 \pm 0.05 \mathrm{eV}$.
537.311.33: 546.561-31

513
Linear and Quadratic Zeeman Effects and Diamagnetism of the Exciton in Cuprous Oxide Crystals.-E. F. Gross \& B. P. Zakhartchenia. (J. Phys. Radium, Jan. 1957, Vol. 18, No. 1, pp. 68-71.) $\mathrm{Cu}_{2} \mathrm{O}$ films $100 \mu$ thick were studied at a temperature of $1.3^{\circ} \mathrm{K}$ in a magnetic field of 30000 oersteds by means of a spectrograph of $1.5 \AA / \mathrm{mm}$ dispersion.

The Transverse Magnetoresistance Effect in Indium Arsenide.-C. H Champness \& R. P. Chasmar. (J. Electronics Control, Nov. 1957, Vol. 3, No. 5, pp. 494-499.) "Measurements were made on samples of various shapes. For a long thin sample the magnitude of the effect is considerably smaller than expected for acoustic lattice scattering. It is suggested that this result may be explained by the presence of some impurity scattering. In approximately square samples the magnitude of the magnetoresistive changes are large being $100 \%$ or more at room temperature in a field of $10^{4}$ G."
$537.311 .33:[546.682 .86+546.681 .86 \quad 515$
Nuclear Magnetic Resonance in Semiconductors : Part 2 - Quadrupole Broadening of Nuclear Magnetic Resonance Lines by Elastic Axial Deforma-tion.-R. G. Shulman, B. J. Wyluda \& P. W. Anderson. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, pp. 953-958.) By applying stresses to samples of InSb and GaSb having a high degree of crystalline perfection, it has been possible to destroy the crystalline symmetry reversibly, thereby producing quadrupole broadening of the nuclear-magnetic-resonance lines. Strains of less than $10^{-4}$ have been detected and the resulting field gradients measured. Part 1 1107 of 1956 (Shulman et al.).
537.311 .33 : 546.682 .86 516
Electrical Properties of P-Type Indium Antimonide.-T. Fukuroi \& C. Yamanouchi. (Sci. Rep. Res. Inst. Tohoku Univ., Ser. A, Aug. 1957, Vol, 9, No. 4, pp. 262 266.) Report of measurements of resistance, Hall coefficient and magnetoresistance, on polycrystalline specimens, in the temperature range $289^{\circ}-1 \cdot 4^{\circ} \mathrm{K}$.
537.311.33: 546.682.86 517
Absorption and Dispersion of Indium Antimonide.-T. S. Moss, S. D. Smith \& T. D. F. Hawkins. (Proc. phys. Soc., Ist Aug. 1957, Vol. 70, No. 452 B, pp. 776-784.)
537.311 .33 : 546.682 .86 : 535.343

Infrared Resonant Absorption from Bound Landau Levels in InSb.-W. S. Boyle \& A. D. Brailsford. (Phys. Rev., 1st Aug. 1957, Vol. 107, No. 3, pp. 903-904.) Measurements of light transmission as a function of magnetic field, on thin $n$-type samples show a field-dependent resonance absorption which is ascribed primarily to Landau levels bound to donor impurities.

### 537.311 .33 : $546.682 .86: 538.63$

519
 in $n$-type Indium Antimonide.-Y. Kanai \& W. Sasaki. (J. phys. Soc. Japan, Sept. 1956, Vol. 11, No. 9, pp. 1017-1018.) Measurements were made of magnetoresistance and Hall coefficient in the temperature range $1 \cdot 3-300^{\circ} \mathrm{K}$. At $1 \cdot 3^{\circ} \mathrm{K}$ an oscillatory dependence on magnetic field strength was observed. See also 477 of 1956 (Kanai).
$537.311 .33: 546.873 .241520$
Electrical Properties of $\mathrm{Bi}_{2} \mathrm{Te}_{3}$.-S. Shigetomi \& S. Mori. (J. phys. Soc. Japan, Sept. 1956, Vol. 11, No. 9, pp. 915-919.) The conductivity, Hall coefficient and
thermoelectric power have been measured in the temperature range $100-750^{\circ} \mathrm{K}$. The conductivity is $p$ type at room temperature. Hole mobility varies with temperature as $1.2 \times 10^{8} \mathrm{~T}^{-2 \cdot 3}$, and the gap width is 0.21 eV at $0^{\circ} \mathrm{K}$.
537.311.33:546.873.241:537.322.1 521

Performance of Composite Peltier Junctions of $\mathbf{B i}_{\mathbf{2}} \mathbf{T} \mathbf{e}_{3}$--T. S. Shilliday. ( $J$. appl. Phys., Sept. 1957, Vol. 28, No. 9, pp. 1035-1042.) An experimental Peltier-type refrigerator using $p$ - and $n$-type $\mathrm{Bi}_{2} \mathrm{Te}_{3}$ as thermoelements of annular shape is described. Under no-load conditions a maximum temperature difference of $49^{\circ} \mathrm{C}$ was obtained. The experimental results agree with the theoretical predictions. See also 3224 of 1956 (Stil'bans et al.).

## $537.311 .33: 548.73$

 522The Crystalline Perfection of some Semiconductor Single Crystals.-R. L. Bell. (J. Electronics Control, Nov. 1957, Vol. 3, No. 5, pp. 487-493.) "Single crystals of Ge, $\mathrm{Si}, \mathrm{InSb}$ and HgTe were examined by the Guinier-Tennevin X-ray technique. The degree of perfection as shown by the width of the focused Laue image was compared with the dislocation density as revealed by etch-pits."

### 537.311.33.096

523
Graphical Analysis of the Temperature Dependence of the Electronic Population in Semiconductors.-G. Brouwer. (Philips Res. Rep., Oct. 1957, Vol. 12, No. 5, pp. 415-422.) ''The distribution of electrons and holes in semiconductors and its variation with temperature may be derived by means of a graphical approximation presented in this paper. The method is based directly on the electronic reaction equations in the equilibrium."
537.32 : 546.562-31

524
Thermoelectric Effects Shown by some Oxides. Investigation of Cupric Oxide.-G. Péri, M. Perrot \& J. Robert. (J. Phys. Radium, April 1957, Vol. 18, No. 4, pp. 282-283.) See 3111 of 1956 (Perrot et al.).

### 538.22

525
Theory of the Magnetic Properties of Ferrous and Cobaltous Oxides: Parts 1 \& 2.-J. Kanamori. (Prog. theor. Phys., Feb. 1957, Vol. 17, No. 2, pp. 177-222.)

### 538.22 : 538.569 .4

526
High-Field Antiferromagnetic Resonance in $\mathbf{M n F}_{2}$ using Pulsed Fields and Millimetre Wavelengths.-S. Foner. (Phys. Rev., lst Aug. 1957, Vol. 107, No. 3, pp. 683 685.) Measurements from $4 \cdot 2^{\circ} \mathrm{K}$ up to the Néel temperature ( $68^{\circ} \mathrm{K}$ ) are reported; they agree with the molecularfield approximation of antiferromagneticresonance theory.
538.22 : 538.569 .4 : 539.15

527
Observation of Nuclear Magnetic Resonance in Antiferromagnetic $\mathbf{M n}\left(\mathbf{F}^{18}\right)_{2}$.-V. Jaccarino \& R. G. Shulman. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, pp. 1196-1197.) Magnetic resonances have been observed at frequencies in the range $152-168 \mathrm{Mc} / \mathrm{s}$, in external magnetic fields between 300 and 3000 oersteds and at temperatures between $1 \cdot 3^{\circ}$ and $20 \cdot 4^{\circ} \mathrm{K}$.
538.22 : 546.3-1'71 1'681'26

Spontaneous Magnetization in Mn-Ga-C Alloys.-H. P. Myers. (Canad. J. Phys., July 1957, Vol. 35, No. 7, pp. 819 822.) In the alloy systems $\mathrm{Mn}-\mathrm{Al}-\mathrm{C}$, $\mathrm{Mn}-\mathrm{Zn}-\mathrm{C}, \mathrm{Mn}-\mathrm{Sn}-\mathrm{C}$ and $\mathrm{Mn}-\mathrm{In}-\mathrm{C}$, there is a distinctive face-centred cubic ternary phase which has pronounced spontaneous magnetization. A similar phase has been found in the Mn-Ga-C system. See also 3924 of 1957 (Brockhouse \& Myers).
538.221

529
Magnetic Influence on the Recrystallized Grain Texture of a Ferromagnetic Alloy.-B. Sawyer \& R. Smoluchowski. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9, pp. 1069-1070.) A note on the effect of a magnetic field on the texture of an Fe -Co alloy in the form of rolled sheet.
538.221

Temperature Dependence of Anisotropy Energy of Ferromagnetics.-T. Kasuya. (J. phys. Soc. Japan, Sept. 1956, Vol. 11, No. 9, pp. 944-947.) Calculations are made using the spin-wave method. The anisotropy constant is shown to depend on $\left(M / M_{0}\right)^{16}$ where $M_{0}$ and $M$ are, respectively, magnetizations at absolute zero and at the finite temperature considered.
538.221: 538.24:538.652

Magnetization, Magnetostriction and Relaxation Phenomena during Isothermal Magnetic Annealing at High Temperatures in Ni-Co Alloys.- H Masumoto, H. Saito \& M. Takahashi. (Sci Rep. Res. Inst. Tohoku Univ., Ser. A, Aug. 1957, Vol. 9, No. 4, pp. 293 308.) The magnetization and magnetostriction as a function of time were investigated at constant temperature after the application of a magnetic field to thermally demagnetized $\mathrm{Ni}-\mathrm{Co}$ alloys. In a temperature range between about $300^{\circ} \mathrm{C}$ and the Curie point a relaxation effect was observed which is attributed to displacements of impurities or lattice defects due to the magnetostriction at high temperatures.
538.221: 621.318.1 532
The Unusual Magnetic Properties of Quenched Alcomax III.-M. McCaig. (Proc. phys. Soc., 1st Sept. 1957, Vol. 70, No. $453 \mathrm{~B}, \mathrm{pp} .823$ 826.) Quenching of alcomax III from a high temperature results in an unusual soft magnetic material. The permeability is almost constant up to flux densities of 5000 G , and the ratio of resonance to saturation intensity is less than $0 \cdot 1$.
538.221: 621.318.122

533
Processes occurring during the Heat Treatment of Alcomax.-A. G. Clegg \& M. McCaig. (Proc. phys. Soc., 1st Sept. 1957, Vol. 70, No. 453B, pp. 817-822.) The dependence of saturation intensity and coercivity on temperature, from room temperature to $900^{\circ} \mathrm{C}$, is shown. Maxima in the cocrcivity curves are associated with subsidiary Curie points.
538.221: 621.318.124

534
Rotational Model of Flux Reversal in Square-Loop Ferrites.-E. M. Gyorgy. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9 pp. 1011-1015.) A discussion of the mech.
anism of magnetic flux reversal using fields much higher than those encountered in quasi-static processes. Detailed results for the switching coefficients are given.

### 538.221: 621.318.134

535
The $K_{1^{-}}$and True $g$-values of Polycrystalline Ferrites.-J. Snieder. (Appl. sci. Res., 1957, Vol. B6, No. 6, pp. 471-473.) Measurements are reported which give a true $g$-value of $2 \cdot 11$ and a $K_{1}$-value at room temperature of $-5 \cdot 8 \times 10^{3} \mathrm{~J} / \mathrm{m}^{3}$ for $\mathrm{Ni}-\mathrm{Zn}$ ferrites with $50 \% \mathrm{NiO}$.
538.221: 621.318.134

536
Magnetic Annealing Effect in IronNickel Ferrites.-Y. Aiyama, H. Sekizawa \& S. Iida. (J. phys. Soc. Japan, June 1957, Vol. 12, No. 6, p. 742.)
538.221: 621.318.134

537
Structural Study of Iron Selenides FeSex: Part 1-Ordered Arrangement of Defects of Fe Atoms.-A. Okazaki \& K. Hirakawa. (J. phys. Soc. Japan, Sept. 1956, Vol. 11, No. 9, pp. 930-936.)
538.221: 621.318.134

538
Ferrimagnetic Resonance in Gadolinium Iron Garnet.-B. A. Calhoun, J. Overmeyer \& W. V. Smith. (Phys. Rev., 15th Aug. 1957, Vol. 107, No. 4, pp. 993 994.) The apparent $g$-factor and line width have their maximum values at the compensation point $\left(13^{\circ} \mathrm{C}\right)$, which implies that the $g$-factors of the $\mathrm{Gd}^{3+}$ and $\mathrm{Fe}^{3+}$ ions are equal.
538.221: 621.318.134 539
Antiferromagnetism of $\mathrm{Zn}_{n}$ Ferrite. M. Tachiki \& K. Yosida. (Prog. theor. Phys., Feb. 1957, Vol. 17, No. 2, pp. 223-240.) Magnetic dipole-dipole spin interaction probably causes the main anisotropy energy below the Neel temperature. Above this temperature calculations are made for susceptibility and specific heat taking account of short-range order.
538.222: 538.569.4

540
Paramagnetic Resonance of Nickel Fluosilicate under High Hydrostatic Pressure.-W. M. Walsh, Jr, \& N. Bloembergen. (Phys. Rev., Ist Aug. 1957, Vol. 107, No. 3, pp. 904-905.)
621.315.616.9

541
Dielectric Strength of Polyethylene at $3 \mathbf{3 0 0} \mathrm{Mc} / \mathrm{s}$.-H. Farber \& J. W. E. Griemsmann. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9, pp. 1002-1005.) The dielectric strength at $3300 \mathrm{Mc} / \mathrm{s}$ was measured to be $16 \cdot 8,13 \cdot 1$ and $6: 0 \mathrm{kV} / 10^{-3} \mathrm{in}$. at $26^{\circ}$, $57^{\circ}$ and $95^{\circ} \mathrm{C}$, respectively. The values are the same as those obtained for a d.c. field. The specially designed electrode system is described.

### 621.315.616.95: 621.317.335.3.029.64 538.569.3

Temperature Dependence of Dielectric Loss of Shellac in Microwave Region.-S. S. Srivastava, D. D. Puri \& P. C. Mehendru. (Proc. nat. Inst. Sci. India, Part A, 26th July 1957, Vol. 23, No. 4, pp. 289-292.) A description of measurements on three grades of purified shellac in the $3-\mathrm{cm}$ region at temperatures between $20^{\circ} \mathrm{C}$ and
$50^{\circ} \mathrm{C}$, using a standing wave technique. Tan $\delta$ increased rapidly with temperature in all cases.

### 621.318.2.002.2

543
Manufacture of Anisotropic Lead Ferrite Permanent Magnets Without the Use of a Magnetic Field during Moulding.-F. Pawlek \& K. Reichel. (Naturwissenschaften, July 1957, Vol. 44, No. 14, p. 390.) Comparative demagnetization curves of oxide magnets are shown; the Pb -ferrite magnet moulded without magnetic field has higher resonance than one of Ba ferrite.

## MEASUREMENTS AND TEST GEAR

## 529.7

544
Relation between the Proper Time of a Terrestrial Clock and Schwarzschild's Astronomical Time to an Approximation of $10^{-12}$.- O. Costa de Beauregard. (J. Phys. Radium, Jan. 1957, Vol. 18, No. 1, pp. 17-21.) An evaluation of the corrections necessary to a perfect terrestrial clock with reference to a perfect clock at rest at an infinite distance from the sun.
$621.3 .018 .41(083.74)+529.786]$ : 538.569.4
Frequency Shift in Ammonia Absorption due to Foreign Gases.-K. Matsuura, Y. Sugiura \& G. M. Hatoyama. (J. phys. Soc. Japan, July 1957, Vol. 12, No. 7, p. 835.) See also 3949 of 1957
621.317.3: 621.314.6

546
Measurement of the Mean Rectified Value by Vacuum Diodes and BarrierLayer Rectifiers.-E. Czeija. (Arch. tech. Messen, June 1957, No. 257, pp. 137-140.) The inherent errors in basic rectifier circuits and the suitability of the circuits for d.c. calibration are discussed.
621.317.3.029.64: 621.375.9

547 538.569.4

Maser Noise Measurement,-J. C. Helmer. (Phys. Rev., Ist Aug. 1957, Vol. 107, No. 3, pp. 902-903.) Measurements on an ammonia-beam maser amplifier at 24000 $\mathrm{Mc} / \mathrm{s}$ confirm the theoretically low noise figure of such a device.
621.317.33: 621.372.412

548
The Accuracy of a Method of Measuring the Series Capacitance and Inductance of Crystal Resonators.-H. Rühl. (Nachrichtentech. Z., June 1957, Vol. 10, No. 6, pp. 297-302.) The accuracy obtainable with Herzog's method (T.F.T., Sept. 1941, Vol. 30, No. 9, pp. 260 263. Abstract 2031 of 1942) has been investigated. A modification of this method is outlined leading to a simple formula for the series capacitance.
621.317.331: 537.311 .33 549
Semiconductor Specific-Resistance Meter by means of A.C. Method.-A. Sato \& S. Kanai. (Rep. elect. Commun. Lab., Japan, March 1957, Vol. 5, No. 3, pp. 1821.) Details of a transistor circuit are given
621.317.332: 621.314.7

550
Measurements of the Impedance Parameters of Junction Transistors. E. E. Ward. (Brit. J. appl. Phys., Aug. 1957, Vol. 8, No. 8, pp. 329-331.) Practical details are given of equipment for null measurements of earthed-base impedance parameters and $\alpha^{1}$, defined as $\alpha /(1-\alpha)$. Measurements with collector open-circuit are included and typical results at frequencies up to $30 \mathrm{kc} / \mathrm{s}$ are shown.
621.317.335.3: 621.372.51.029.6 551
The Dielectric Disk used as Trans formation Quadripole for the Magnification of the Node Displacement on Measuring Lines.-Breitenhuber. (See 349.)
621.317.34:621.396.65 552

Measurement of Transmission Distortion in F.M. Radio-Link Equipment. -H. Hartbaum. (Arch. elekt. Ubertragung, June 1957, Vol. 11, No. 6, pp. 239-252.) In the method described static and dynamic nonlinearities are determined separately. Equipment operating on this principle can be used for testing the individual elements of radio links as well as the complete system.

### 621.317 .361

553
Automatic Frequency Measurement Techniques.-A. J. Green. (Brit. Commun. Electronics, June 1957, Vol. 4, No. 6, pp. 342 345.) The equipment described has an upper counting limit of over $30 \mathrm{Mc} / \mathrm{s}$; a commercial-type $100-\mathrm{kc} / \mathrm{s}$ frequency standard and the $200-\mathrm{kc} / \mathrm{s}$ transmission from Droitwich are used as reference.
621.317.4.083: 538.221

554
The Shape of Specimens for Measurements on Ferromagnetic Materials.P. K. Hermann. (Arch. tech. Messen, May July 1957, Nos. 256-258, pp. 105-106, 129-132 \& 155-158.)
621.317.7: 621.397.62

555
Transistorized TV Pattern Gener-ator.-F. Rozner. (Brit. Commun. Electronics, June 1957, Vol. 4, No. 6, pp. 346-349.) The generator described is battery operated and incorporates both $p-n-p$ and $n-p-n$ transistors. The mains are used only to provide frequency locking.
621.317 .7 : 621.397 .62 : 535.623

556
Choosing a Colour-Bar Generator.A. R. Stamiti. (Radio TV News, July 1957, Vol. 58, No. 1, pp. 62-63 . . 139.) Comparison of American signal generators for aligning colour-television receivers. Performance features and prices of fourteen types are given in tabular form.
621.317.7.087.9: 621.396.822

557
Probability Computer for Noise Measurement.-A. W. Sullivan \& J. D. Wells. (Electronics, Ist Oct. 1957, Vol. 30, No. 10, pp. 208-209.) The equipment described is designed for the investigation of
the amplitude distribution of atmospheric noise and its effect on radio communication systems. A constant-amplitude pulse is produced each time a reference level is exceeded by the noise input.
621.317 .715

558
Sensitive D.G. Null Detector.-F. Oakes \& E. W. Lawson. (Wireless World, Dec. 1957, Vol. 63, No. 12, pp. 597-598.) Constructional details are given of a galvanometer of $50 \mu \mathrm{~A}$ full-scale deflection incorporating transistors.
621.317 .723

559
An Electrometer Amplifier with Two Dynamic Condensers.-R. J. Ritsma. (Appl. sci. Res., 1957, Vol. B6, No. 6, pp. 429-445.) Capacitive modulators for converting d.c. charge into an a.f. signal are reviewed. A type using two capacitors vibrating in opposite phase. is described which eliminates the converted a.f. noise. An experimental model was used to measure a charge of $125 e$ in 13 sec .
621.317.755: 621.373.431

560
A Wide-Range Oscilloscope Time-base.-A. H. Koster. (R.S.G.B. Bull., June 1957, Vol. 32, No. 12, pp. 546-547.)
621.317.757.029.55 561
A 3 to $30 \mathrm{Mc} / \mathrm{s}$ Spectrum Analyser.J. R. Hayward. (Brit. Commun. Electronics, Sept. 1957, Vol. 4, No. 9, p. 541.) A panoramic display on the c.r. tube screen of the instrument covers a frequency band up to $30 \mathrm{kc} / \mathrm{s}$ wide and an amplitude range of 60 dB ; facilities for direct calibration are provided.

### 621.317 .77

562
Simple Measurement of Phase Differ-ence.-G. de Visme. (Wireless World, Dec. 1957, Vol. 63, No. 12, pp. 581-582.) One of the two sinusoids is reversed in phase and added to the other and the resultant amplitude is adjusted to minimum. Details of a practical circuit with valve voltmeter indication are given.

### 621.317.794: 621.316.825

563
Two Portable Thermistor Radio-meters.-W. H. Ward. (J. sci. Instrum., Aug. 1957, Vol. 34, No. 8, pp. 317-321.) A description of the construction and calibration of two radiometers for the measurement of the hemispherical shortwave radiation and the total radiative flux through a plane, respectively.
621.317.799: 538.569.4:539.152.1 564

Low-Fie1d Nuclear-Magnetic-Spectrometer.-R. W. Mitchell \& M. Eisner. (Rev. sci. Instrum., Aug. 1957, Vol. 28, No. 8, pp. 624-628.) A description of a spectrometer for fields below 50 G for use in studies of nuclear magnetic resonance. A resolution of $10-20 \mu \mathrm{G}$ is obtained over a $30-\mathrm{cm}^{3}$ sample. Some results on the relaxation time for ethanol-water mixtures are also given.

### 621.317.799: 621.314.7

565
Test Equipment for Transistor Pro-duction.-A. B. Jacobsen \& C. G. Tinsley. (Electronics, 1st Oct. 1957, Vol. 30, No. 10, pp. 148-151.)

OTHER APPLICATIONS OF
RADIO AND ELECTRONICS
539.172.4: 621.317.7: 621-52

The Control and Instrumentation of a Nuclear Reactor.-A. B. Gillespic. (Proc. Instn elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, pp. 602-604.) Discussion on 3838 of 1956.

## 621-52: 621.398: 681.17

567
The Digitizer-a High-Accuracy Scale for Automatic Data Processing.-D. S. Evans. (Brit. Commun. Electronics, June 1957, Vol. 4, No. 6, pp. 334-339.) The use of finely subdivided coded scales for the accurate conversion of mechanical motion to digital or numerical form in data transmission systems is described. Development and applications of such encoding equipment are reviewed, in particular, of devices which use a 1000 -division scale on a metal disk as a commutator, or on glass for optical scanning [see e.g. 2975 of 1956 (Jones)].

### 21.384.6.029.6

568
Theory of the Rebatron-a Relativistic Electron Bunching Accelerator for Use in Megavolt Electronics.-P. D. Coleman. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9, pp. 927-935.) A theoretical discussion of the production of highly bunched electron beams having an energy of $1-3 \mathrm{MeV}$, and the application of the technique in the generation of sub-mm waves ( $100-3000 \mathrm{kMc} / \mathrm{s}$ ). Calculations indicate that the emergent beam has an appreciable harmonic content up to the 1 000th harmonic, with a velocity spread of $0.07 \%$. Pulsed beam powers of about 100 kW should be obtainable using a $3 \mathrm{kMc} / \mathrm{s}$ rebatron.

### 621.384.6.029.64

569
Design and Evaluation of an S-Band Rebatron.-I. Kaufman \& P. D. Coleman. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9. pp. 936-944.) Details of the practical design of a rebatron (see 568 above) for producing a high-power, bunched, megavolt electron beam. The properties of the beam are examined experimentally, and the validity of the method is examined by measurements of the ratio of the 26 th beam harmonic current amplitudes under two different sets of conditions.

### 621.384.6.029.65

570
The Harmodotron-a Megavolt Electronics Millimetre Wave Gener-ator.-M. D. Sirkis \& P. D. Coleman. (J. appl. Phys., Sept. 1957, Vol. 28, No. 9, pp. 944-950.) A description of a method of producing high powers at sub-mm $\lambda$ by electronic excitation, at a single frequency, of a high-order TM mode in a cylindrical cavity. Typical experimental measurements at 8.3 mm are described.
621.384.62

571
An Experimental Proton Linear Accelerator using a Helical Waveguide. -D. R. Chick, D. P. R. Petrie, D. G. Keith Walker \& H. Longley. (Nature, Lond., 31st Aug. 1957, Vol. 180, No. 4583, p. 432.) An
experimental section or the accelerator proposed by Chick \& Petrie (1694 of 1952) has been constructed. Accelerations up to $4 \cdot 3 \mathrm{MeV}$ were obtained.
621.385.833: 537.533 572
Photoemission-Type Electron Micro-scope.-E. L. Huguenin. (Ann. Phys., Paris, March/April 1957, Vol. 2, Nos. 3/4, pp. 214-266.) Detailed description of the design and operation of the instrument which is based on electron emission from a metallic surface under ultraviolet irradiation. A magnification of 200 is obtained. Micrograms of specimens of $\mathrm{Ag}, \mathrm{Cu}, \mathrm{Zn}$ and Au etched by ion bombardment are shown.

### 621.398

573
F.M.-F.M. Telemetering.-E. S. Cassedy, Jr. (Electronic Radio Engr, Dec. 1957, Vol, 34, No. 12, pp. 465-467.) Analysis of the frequency spectrum of a double frequency-modulated wave.

## PROPAGATION OF WAVES

### 621.396 .11

Theory of Scattering from a Nearly Transparent Anomaly.-V. W. Bolie. (Appl. sci. Res., 1957, Vol. B6, No. 6, pp. 422-428.) An approximate equation for the propagation of e.m. energy in a nearly transparent medium is applied to the case in which the medium contains a dielectric inhomogeneity in the form of an isolated Gaussian-shaped perturbation in the refractive index. Equations for the scattering are illustrated graphically. The energy extracted from the incident wave due to the anomaly is shown by a graph of the total scattering cross-section as a function of perturbation size.
621.396.11

575
Propagation of a Pulse across a Coast Line.-J. R. Wait. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. I1, pp. 1550-1551.) A generalization of earlier results ( $J$. Res nat. Bur. Stand., July 1956, Vol. 57, No. I, pp. 1-15) applied to various transient waveforms.
621.396.11: 523.5

576
V.H.F. Meteor Scatter Propagation. -W. F. Bain. (QST, April 1957, Vol. 41, No. 4, pp. 20-24.. 144.) Basic principles are described with relevant information on direction of transmission, aerial height and directivity, and occurrence of meteor showers for obtaining optimum communication conditions.
621.396.11:550.389.2

577
Propagation and the International Geophysical Year.—Slack. (Sce 448).
621.396.11:551.501.8 578

The Use of Surface Weather Observations to Predict the Total Atmospheric Bending of Radio Rays at Small Elevation Angles.-B. R. Bean \& B. A.

Cahoon. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp. 1545-1546.) Useful accuracy even for elevation angles as small as 10 milliradians is obtained. The method is extended to zero elevation by substituting profiles with strong ground-based refractive layers for the ducting profile.
621.396.11: 551.51

579
Scattering of Electromagnetic Waves by an Acoustic Disturbance in the Atmosphere.-A. Tonning. (Appl. sci. Res., 1957, Vol. B6, No. 6, pp. 401-421.) It is shown theoretically that the density variations associated with an acoustic wave affect the propagation of an e.m. wave. Under the assumption that the acoustic waves are spherical, the scattered field at large distances is given in terms of definite integrals. The limiting case of plane acoustic waves is discussed. Two numerical examples show the greater efficiency of scattering from plain waves compared with spherical waves.

### 621.396.11: 551.510.52/.53

580
On the Scattering of Radio Waves in the Troposphere, Stratosphere and Ionosphere.-K. Takahasi. (J. Radio Res. Labs, Japan, July 1957, Vol. 4, No. 17, pp. 333-340.) The scattering is assumed to be due to partial reflexion caused by random isotropic fluctuations in refractive index. A few comparisons are made between the theoretical and experimental results.
621.396.11:551.510.52

581
Notes on Phase Incoherence in Tropospheric Propagation and its Effects on Scattered Field.-M. Hirai. (J. Radio Res. Labs, Japan, July 1957, Vol. 4, No. 17, pp. 255-266.)

### 621.396.11: 551.594.5

582
Reflection of Short and Ultra-short Waves from the Aurora.-G. LangeHesse. (Arch. elekt. Ubertragung, June \& July 1957, Vol. 11, Nos. 6 \& 7, pp. 253-261 \& 283-288.) A review article on observations of h.f. and v.h.f. reflections from the aurora, covering the state of research at the beginning of the I.G.Y. 92 references.

### 621.396.11: 621.396.677

Aerial/Propagation Mismatch.Hitchcock. (See 358.)
621.396 .11 .01

584
Terms and Symbols in the Field of Wave Propagation.-( Nachrichtentech. Z., May 1957, Vol. 10, No. 5, pp. 255-256.) Terms and symbols proposed by the special committee on wave propagation of the German Telecommunications Association (Nachrichtentechnische Gesellschaft) are tabulated with their definitions.

### 621.396.11.029.51/.53

585
The E.B.U. Project of Measurements for the Study of Sky-Wave Propagation in the Long- and Medium-Wave Bands. -H. Ehlers \& R. Dobiasch. (Rundfunktech. Mitt., June 1957, Vol. 1, No. 3, pp. 110120.) Details are given of the organization for the project and of the methods used, and some experiments and field-strength tests are described.
621.396.11.029.62/.63

586
Some Comparative Tests of Propagation Conditions in Bands II and IV.W.,Knöpfel. (Nachrichtentech. Z., May 1957, Vol. 10, No. 5, pp. 233-235.) Comparative measurements show that attenuation in band IV due to local causes and diffraction is greater than that obtained for band II. To ensure equally good coverage a closer spacing of transmitters of higher power appears necessary.

### 621.396.11.029.62

587
Experimental Investigations of the Mechanism of Long-Distance Propagation in the Metre Wavelength Range. -L. Klinker. (NachrTech., May 1957, Vol. 7, No. 5, pp. 210-215.) The results of one year's observations at Kühlungsborn are summarized (see also 2586 of 1957). The fading rate does not change appreciably over distances ranging from 50 to 400 km , and does not appear to depend on the mean turbulence velocity; however, a close correlation with the vertical drift component of tropospheric inhomogeneities was found. Partial reflections at layer inhomogeneities appears to be the predominant, if not exclusive, mechanism for propagation at $m \lambda$ for distances up to about 500 km .

## RECEPTION

### 621.376.332

588
F.M. Discriminator Bandwidth.G. J. Phillips. (Wireless World, Dec. 1957, Vol. 63, No. 12, pp. 571-574.) A significant reduction of co-channel interference by means of a wide-band discriminator is only obtained when the ratio of wanted to unwanted carriers is less than 6 dB . For normal conditions of broadcast reception a narrow-band discriminator and an a.m. suppression ratio of 35 dB are generally satisfactory. Other forms of interference are not improved by the use of a wide-band discriminator
621.396.621: 621.372.632

589
A Low-Noise Converter for Four Metres.-G. M. C. Stone.-(R.S.G.B. Bull., June 1957, Vol. 32, No. 12, pp. 54 1-543.) Full constructional details are given.
621.396.621: 621.373.4

590
A Stable Oscillator for Two-Metre Receivers.-W. H. Allen. (R.S.G.B. Bull., June 1957, Vol. 32, No. 12, pp. 544-545.)

### 621.396 .8 : 621.396 .712

591
The Fixing and Measurement of the Limits of Coverage of A.M. Broadcast Transmitters.-P. Thiessen. (Rundfunktech. Mitt., June 1957, Vol. 1, No. 3, pp 102-109.) It is proposed that the limit of the near fading zone should be determined on the basis of the statistical distribution of field strengths. The distribution of fluctuating field-strength amplitudes and phase displacements over two propagation paths is examined, and the relation between subjective assessments of quality, signal/noise ratio and field-strength fluctuations is discussed. See also 592 below.
621.396.8: 621.396.712.029.53 592
Statistical Investigation of the Quality of Reception of A.M.. Sound Broadcasts.-F. von Rautenfeld \& $P$ Thiessen. (Rundfunktech. Mitt., June 1957, Vol. 1, No. 3, pp. 90-101.) Results of a series of subjective and objective tests are statistically evaluated to assess the quality of reception in West Germany of the $100-\mathrm{kW}$ transmitter at Langenberg as affected by the $100-\mathrm{kW}$ transmitter at Hamburg; distant 315 km and operating at the same frequency $971 \mathrm{kc} / \mathrm{s}$, with or without reduced radiation towards Langenberg.

## Stations

## AND COMMUNICATION SYSTEMS

621.396 .1

Wavelengths as an International and Technical Problem.-W. Nestel. (Telefunken Ztg, Sept. 1957, Vol. 30, No. 117, pp. 161-173. English summary, pp. 216-217.) The characteristics of the various modes of wave propagation in the entire r.f. spectrum are summarized and their significance in the past and future planning of international frequency allocations is discussed:
621.396 .41 : 621.376 .3 : 621.396 .82

594
The Equalization of Base-Band Noise in Multichannel F.M. Radio Systems.C. A. Parry. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp. 1527-1534.) Preand de-emphasis noise-equalizing networks with a maximum attenuation slope of 6 dB /octave are discussed. Second-order distortion is assumed to be predominant. An improvement of signal/noise ratio of $3-6 \mathrm{~dB}$ is obtained in the top channel when the mean power of the multichannel signal is adjusted to be unaffected by the networks.
621.396.43.029.62/.63: 621.396.5

595
The Planning of Radio Link Networks for Metre and Decimetre Wave-lengths.-H. Paul. (Nachrichtentech. Z., Vol. 10, No. 5, pp. 223-233.) Planning aids in the form of slide rules or similar devices are described; they are based on the relevant C.C.I.F. recommendations.
621.396.65: 621.317.34

596
Measurement of Transmission Dis. tortion in F.M. Radio-Link Equipment. -Hartbaum. (See 552.)
621.396.65.029.63

597
A Decimetre-Wavelength Radio-Link Network providing High-Quality Program Channels using Pulse Phase Modulation.-(Telefunken Ztg, June 1957, Vol. 30, No. 116, pp. 85-118.)

Part 3-Modulation Equipment.-H. Oberbeck (pp. 85-99, English summary, p. 150).

Part 4 The Radio Equipment.-E. Willwacher (pp. 100-111, English summary, pp. 150-151).

Part 5-Equipment for Unattended Operation.-K. Hoffmann (pp. .111-118, English summary, p. 151).
Part 1: 3534 of 1956 (Brühl). Part 2 : 3283 of 1956 (Schüttlöffel)

## SUBSIDIARY APPARATUS

621.311 .6

598
Choke or Capacitor Input?- (Wireless World, Dec. 1957, Vol. 63, No. 12, pp 589-591.) Basic differences of operation and application of the two systems of power supplies are explained.
621.311 .62 : 621.314 .7

599
Design of Transistor Regulated Power Supplies.-R. D. Middlebrook. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp. 1502-1509.) Two applications of the circuit are described, one giving 0.5 A at $18-22 \mathrm{~V}$ and the other 1 A at $5-25 \mathrm{~V}$. Output resistance is about $0.01 \Omega$ and ripple on full load is less than 5 mV .

## $621.314 .63:[546.28+546.289 \quad \mathbf{6 0 0}$

Germanium and Silicon Power Recti-fiers.-T. H. Kinman, G. A. Carrick, R. G. Hibberd \& A. J. Blundell. (Proc. Instn elect. Engrs, Part A, Aug. 1957, Vol. 104, No. 16, pp. 327-330.) Further discussion on 2885 of 1956 .

## TELEVISION

AND PHOTOTELEGRAPHY

### 621.397 .26

601
Spectrum of Frequency-Shift Radio Photo-transmissions.-A. D. Watt. (Trans. Inst. Radio Engrs, Oct. 1956, Vol. CS-4, No. 3, pp. 27-40. Abstract, Proc. Inst. Radio Engrs, Jan. 1957, Vol. 45, No. 1, p. II2.)

### 621.397.61: 621.396.664 <br> 602

Transistors boost Video for TV Studio Monitors.-L. N. Merson. (Electronics, 1st Oct. 1957, Vol. 30, No. 10, p. 205.) Brief description of a compact transistor pre-amplifier unit.

### 621.397.611.2

603
Typical Transmission Characteristics of the Image Orthicon Television Camera Tube.-R. Theile \& F. Pilz. (Rundfunktech. Mitt., June 1957, Vol. 1, No. 3, pp. 77-85.) The performance and limitations of image orthicons are discussed (see also 2926 of 1957). Instructions for optimum methods of operation are tabulated ; some compromise is unavoidable and some faults can be reduced only by suitable lighting and arrangement of the scene.
621.397.62:525.623:621.317.7 604

Choosing a Colour-Bar Generator.Stamiti. (See 556.)

### 621.397.62: 621.317.7

 605Transistorized TV Pattern Gener-ator.-Rozner. (See 555.)

### 621.397.62: 621.373.52

606
A Transistorized Horizontal-Deffection System.-H. C. Goodrich. (RCA Rev., Sept. 1957, VoI. 18, No. 3, pp. 293307.) A horizontal-deflection system using only transistors is described consisting of an oscillator, driver; output stage with e,h.t.
supply, and phase detector. Audio-type power transistors operated beyond the manufacturer's ratings are used in the output stage, and the results indicate the desirable characteristics for an output transistor designed for this application.
621.397.62: 621.375.4

607
Transistor Receiver Video Ampli-fiers.-M. C. Kidd. (RCA Rev., Sept. 1957, Vol. 18, No. 3, pp. 308-321.) General design problems are discussed and a practical two-stage amplifier is described which uses drift-type transistors.

### 621.397 .621 .2

608
Improvements in Television Receivers: Part 4-Line Synchronization with Automatic Phase Control.-A. Boekhorst, B. G. Dammers, H. Heyligers \& A. G. W. Uitjens. (Electronic Applic. Bull., 1956/1957, Vol. 17, No. 4, pp. 129 -149.) An analysis of principles and practical requirements. New types of line timebase oscillator and phase discriminator, and a locking circuit are described. Parts 2 \& 3 : 3674 of 1957.

### 621.397 .7

609
The B.B.C. Riverside Television Studios: some Aspects of Technical Planning and Equipment.-H. C. Nickels \& D. M. B. Grubb. (B.B.C. Engng Div. Monographs, Oct. 1957, No. 14, pp. 5-31.)
621.397 .74 : 621.317.34 610

Waveform Testing Methods for Television Links.-A. R. A. Rendall. (Electronic Radio Engr, Dec. 1957, Vol. 34, No. 12, pp. 451-453.) A system of testing by means of three standard waveforms has been evolved. Acceptance limits are fixed in relation to subjective picture quality.

### 621.397 .743

611
Television Coverage in the German Democratic Republic using a New Unified Frequency Plan.-U. Kühn. (NachrTech., May 1957, Vol. 7, No. 5, pp. 215 220.) The allocation of channels according to C.C.I.R. recommendations is discussed.

### 621.397 .743

612
The Local Television Cable Network in West Berlin.-R. Hoffmann. (Nachrichtentech. Z., May 1957, Vol. 10, No. 5, pp. 209-214.) The design and the various facilities available are described.

### 621.397.743: 535.623

613
Transmission of Colour over NationWide Television Networks.-F. A. Cowan. (J. Soc. Mot. Pict. Telev. Engrs, May 1957, Vol. 66, No. 5, pp. 278-283.) Coaxial and radio relay systems in the U.S.A. are described and their operation is discussed
621.397 .8

614
Minimizing the Effects of Ambient Light on Image Reproduction.-G. L. Beers. (J. Soc. Mot. Pict. Teleo. Engrs, June 1957, Vol. 66, No. 6, pp. 347-354. Discussion, pp. 353-354.) In the method described an oscillating honeycomb screen placed in front of the picture tube prevents light from sources outside a predetermined viewing angle from degrading the image.

## TRANSMISSION

621.396.61/.62: 621.316 .726

615
'Autosync' Frequency Control.-R. J Moser. (QST, June 1957, Vol. 41, No. 6, pp. 11-16.) Outputs taken from the mixer and b.f.o. of a commercial receiver are mixed and the resulting frequency is used to control an s.s.b. transmitter, which is thus automatically kept in tune with the receiver
621.396.61: 62I.396.664

616
Central Supervisory Equipment for Broadcast Transmitters.-H. Müller. (Telefunken Ztg, Sept. 1957, Vol. 30, No. 117, pp. 196 200. English summary, p. 218.) A monitoring installation is described for supervising and modulating up to 10 medium- and short-wave transmitters from one control centre.
621.396.61: 621.396.82

617
Reduction of Adjacent-Channel Interference from On-Off Keyed Carriers.A. D. Watt, R. M. Coon \& V. J. Zurick (Trans. Inst. Radio Engrs, Oct. 1956, Vol. CS-4, No. 3, pp. 4I-58.)

### 621.396.61.005

618
High-Power Broadcast Transmitters for Medium Waves.-A. Ruhrmann. (Telefunken Ztg, Sept. 1957, Vol. 30, No. 117, pp. 185-195. English summary, pp. 217218.) Novel features of recently installed transmitters are described.
621.396.61.029.63: 621.397.8

619

### 621.396.11.083

A 12-kW Pulse Transmitter for Propagation Tests in Band IV.-P. Mallach. (Rundfunktech. Mitt., June 1957, Vol. I, No. 3, pp. 86-89.) According to the type of directional aerial used, the transmitter described has an effective radiated power of up to 700 kW with $0 \cdot 03-0 \cdot 1-\mu \mathrm{s}$ pulse length at a repetition frequency of $15 \cdot 625 \mathrm{kc} / \mathrm{s}$. Various applications of the equipment and planned refinements are discussed with examples of results so far achieved.

### 621.396.61.07

620
Power Supply, Control and Protective Equipment [for high-power transmitters]. -P. G. Zehnel. Telefunken Ztg, Sept. 1957, Vol. 30, No. 117, pp. 201-206. English summary, p. 218.) Details of recent installations, including remote-control equipment, are given. See also 1588 of 1957 (Burkhardtsmaier).
621.396.712: 621.398

621
The Remote and Automatic Control of Semi-attended Broadcasting Trans-mitters.-R. T. B. Wynn \& F. A. Peachey. (Proc. Instn elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, pp. 529-539.) Discussion, pp. 549-552.) Techniques developed by the B.B.C. for controlling semi-attended transmitting stations are described. The performance of the stations is analysed and the economics of the system discussed. Considerable financial saving in operating costs is achieved without sacrifice of broadcasting continuity.

The Design of High- and Low-Power Medium-Frequency Broadcasting Transmitters for Automatic and Semiattended Operation.-W. J. Morcom \& D. F. Bowers. (Proc. Instn elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, pp. 540549. Discussion, pp. 549-552.) Two m.f. transmitters are described having power outputs of 660 W and 100 kW respectively. Three of the low-power units are used in parallel to provide a $2-\mathrm{kW}$ fully automatic transmitter. Two high-power units can be used as a semi-attended $200-\mathrm{kW}$ transmitter. See also 621 above.

## Valves and thermionics

### 537.533

 623Simplified Methods in the Statistical Mechanics of Stationary Electron Beams.-B. Meltzer. (J. Electronics Control, Oct. 1957, Vol. 3, No. 4, pp. 355366.) A mathematical analysis of the effects produced in an electron beam by statistical variations in the initial velocities either of thermionic or secondary emission electrons. Axial symmetry is assumed, but the statistical distribution of initial energies is not limited only to the Maxwellian type. Current density, electron temperature and focusing are discussed, and comparisons are made with experimental results for a television camera tube.
621.314 .63 : 537.311 .33

624
On the Impact Ionization in the Space-Charge Region of $\boldsymbol{p}-\boldsymbol{n}$ Junctions. -F. W. G. Rose. (J. Electronics Control, Oct. 1957, Vol. 3, No. 4, pp. 396-400.) The Townsend equation for impact ionization in semiconductors is shown to be invalid at low voltages in the space charge region of $p-n$ junctions. 'Soft' breakdown must precede Townsend breakdown, although its effect on the characteristic will be masked by surface effects.
621.314.63:546.289

625
Thermal Turnover in Germanium $\boldsymbol{p - n}$ Junctions.-A. W. Matz. (Proc. Instn elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, pp. 555 564.) Static reverse characteristics are analysed, taking into account an avalanche multiplication factor. Examination of the condition for thermal stability relates the onset of thermal runaway to a thermal turnover phenomenon. The existence of a thermal negative resitance region is predicted and verified experimentally, a semi-quantitative analysis of the results shows reasonable agreement with theory.
621.314 .7

626
The Role of Transistors in Elec-tronics.-R. B. Hurley. (J. Soc. Mot. Pict. Telêv. Engrs, June 1957, Vol. 66, No. 6, pp. 330-332. Discussion, p. 332.) The advantages of transistors over valves and other devices are summarized.

Transistor Circuits and Applications. -A. G. Milnes. (Proc. Instn elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, pp. 565-580. Discussion, pp. 581-585.) A review paper which deals with junction transistors; new concepts and trends in design are cliscussed. The applications described include low-level and power amplifiers, square-wave and sinusoidal oscillators, power regulators, and computing and switching circuits, but special types such as tetrodes, $p-n-p-n$ and unipolar devices are not considered. 112 references.
621.314 .7

628
D.C. Stabilization of Junction Tran-sistors.-L. B. Johnson \& P. Vermes. (Mullard tech. Commun., April 1957, Vol. 3, No. 23, pp. 67-96. Electronic Applic. Bull., 1956/1957, Vol. 17, No. 4, pp. 151-177.) The need for stabilization of d.c. operating conditions against temperature variations is pointed out. Detailed consideration is given to the most useful methods of achieving such stability. The effects of production spreads in transistor parameters on the design of stabilizing ci cuity are discussed.

### 621.314 .7

629
Theory of a Wide-Gap Emitter for Transistors.-H. Kroemer. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp . 1535-1537.) The injection deficit ( $1-\gamma$ ), where $\gamma$ is the emitter efficiency, can be increased by several orders of magnitude if the emitter has a higher band gap than the base region.
621.314 .7 : 621.317.332 $\quad 630$

Measurements of the Impedance Parameters of Junction Transistors.Ward. (See 550.)
621.314.7: 621.317 .799

Test Equipment for Transistor Pro-duction.-A. B. Jacobsen \& C. G. Tinsley. (Electronics, lst Cct. 1957, Vol. 30, No. 10, pp. 148-151.)

## $621.314 .7: 621.375 .4: 681.142 \quad 632$

Transistors in Current - Analogue Computing.-Kerfoot. (See 372.)

### 621.314.7: 621.385 .4

633
High-Frequency Semiconductor Spacistor Tetrodes.-H. Statz, R. A. Pucel \& C. Lanza. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45 , No. 11, pp. 1475-1483.) Electrons are injected into the space-charge region of a reversed-biased $p-n$ junction from an emitter contact on its surface. This input current is modulated by the voltage applied to an adjacent reverse-biased contact. Carrier transit in the space-charge region is rapid and practically unaffected by lifetime considerations. The input and output impedances of experimental units are as high as $30 \mathrm{M} \Omega$. See also 1947 of 1957 (Statz \& Pucel).
621.314.7: 621.396 .822

634
Shot Noise in Transistors.-G. H. Hanson \& A. van der Ziel. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp. 1538-1542.) Experimental results over a frequency range which greatly exceeds the transistor cut-off frequency in some cases, are interpreted in terms of a recent theory by van der Ziel ( 600 of 1956). Reasonable agreement is obtained.

The Equivalent Circuit of the Drift Transistor.-J. Almond \& R. J. McIntyre. (RCA Rev., Sept. 1957, Vol. 18, No. 3, pp. 361-384.) The quadripole admittances of a drift transistor, as given by Krömer (3389 of 1954), are examined as functions of frequency and used to derive $\Pi$-type equivalent circuits for common-base and common-emitter configurations. The frequency variations of the admittance elements used in these circuits are compared with those of the admittance functions they represent, and are shown to give good approximations up to frequencies of the order of the $\alpha$-cut-off frequency of the intrinsic transistor. The differences in the behaviour of the phase of $\alpha$ for diffusionand drift-type transistors in grounded-base connection is discussed qualitatively.

### 621.383.2: 546.34

636
Use of Lithium in Photoemissive Cathodes.-A. H. Sommer. (Rev. sci. Instrum., Aug. 1957, Vol. 28, No. 8, pp. 655-656.) A discussion of measurements of peak sensitivity and long-wavelength threshold and an interpretation of earlier results.
621.383 .27 637
On the Mechanism of the Production of Dark-Current Pulses in Photomulti-pliers.-Z. Náray \& P. Varga. (Brit. J. appl. Phys., Sept. 1957, Vol. 8, No. 9, pp. 377-379.) The predominant component of the dark current is produced by different mechanisms in the negative and positive regions of the shield characteristic. In the former case electrons are emitted from the envelope, and in the latter case electrons from the inner electrodes produce scintillations on the envelope, giving rise to photon feedback.
621.383 .5

638
Theoretical Interpretation of Hama-ker-Beezhold Ballistic Effect in BarrierLayer Photocells.-G. Blet. (J. Phys. Radium, Jan. 1957, Vol. 18, No. 1, pp. 5-8.) The theory of statistical exchanges between traps and electrons is developed to explain the build-up and decay effects observed under different conditions of illumination. See 312 of 1957 (Blet \& Ritti).

### 621.385.029.6

639
International Congress on Microwave Valves.-(Le Vide, Jan./Feb. 1957, VoI. 12, No. 67, pp. 1-146.) A further selection of papers, as follows, presented at the Congress. See also 1267 of 1957.
(a) Some Technological Aspects of U.H.F. Triode Design.-E. G. Dorgelo (pp. 3-8, in French \& English).
(b) Some Problems on Disk-Sealed Planar Triodes.-H. Nishio, T. Nemoto \& H. Murakami (pp. 9-22, in French \& English).
(c) Construction and Circuit of a $4000-$ $\mathrm{Mc} / \mathrm{s}$ Triode with L Cathode.-K. Rodenhuis (pp. 23-31, in French \& English).
(d) The Space Charge Distribution in a Magnetron under Static Conditions.-J. Verweel (pp. 32-42, in French \& English).
(e) Power and Gain Limitations of HelixType Travelling-Wave Tubes.-C. W. Barnes (pp. 43-48, in French \& English).
(f) Helix Type Travelling-Wave Valve for $24 \mathrm{Gc} / \mathrm{s}$.-T. Miwa, J. Koyama, M. Mishima \& I. Yanaoka (pp. 49-52, in French \& English).
(g) Low Noise Travelling-Wave Valve: ECL1138.-M. Higuchi, K. Kawazura \& J. Koyama (pp. 53-58, in French \& English).
(h) Magnetless Magnetron.-A. Versnel (pp. 59-63, in French \& English).
(i) A New Electron Lens System providing Convergent-Divergent Action.-T. Seki, Y. Nikaido \& K. Simada (pp. 64-73, in French \& English).
(j) The Design of an Electron Gun for a Strip Beam Device-A. B. Cutting \& I. Fraser (pp. 74-82, in French \& English).
(k) Transmit-Receive Switch Tubes.M. L. W. Roberts (pp. 83-92, in French \& English).
(l) Plug-In T.R. Tubes for use in S-Band Duplexers.-T. L. Dutt (pp. 93-108, in French \& English).
( $m$ ) High-Power Duplexers.-L. Milosevic (pp. 109-116).
(n) Investigation of Pressures and their Evolution in Gas-Filled Valves.-J. Boissière \& C. Romiguière (pp. 117-121).
(o) Power Measurements on MillimetreWave Valves.-H. Weill (pp. 122-127).
( $p$ ) Electron Deflection System of Travel-ling-Wave Cathode-Ray Tube.-H. Maeda \& K. Miyaji (pp. 128-140, in French \& English).
(q) High-Melting-Point Seals.-R. Benichou (pp. 141-146).

### 621.385.029.6

640
Biperiodic Electrostatic Focusing for High-Density Electron Beams.-K.K.N. Chang. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp. 1522-1527.) The potential valley formed by combining two counteracting periodic electrostatic fields is theoretically steeper than in previous focusing systems and should maintain stable flow in thick hollow beams. Proper cancellation of the space-charge field is also obtained. Preliminary experiments indicate that a travelling-wave valve can operate without using any magnets. See also 1954 of 1957.
621.385.029.6: 621.3.072.6

641
Automatic Frequency Control for a Pulsed Klystron.-P. D. Ulm. (Elect. Commun., June 1957, Vol. 34, No. 2, pp. 136-140.) The klystron frequency is compared with that of a stable microwave resonator. The frequency-error information derived from one pulse is delayed and applied to correct the next.

### 621.385.029.6: 621.372.8

642
Delay-Line Valves.-F. W. Gundlach. (Nachrichtentech. Z., June 1957, Vol. 10, No. 6, pp. 265-276.) A theory is derived for valves containing periodic waveguide structures. It is similar to recurrent-network theory and accounts for the properties of the valve in both forward and backward operation.

### 621.385.029.64

643
Slalom Focusing.-J. S. Cook, R. Kompfner \& W. H. Yocom. (Proc. Inst. Radio Engrs, Nov. 1957, Vol. 45, No. 11, pp. 1517-1522.) A linear array of line charges produces two equipotential surfaces which contain exact electron trajectories.

Such a field is obtained by placing an array of positive wires between two negative plates; this structure can focus a ribbontype electron beam. A backward-wave oscillator with this slalom focusing generated oscillations in the range $3 \cdot 3.4 \cdot 3 \mathrm{kMc} / \mathrm{s}$.

### 621.385.029.65

644
A Versatile Source of Millimetre Waves.-C. F. Hempstead \& A. R. Strnad. (Bell Lab. Rec., July 1957, Vol. 35, No. 7, pp. 241-245.) A number of simplifications in design and improvements in fabrication of backward-wave oscillators are described, including a re-designed electron gun assembly. The latest versions of the back-ward-wave oscillator deliver $5-10 \mathrm{~mW}$ at between 45000 and $57000 \mathrm{Mc} / \mathrm{s}$; oscillation has been achieved at $200000 \mathrm{Mc} / \mathrm{s}$.

### 621.385.032.213: 537.533

645
On the Electron Gun with Hairpin Cathode: the Intensity of Emission and the Nature of the Electron Source. -K. T. Dolder \& O. Klemperer. ( $J$. Electronics Control, Nov. 1957, Vol. 3, No. 5, pp. 439-454.) Emission per unit solid angle is maximum for zonal rays when grid bias is just sufficient to prevent multiple source formation and cathode-to-grid distance is of the order of one grid-aperture radius. Experiments show that emission can be direct from the cathode tip, or pass through a cross-over, or be drawn from a virtual cathode. The last condition yields the highest emission over a relatively large solid angle.
621.3.032.213.13

Barium-Supplied Oxide-Coated Cath-odes.-T. Imai. (J. phys. Soc. Japan, July 1957, Vol. 12, No. 7, p. 831.) The beneficial effects on emission of excess Ba in the coating layer of oxide-coated cathodes are described and methods of introducing the Ba are discussed.
621.385.032.213.13

647
Activation of an Oxide Cathode by Deposition of Alkaline Earth Metal Ions via a Mass Spectrometer.-R. M. Matheson, L. S. Nergaard \& R. H. Plumlee. ( RCA Rev., Sept. 1957, Vol. 18, No. 3, pp. 385-431.)
621.385.032.213.13

648
: 621.317.332.029.63
The Impedance of the Oxide-Coated Cathode at Ultra-high Frequencies.L. J. Herbst. (Brit. J. appl. Phys., July 1957, Vol. 8, No. 7, pp. 277-282.) The impedance of the cathode was measured on a number of disk-seal triodes at frequencies between 500 and $2365 \mathrm{Mc} / \mathrm{s}$.
621.385.032.213.13: 621.327.5

649
The Emission from Oxide Cathodes in Low-Pressure Discharges.-M. A. Cayless. (Brit. J. appl. Phys., Aug. 1957, Vol. 8, No. 8, pp. 331-336.) Cathodes in fluorescent lamps are considered. The zero-field emission at a pressure of a few mm is found experimentally to be about 10 times that in a vacuum. Various processes of field and secondary emission are described.

### 621.385.032.213.2

650
The Effect of Oxygen and Sulphur on the Thermionic Emission from Matrix Cathodes.-J. F. Richardson. (Brit. J.
appl. Phys., Sept. 1957, Vol. 8, No. 9, pp. 361-362.) "The poisoning of the emission from matrix cathodes by oxygen and sulphur is reversible. Recovery of the emission is more rapid from oxygen poisoning. The shape of the recovery curves indicates that the poisoning agent is present on the surface and has also diffused into the cathode pores."
621.385.032.26:537.533

651
Exact Electrode Systems for the Formation of a Curved Space-Charge Beam.-R. J. Lomax. (J. Electronics Control, Oct. 1957, Vol. 3, No. 4, pp. 367-374.) An analytical method of determining the shape of the Pierce-type electrodes required to maintain a two-dimensional space-charge beam is given, which is valid when the edge of the beam is curved. The method is applied to a solution of the space-charge equations given by Meltzer ( 957 of 1957); this leads to a completely enclosed electrode system.
621.385.1.01

652
Recommendations of the Special Committee on Valves of the N.T.G. (Nachrichtentechnische Gesellschaft) concerning Definitions in the Field of High-Vacuum Diodes and Grid-Controlled Vacuum Tubes.- (Nachrichtentech. Z., May 1957, Vol. 10, No. 5, pp. 257-262.) Many of the German terms and definitions given are based on those recommended by the I.R.E. Committee on Electron Tubes.
621.385.2: 621.3.011.4

653
The Capacitance between Diode Electrodes in the Presence of Space Charges. -I. A. Harris: C. S. Bull. (Proc. Instn. elect. Engrs, Part B, Nov. 1957, Vol. 104, No. 18, p. 598.) Comment on 3357 of 1957 and author's reply.
621.385.3.029.63

654
The Design and Life of Planar Microwave Transmitting Tubes.-H. D Doolittle. (Trans. Inst. Radio Engrs, May 1957, Vol. PGVC-8, pp. 31-35. Abstract, Proc. Inst. Radio Engrs, July 1957, Vol. 45, No. 7, p. 1039.)

### 621.387 : 621.3.015.532

655
The Corona Triode.-G. A. Ostroumov. (Dokl. Ak. Nauk S.S.S.R., 11 th Aug. 1957, Vol. 115, No. 5, pp. 919-921.) The principle and circuit of an amplifying device is described which consists of a sharp point and a blunt electrode as anode with a high voltage between them, so that a corona is formed. For operation at high voltages the anode is of a tubular shape. See also 2927 of 1956 (Hertz).

## MISCELLANEOUS

### 621.3.002.2/.3

656
Miniaturization of Electronic Equip-ment.-D. A. Findlay. (Electronics, Ist Cct. 1957, Vol. 30, No. 10, pp. 177-204.) A report dealing with design and materials, various classes of components, and production techniques.

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|  | GA61-A | 106 | 94 | 2.0 at $60^{\circ} \mathrm{C}$ | $3 \frac{1}{2}$ |
|  | GA52-A | 340 | 303 | 2.0 at $40^{\circ} \mathrm{C}$ | 5 |
|  | GA62-A | 170 | 151 | 2.0 at $60^{\circ} \mathrm{C}$ | 5 |
|  | GA53-A GA63-A | $\begin{aligned} & 510 \\ & 254 \end{aligned}$ | $\begin{aligned} & 455 \\ & 227 \end{aligned}$ | $\begin{aligned} & 2.0 \text { at } 40^{\circ} \mathrm{C} \\ & 2.0 \text { at } 60^{\circ} \mathrm{C} \end{aligned}$ | $6 \frac{1}{2}$ $6 \frac{1}{2}$ |
|  | GB3I-A | 140 | 188 | 3.0 at $35^{\circ} \mathrm{C}$ | $4 \frac{5}{88}$ |
|  | GB4I-A | 53 | 71 | 3.0 at $55^{\circ} \mathrm{C}$ | $4 \frac{5}{88}$ |
|  | GB51-A | 210 | 283 | 3.0 at $35^{\circ} \mathrm{C}$ | $4 \frac{5}{8}$ |
|  | GB61-A | 106 | 143 | 3.0 at $55^{\circ} \mathrm{C}$ | $4 \frac{5}{8}$ |
|  | GB52-A | 340 | 458 | 3.0 at $35^{\circ} \mathrm{C}$ | $6 \frac{3}{4}$ |
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